

CAE 464/517 HVAC Systems Design

Spring 2023

March 21, 2023

Air distribution systems: Duct design

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ANNOUNCEMENTS

Announcements

- Assignment 4 is posted (due next week)
- Do not forget to work on Project Part 2

IIT-BIM Collaborate • CAE 464_sp23 Group 5



Welcome to CAE 464_sp23 Group 5

Mohammad Heidarinejad,
Mohammad Heidarinejad added you as a project admin to CAE 464_sp23 Group 5.

If you can't access the project, [contact Mohammad Heidarinejad](#), the project administrator who invited you to this project.

[Go to your project](#)

Announcements

- Final project presentation:
 - May 4, 8 am to 10 am
 - Location: Hermann Hall
 - All students are are required to present

Announcements

- Do not forget to review the Q&A file:

SUMMARY	+
<hr/>	
OUTLINE	
— CAE 464/517 Spring 2023 Q&As	
Project Part 1	
Assignment 3	
Assignment 2	
Assignment 1	
Midterm Exam 1	

CAE 464/517 Spring 2023 Q&As

Project Part 1

Question: After class when we spoke with you, you mentioned that the maximum amount of space types we should use is 4. We came up with:
Corridor/Transition
Operating/Patient Room
Office
Lounge/Recreation
as per ASHRAE common space types for hospitals.

https://docs.google.com/document/d/1m6ezSl6Bi9wGQcjnaYj_iAXY2kzRICPYWkKfayNp5WE/edit#heading=h.7xv0zdhfny5a

Ductwork in Practice

- Adding interesting and daily application of HVAC systems:

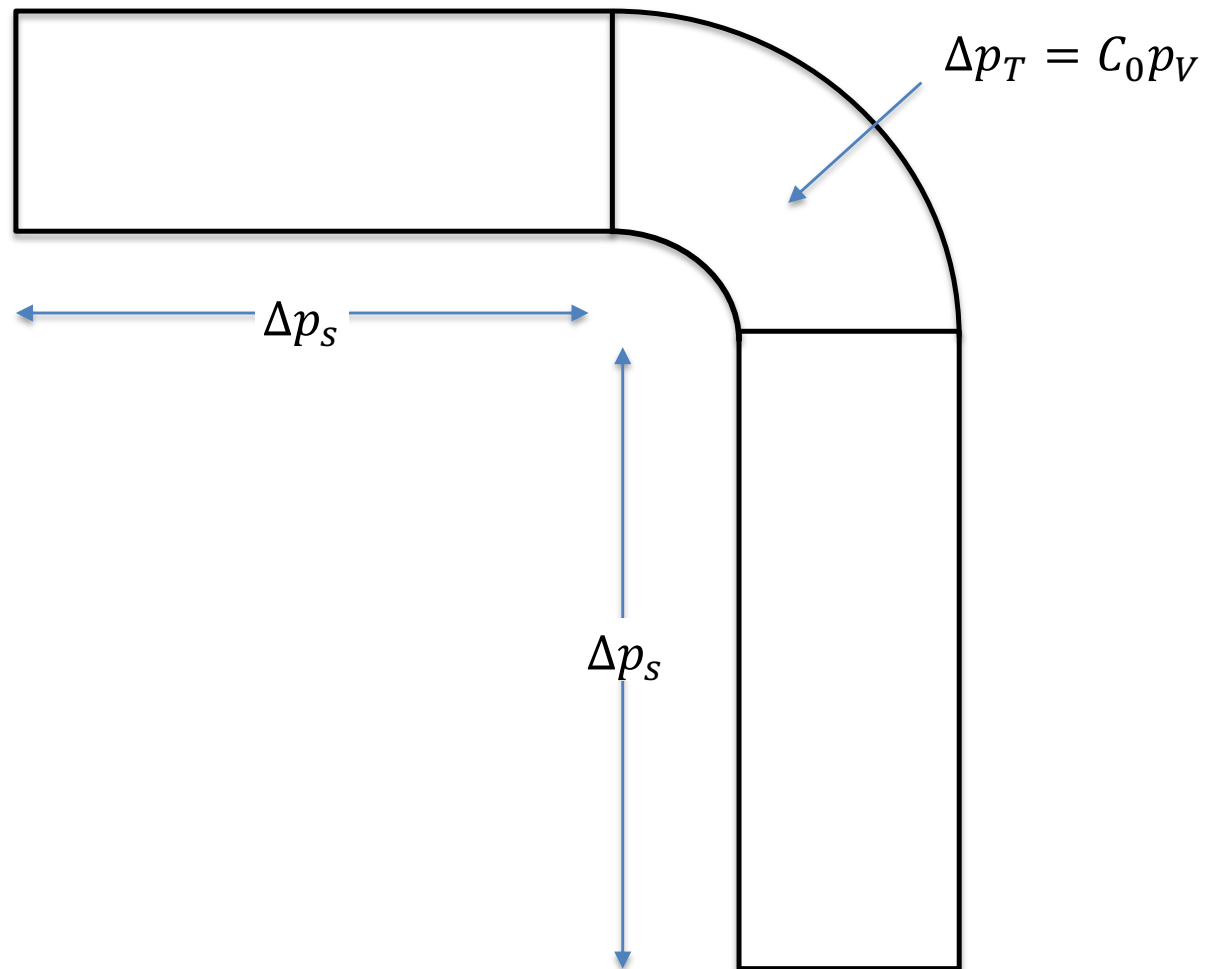
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RECAP

Recap

- Pressure drop calculations (elbows and transitions)

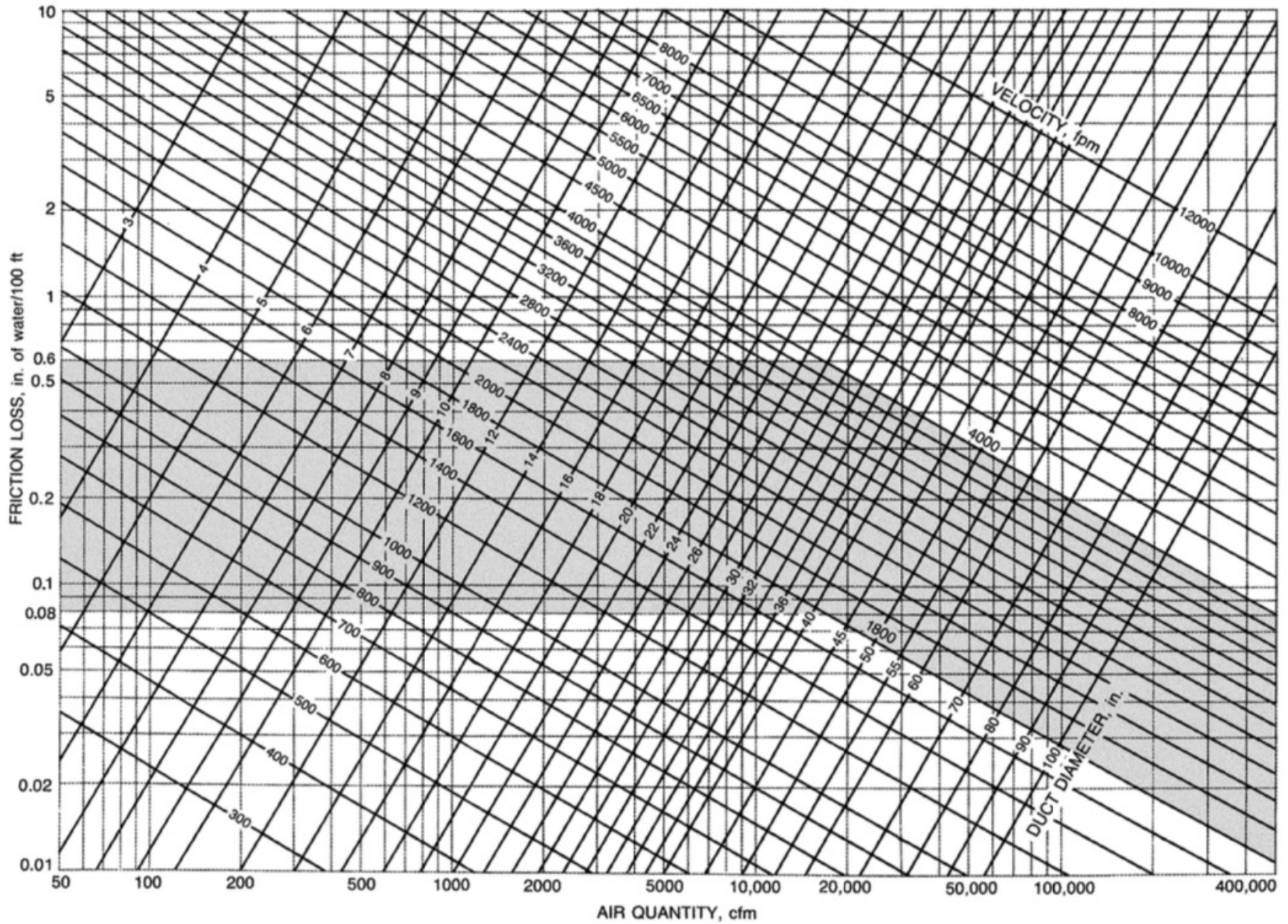


Recap

$$p_{v,o} = \left(\frac{V_o}{4,005} \right)^2$$

Duct velocity V_o (fpm)	Duct pressure p_v (in w.c.)
4,000	1.00
3,000	0.56
2,000	0.25
1,000	0.06

Recap



Recap

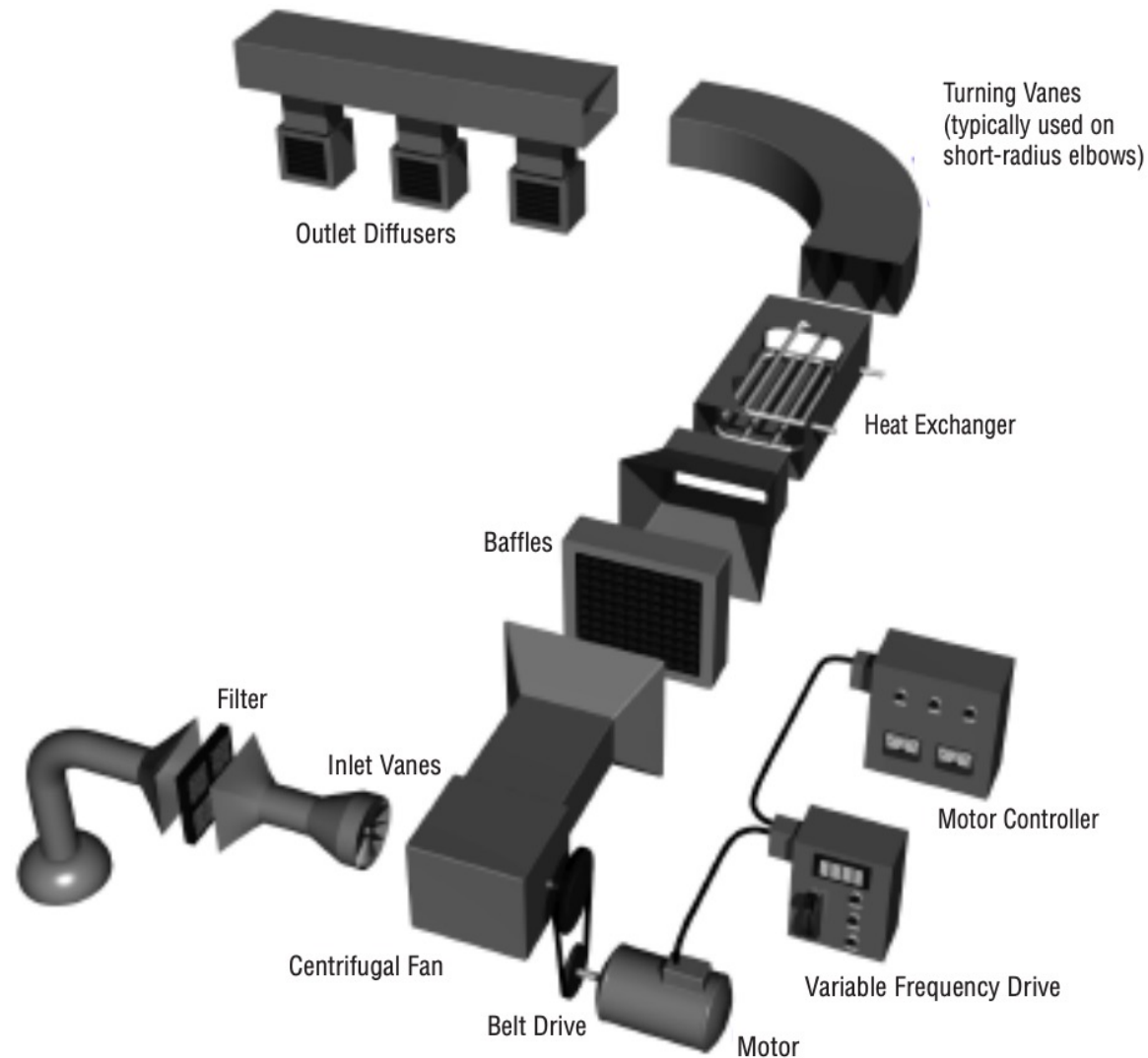
- See Table 12 for the recommended maximum airflow velocities:

Table 12 Recommended Maximum Airflow Velocities to Achieve Specified Acoustic Design Criteria*

Duct Location	NC or RC Rating in Adjoining Occupancy	Maximum Airflow Velocity, fpm	
		Rectangular Duct	Round Duct
1	2	3	4
In shaft or above solid drywall ceiling	45	3500	5000
	35	2500	3500
	25 or less	1500	2500
Above suspended acoustical ceiling	45	2500	4500
	35	1750	3000
	25 or less	1000	2000
Duct within occupied space	45	2000	3900
	35	1450	2600
	25 or less	950	1700

Ductwork in Practice

- The air distribution includes various components:



Recap

- You can use other resources (e.g., Chapter 8 of the Price Industries Handbook)
- Older version of ASHRAE Handbook

Recap

- Some common fitting terminology are:

Fitting Function	Geometry	Category	Sequential Number
S: Supply	D: Round (Diameter)	1. Entries 2. Exits	1, 2, 3, ...
E: Exhaust / Return	R: Rectangular	3. Elbows 4. Transitions	
C: Common (supply/ return)	F: Flat oval	5. Junctions 6. Obstructions	
		7. Fan and system interactions	
		8. Duct-mounted equipment	
		9. Dampers	
		10. Hoods	

DUCT DESIGN METHODS

Duct Design Methods

- Codes & standards
- Airflow rates
- Single line ductwork
- Size ductwork
- Calculate pressure drop
- Establish system total pressure

Duct Design Methods

- There are different duct design methods:
 - ❑ **Equal friction:** Size based on chosen friction loss rate (per 100 ft) for each duct section to balance the pressure gradient (commonly used)
 - ❑ **Equal velocity:** Size based on maintaining a constant velocity for duct sections (applicable for simple or industrial systems to carry particles out)
 - ❑ **Balanced capacity:** Equal pressure drops from fan to outlets of each branch (e.g., VAV systems)
 - ❑ **Static regain:** Duct size at the fan is selected using the friction chart to get the starting velocity. Other main ducts are sized to achieve static regain from section to section, meaning keep static pressure same throughout a system

Duct Design Methods

- The velocity classifications are important:

Method	Velocity	Velocity Range	Pressure Drop
Equal friction	Low Velocity	Less than 2500 fpm (13 m/s)	Less than 0.15 in./100 ft (1 Pa/m) [0.1 in./100 ft is a common value]
Equal velocity			
Balanced capacity			
Static regain	High Velocity	Up to 4500 fpm (23 m/s)	Less than 0.7 in./100 ft (4.7 Pa/m)

Duct Design Methods

- When do we use high velocity design?
 - When the heating or cooling loads are large (e.g., commercial buildings)
 - Special considerations are required (e.g., balancing and leakage control)

Duct Design Methods

- When do we use low velocity design?
 - When the low flow rate is adequate, and it is possible to run large ductwork
 - Can achieve low fan energy use

EQUAL FRICTION METHOD

Equal Friction Method

- The design friction rate per unit length (in. w.c per 100 ft) is maintained
- The aim is to design a well-balanced system
- If the layout is symmetrical and all runs from fan to diffuser approximately the same length this method works well

Equal Friction Method

- However, in most duct systems, there are variety of duct runs from long to short.
- Thus, short runs need to use balancing dampers in order to balance the flow rate to each space, which can cause considerable noise

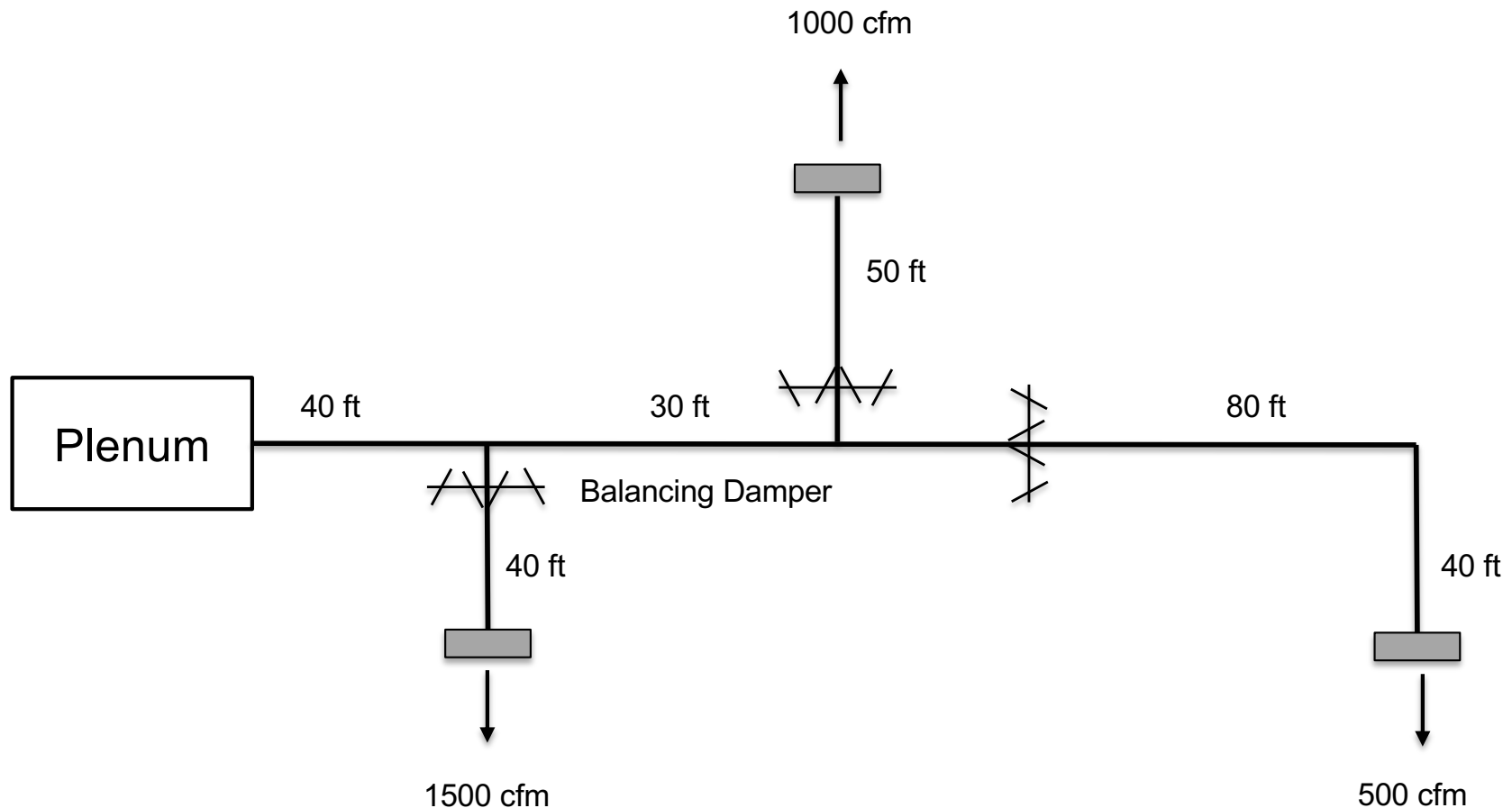
Equal Friction Method

- The design friction rate depends upon the velocity allowable in the system
- Start from usually know flow rates adjacent to the fan to establish the lost pressure per unit of length
- After sizing the designer need to compute the total pressure loss of the longest run with the consideration of all fittings

Equal Friction Method

- **Example:**

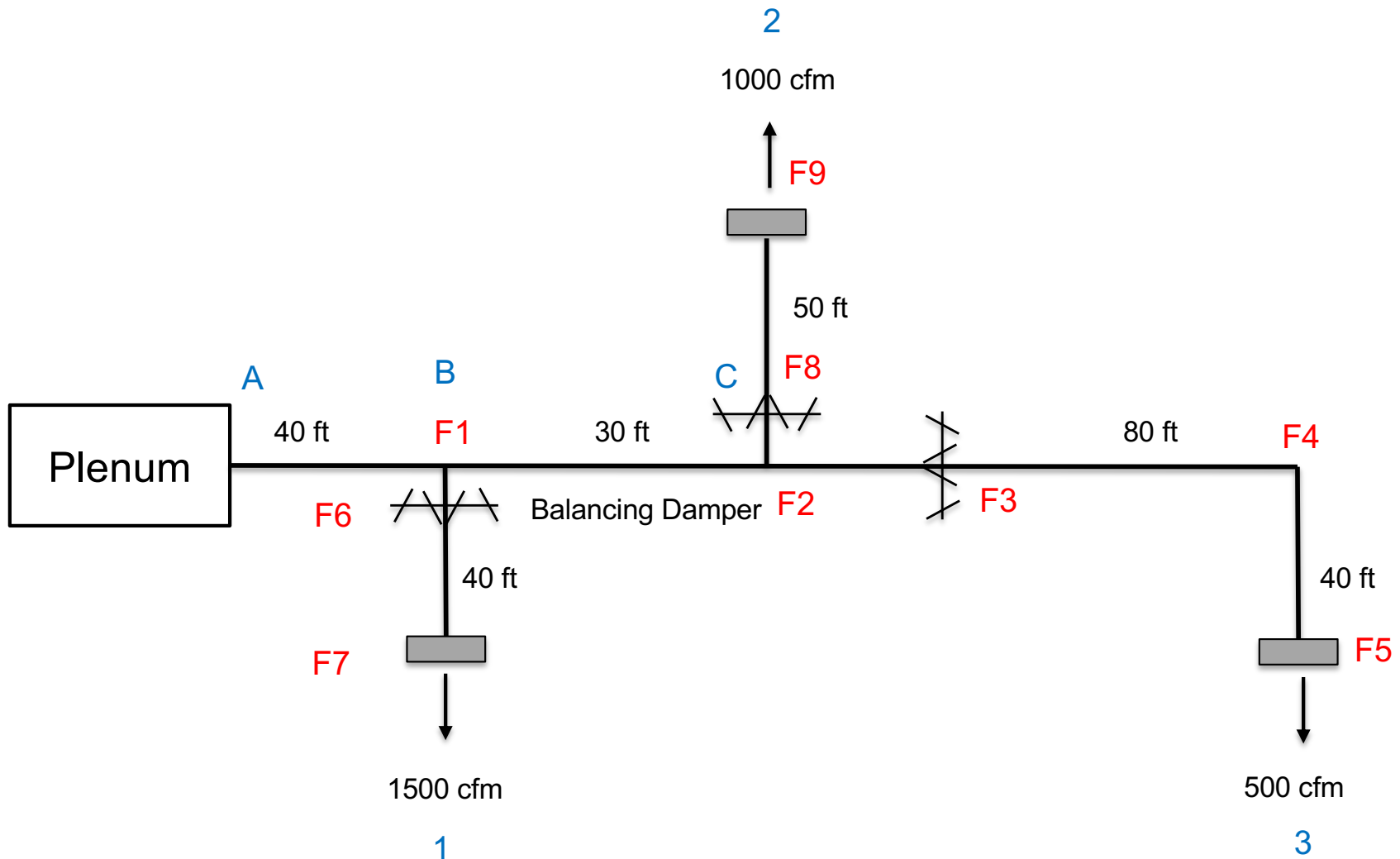
- ❑ Loss for each outlet is 0.05 in. w.c.
- ❑ Maximum velocity mains = 1,300 fpm, branches = 900 fpm
- ❑ Uniform pressure loss/100 ft and for elbows $r/W = 1.0$



Equal Friction Method

- **Solution:**

- Add labels for different branches and fittings



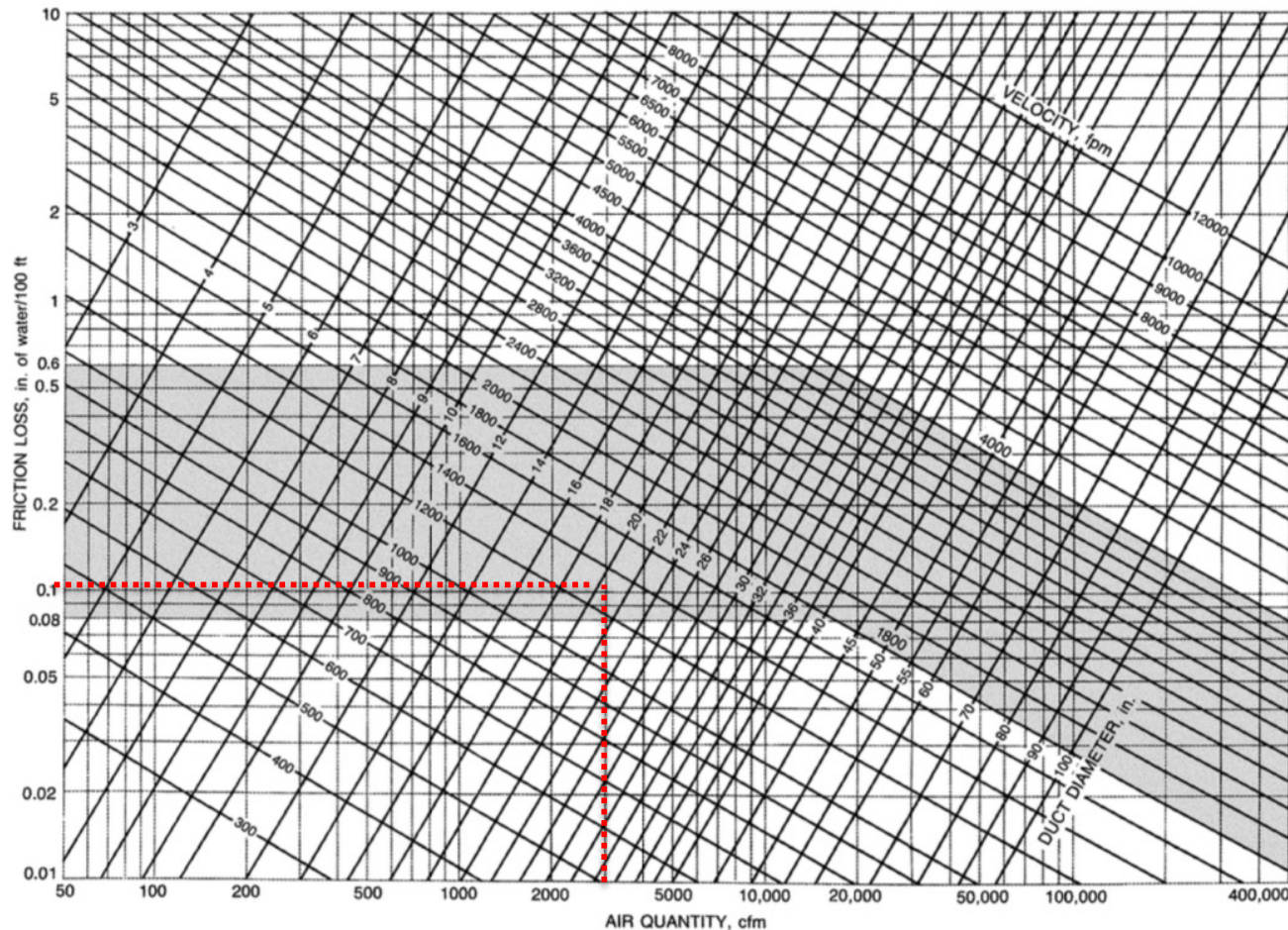
Equal Friction Method

- **Solution:**

- Estimate the equal friction method

$$Q_{main} = 500 \text{ cfm} + 1500 \text{ cfm} + 1000 \text{ cfm} = 3000 \text{ cfm}$$

$$V_{max} = 1300 \text{ fpm}$$



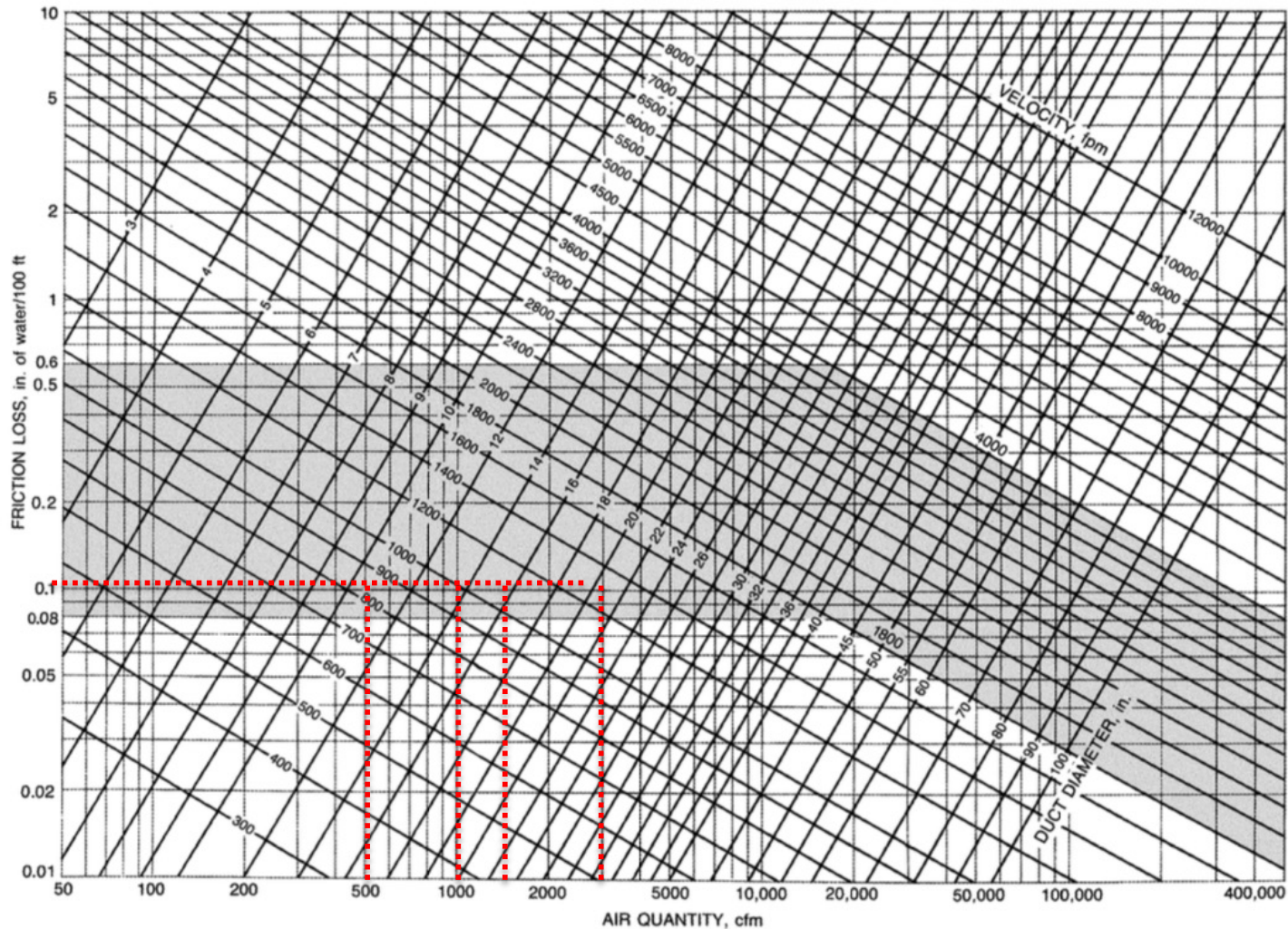
Equal Friction Method

- **Solution:**
 - Construct a tabular air flow

Section	Air Flow Rate (cfm)	Duct Size (in)	Duct (in Rectangular)	Velocity (fpm)
AB	3,000			
BC	1,500			
B1	1,500			
C2	1,000			
C3	500			

Equal Friction Method

- **Solution:**
 - Find round diameters and velocities



Equal Friction Method

- **Solution:**
 - Add the duct sizes and velocity rates

Section	Air Flow Rate (cfm)	Duct Size (in)	Duct (in Rectangular)	Area (ft ²)	Velocity (fpm)
AB	3,000	21			1,059
BC	1,500	16			1,000
B1	1,500	16			1,000
C2	1,000	14.5			750
C3	500	11			600

Equal Friction Method

- Solution:**

- Find square duct sizes

Circular Duct Diameter, in.	Length of One Side of Rectangular Duct (<i>a</i>), in.																			
	4	5	6	7	8	9	10	12	14	16	18	20	22	24	26	28	30	32	34	36
	Length Adjacent Side of Rectangular Duct (<i>b</i>), in.																			
5	5																			
5.5	6	5																		
6	8	6																		
6.5	9	7	6																	
7	11	8	7																	
7.5	13	10	8	7																
8	15	11	9	8																
8.5	17	13	10	9																
9	20	15	12	10	8															
9.5	22	17	13	11	9															
10	25	19	15	12	10	9														
10.5	29	21	16	14	12	10														
11	32	23	18	15	13	11	10													
11.5		26	20	17	14	12	11													
12		29	22	18	15	13	12													
12.5		32	24	20	17	15	13													
13		35	27	22	18	16	14	12												
13.5		38	29	24	20	17	15	13												
14			32	26	22	19	17	14												
14.5			35	28	24	20	18	15												
15			38	30	25	22	19	16	14											
16			45	36	30	25	22	18	15											
17				41	34	29	25	20	17	16										
18				47	39	33	29	23	19	17										
19				54	44	38	33	26	22	19	18									
20					50	43	37	29	24	21	19									
21					57	48	41	33	27	23	20									

→ C-3

→ C-2

→ B-C

→ A-B

Equal Friction Method

- **Solution:**

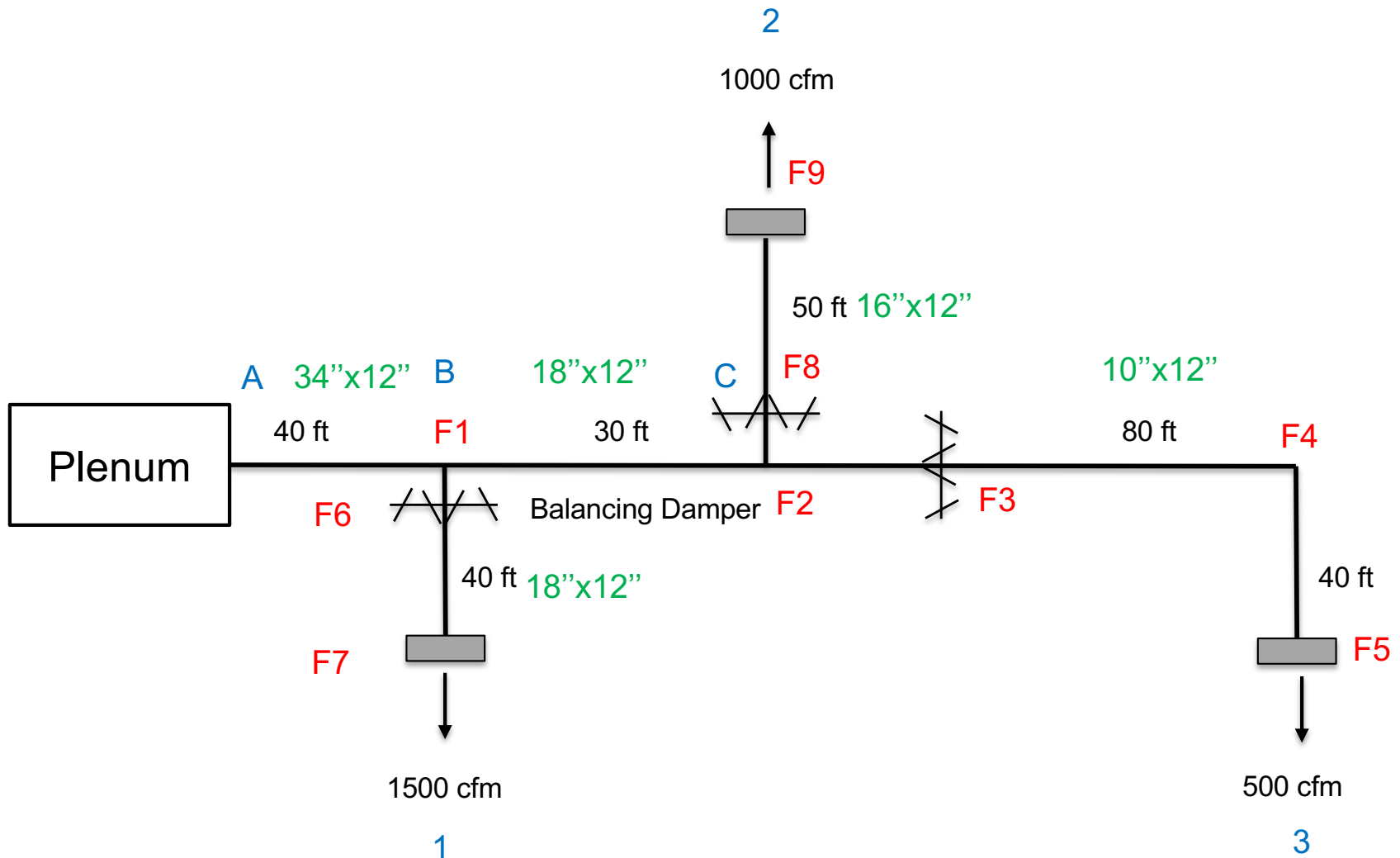
- Add the rectangular values to the table

Section	Air Flow Rate (cfm)	Duct Size (in)	Duct (in Rectangular)	Area (ft ²)	Velocity (fpm)
AB	3,000	21	34 / 12	2.83	1,059
BC	1,500	16	18 / 12	1.50	1,000
B1	1,500	16	18 / 12	1.50	1,000
C2	1,000	14.5	16 / 12	1.33	750
C3	500	11	10 / 12	0.83	600

Equal Friction Method

- **Solution:**

- Add the calculated ductwork sizes to the diagram



Equal Friction Method

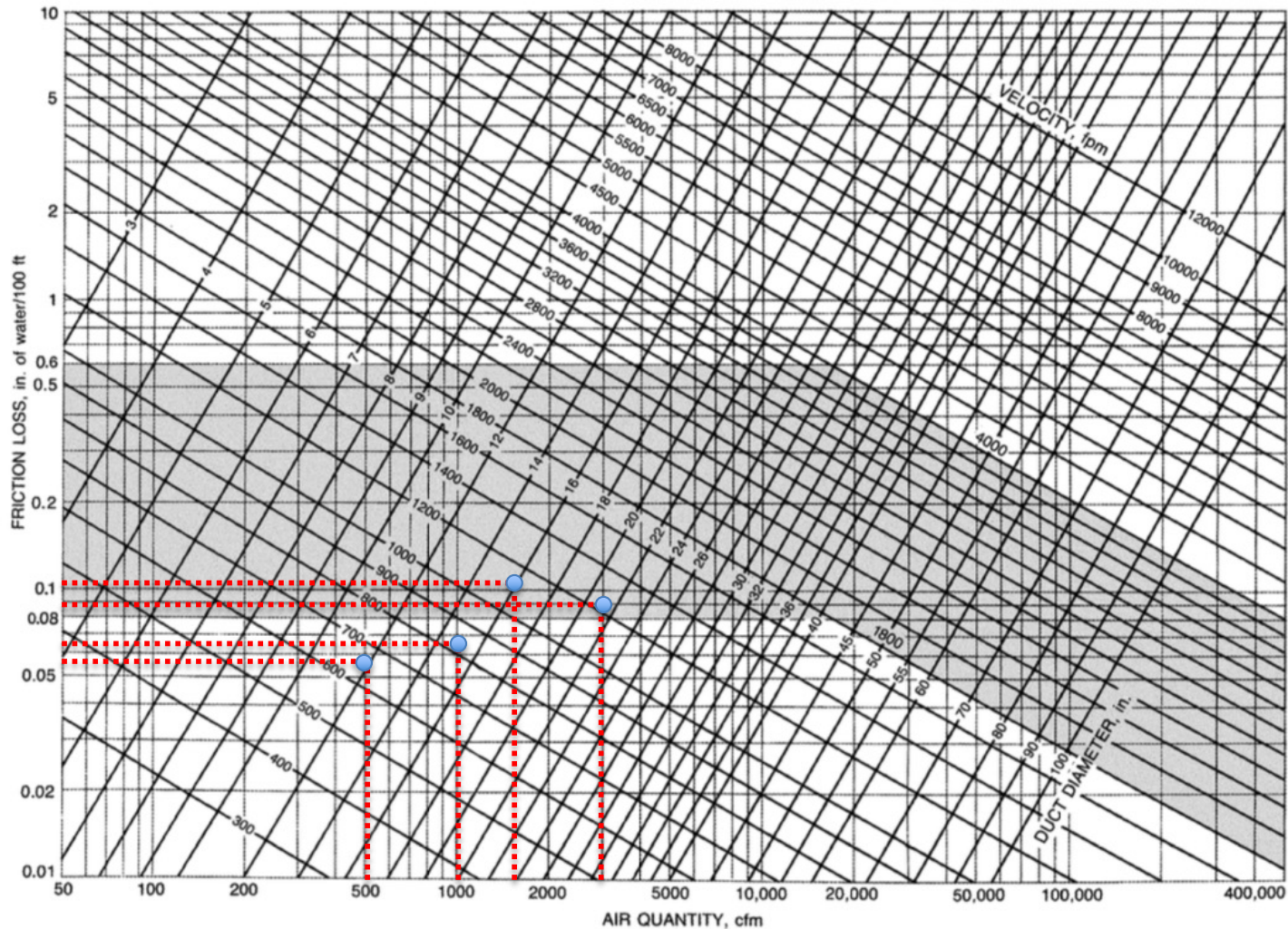
- **Solution:**

- Find the friction loss (in/100 ft) since we made slight changes to the duct cross sections

Section	Air Flow Rate (cfm)	Duct (in Rectangular)	D _e (in)	Friction Loss (in/100 ft)	Length (ft)	Section Loss (in. w.c.)
AB	3,000	34 / 12	21.4		40	0.035
BC	1,500	18 / 12	16		30	0.03
B1	1,500	18 / 12	16		40	0.04
C2	1,000	16 / 12	15.1		50	0.033
C3	500	10 / 12	12		120	0.067

Equal Friction Method

- **Solution:**
 - Friction losses (in/100 ft)



Equal Friction Method

- Solution:**

- Find the friction losses (in/100 ft)

Section	Air Flow Rate (cfm)	Duct (in Rectangular)	D _e (in)	Friction Loss (in/100 ft)	Length (ft)	Section Loss (in. w.c.)
AB	3,000	34 / 12	21.4	0.088	40	$0.088 \times \left(\frac{40}{100}\right) = 0.035$
BC	1,500	18 / 12	16	0.1	30	$0.1 \times \left(\frac{30}{100}\right) = 0.03$
B1	1,500	18 / 12	16	0.1	40	$0.1 \times \left(\frac{40}{100}\right) = 0.04$
C2	1,000	16 / 12	15.1	0.065	50	$0.065 \times \left(\frac{50}{100}\right) = 0.0325$
C3	500	10 / 12	12	0.056	120	$0.056 \times \left(\frac{120}{100}\right) = 0.067$

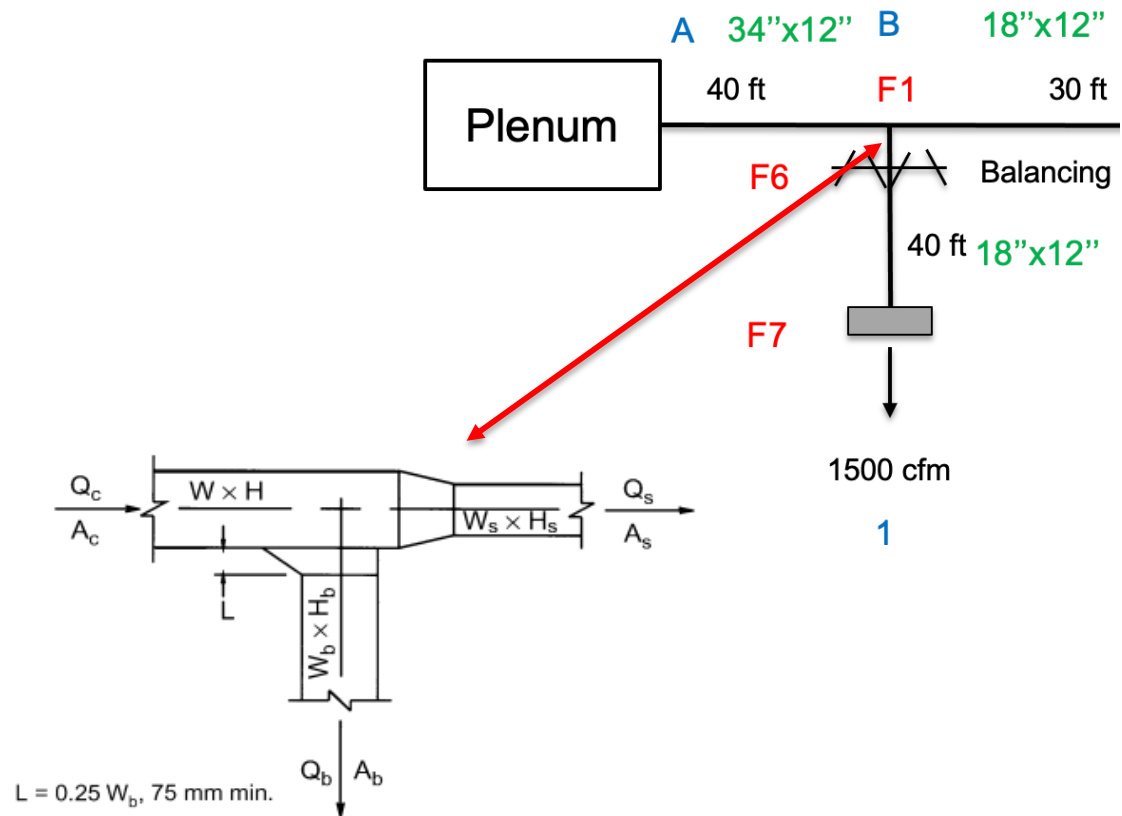
Equal Friction Method

- **Solution:**
 - Select fittings

SR5-13 Tee, 45 Degree Entry Branch, Diverging

		C_b Values								
		Q_b/Q_c								
A_b/A_c		0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.1		0.73	0.34	0.32	0.34	0.35	0.37	0.38	0.39	0.40
0.2		3.10	0.73	0.41	0.34	0.32	0.32	0.33	0.34	0.35
0.3		7.59	1.65	0.73	0.47	0.37	0.34	0.32	0.32	0.32
0.4		14.20	3.10	1.28	0.73	0.51	0.41	0.36	0.34	0.32
0.5		22.92	5.08	2.07	1.12	0.73	0.54	0.44	0.38	0.35
0.6		33.76	7.59	3.10	1.65	1.03	0.73	0.56	0.47	0.41
0.7		46.71	10.63	4.36	2.31	1.42	0.98	0.73	0.58	0.49
0.8		61.79	14.20	5.86	3.10	1.90	1.28	0.94	0.73	0.60
0.9		78.98	18.29	7.59	4.02	2.46	1.65	1.19	0.91	0.73

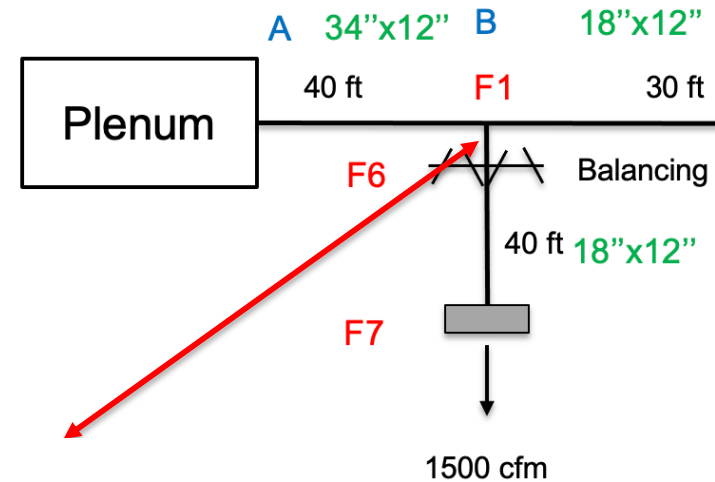
		C_s Values								
		Q_s/Q_c								
A_s/A_c		0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.1		0.04								
0.2		0.98	0.04							
0.3		3.48	0.31	0.04						
0.4		7.55	0.98	0.18	0.04					
0.5		13.18	2.03	0.49	0.13	0.04				
0.6		20.38	3.48	0.98	0.31	0.10	0.04			
0.7		29.15	5.32	1.64	0.60	0.23	0.09	0.04		
0.8		39.48	7.55	2.47	0.98	0.42	0.18	0.08	0.04	
0.9		51.37	10.17	3.48	1.46	0.67	0.31	0.15	0.07	0.04



Equal Friction Method

- Solution:**

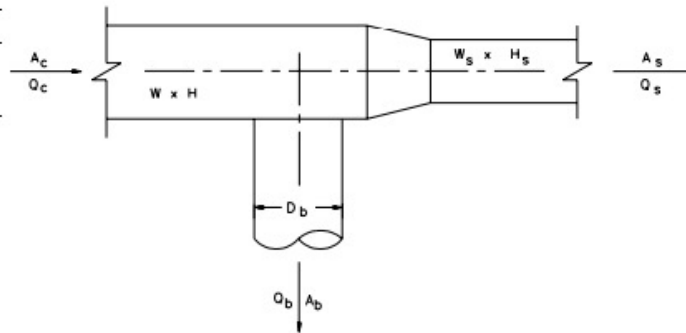
- Select fittings



SR5-11 Tee, Rectangular Main to Round Tap, Diverging

		C_D Values								
		Q_b/Q_c								
A_b/A_c		0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.1		1.58	0.94	0.83	0.79	0.77	0.76	0.76	0.76	0.75
0.2		4.20	1.58	1.10	0.94	0.87	0.83	0.80	0.79	0.78
0.3		8.63	2.67	1.58	1.20	1.03	0.94	0.88	0.85	0.83
0.4		14.85	4.20	2.25	1.58	1.27	1.10	1.00	0.94	0.90
0.5		22.87	6.19	3.13	2.07	1.58	1.32	1.16	1.06	0.99
0.6		32.68	8.63	4.20	2.67	1.96	1.58	1.35	1.20	1.10
0.7		44.30	11.51	5.48	3.38	2.41	1.89	1.58	1.38	1.24
0.8		57.71	14.85	6.95	4.20	2.94	2.25	1.84	1.58	1.40
0.9		72.92	18.63	8.63	5.14	3.53	2.67	2.14	1.81	1.58

		C_s Values								
		Q_b/Q_c								
A_b/A_c		0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.1		0.04								
0.2		0.98	0.04							
0.3		3.48	0.31	0.04						
0.4		7.55	0.98	0.18	0.04					
0.5		13.18	2.03	0.49	0.13	0.04				
0.6		20.38	3.48	0.98	0.31	0.10	0.04			
0.7		29.15	5.32	1.64	0.60	0.23	0.09	0.04		
0.8		39.48	7.55	2.47	0.98	0.42	0.18	0.08	0.04	
0.9		51.37	10.17	3.48	1.46	0.67	0.31	0.15	0.07	0.04



Equal Friction Method

- Solution:** Compute fittings

Section	Fitting No	Fitting Type	ASHRAE Fitting No.	Parameters	Loss Coefficient	Velocity (fpm)	P _v (in. w.c.)	P _t (in. w.c.)
AB	F1 _b	Tee Branch	SR5-13	$\frac{A_b}{A_c} = \frac{1.5}{2.83} = 0.53$ $\frac{Q_b}{Q_c} = \frac{1500}{3000} = 0.5$	0.82	1,000	0.062	0.051
	F1 _s	Tee Straight	SR5-13	$\frac{A_b}{A_c} = \frac{1.5}{2.83} = 0.53$ $\frac{Q_b}{Q_c} = \frac{1500}{3000} = 0.5$	0.06	1,000	0.062	0.004
BC	F2	Tee Branch	SR5-13	$\frac{A_b}{A_c} = \frac{1.33}{1.50} = 0.9$ $\frac{Q_b}{Q_c} = \frac{1000}{1500} = 0.67$	1.33	752	0.035	0.047
	F2	Tee Straight	SR5-13	$\frac{A_b}{A_c} = \frac{0.83}{1.5} = 0.55$ $\frac{Q_b}{Q_c} = \frac{500}{1500} = 0.3$	0.58	602	0.023	0.013
B1	F3	Damper	CR9-1	$q = 0^0$	0.19	600	0.022	0.004
	F4	Elbow	CR3-1	$\frac{r}{W} = 1$ $\frac{H}{W} = 1.2$	0.20	600	0.022	0.004
	F5	Outlet	----	----	---	---	---	0.050
C2	F7	Damper	CR9-1	$q = 0^0$	0.19	1,000	0.062	0.012
	F8	Outlet	----	----	---	---	---	0.050
C3	F6	Damper	CR9-1	$q = 0^0$	0.19	750	0.035	0.007
	F9	Outlet	----	----	---	---	---	0.050

Equal Friction Method

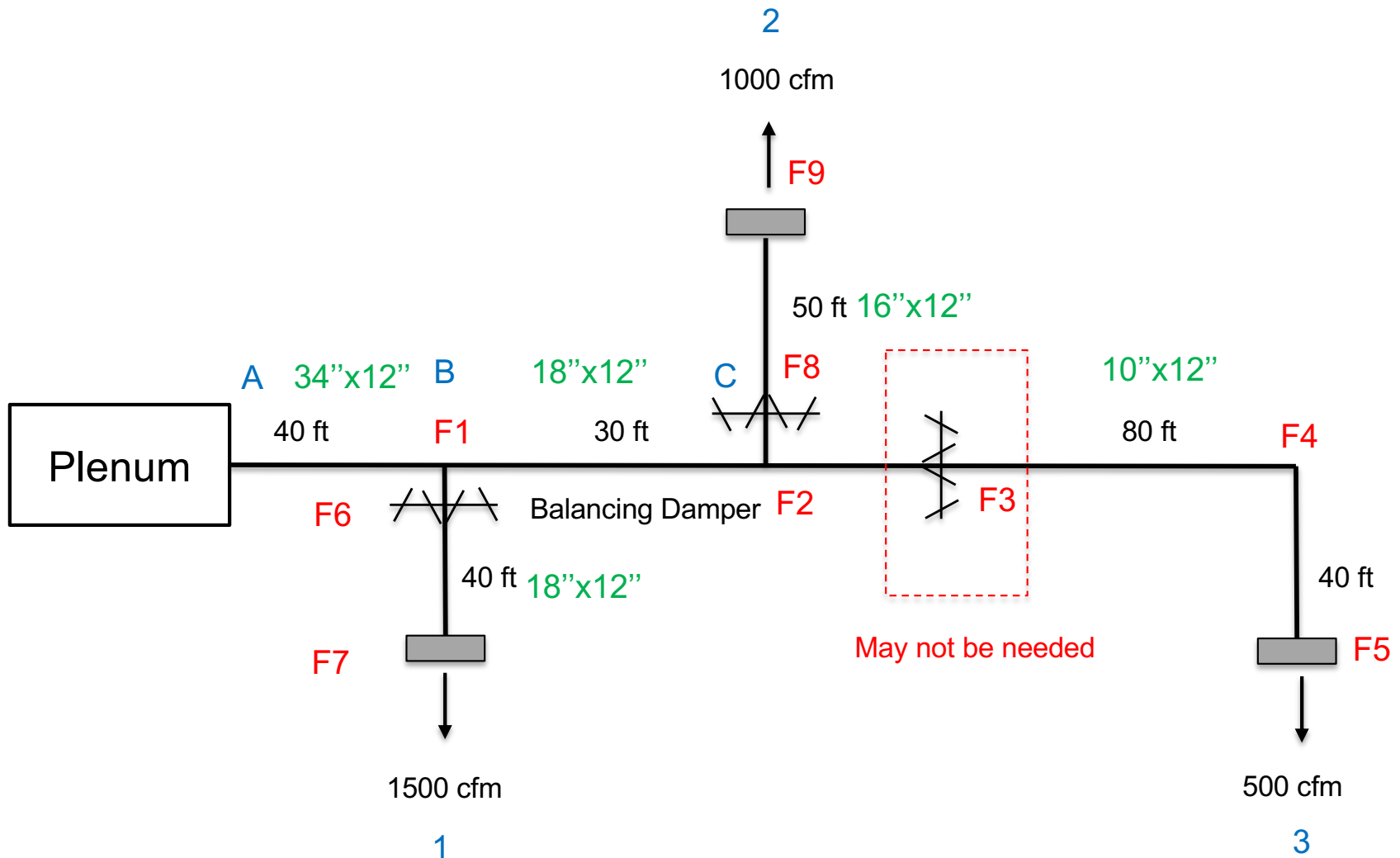
- Solution:** Pressure loss summary for different paths

ΔP (in. w.c.)

Path	Note	Duct	Tee	Duct	Tee	Damper	Duct	Outlet	Total	Difference
ABC 3	Path/Fitting Duct	AB	F1S	BC	F2S	F3	C3	Value		Path ΔP
		0.035	0.004	0.03	0.013	0.004	0.067	0.05	0.204	0.000
ABC 2	Path/Fitting Duct	AB	F1	BC	F2	F6	C2	Value		Path ΔP
		0.035	0.004	0.03	0.013	0.007	0.033	0.05	0.171	0.032
AB1	Path/Fitting Duct	AB	F1	---	---	F7	B1	Value		Path ΔP
		0.035	0.051	---	---	0.012	0.04	0.05	0.188	0.015

Equal Friction Method

- **Solution (summary):**



Equal Friction Method

- Another example is presented in this reference:

8.2 Duct Design Fundamentals

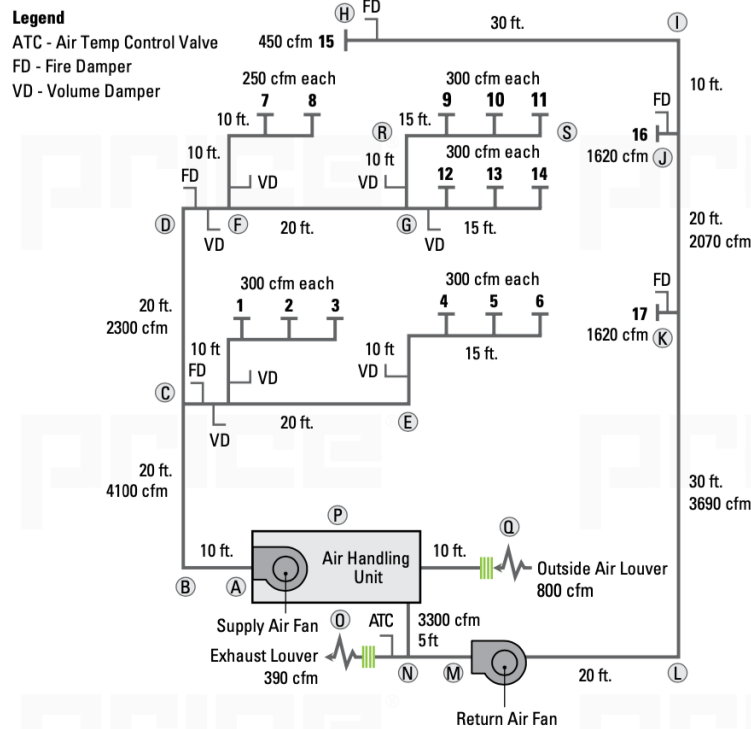


IP

Example 8.3 - Duct Sizing

As shown below, a schematic duct layout has been prepared for a building HVAC system that shows dampers, air volumes, duct length, and other information needed to properly size the duct. Note that all supply and return locations are numbered. A friction loss of 0.1 in. w.c./100 ft will be used for the sizing calculations. The total required discharge static pressure needed to supply the duct layout will be estimated.

The ductwork will be rectangular, but is sized as round and then converted to the rectangular format.



Equal Friction Method

- See Chapter 21 – Page 21.24 of the Fundamentals for another example:

Example 8. For the VAV system shown in [Figure 26](#), design the duct system by both the equal friction (EF) and static regain (SR) methods, and compare the section duct sizes, total pressure required for each path, and the unbalance between paths.

The system is located in Denver (5430 ft elevation) and the duct is spiral round, galvanized steel (absolute roughness $\epsilon = 0.0004$ ft). The duct system is located above a suspended acoustical ceiling, and the allowable background sound in the occupied spaces is NC-35. Terminals T1, T2, T3, and T4 (VAV boxes with a one-row hot-water coil) are 800 cfm. VAV box loss coefficients are 1.68.

BALANCED CAPACITY METHOD

Balanced Capacity Method

- The balanced design method uses the duct network principle
- For all network problems, it satisfies the continuity and the work-energy principles throughout the network

Balanced Capacity Method

- Based on the continuity equation, the summation of air flow rate into any junction is zero

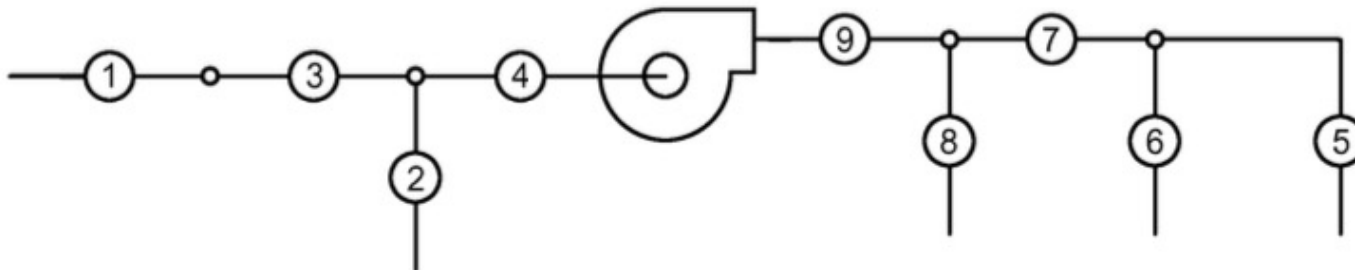
$$\Sigma \pm Q = 0$$

- Based on the network-energy equation, the total pressure loss around any single loop of the network is zero

$$\Sigma \pm P = 0$$

Balanced Capacity Method

- Satisfy all the possible pressure drops



$$P_{total} = \Delta p_1 + \Delta p_3 + \Delta p_4 + \Delta p_9 + \Delta p_7 + \Delta p_5$$

$$P_{total} = \Delta p_1 + \Delta p_3 + \Delta p_4 + \Delta p_9 + \Delta p_7 + \Delta p_6$$

$$P_{total} = \Delta p_1 + \Delta p_3 + \Delta p_4 + \Delta p_9 + \Delta p_8$$

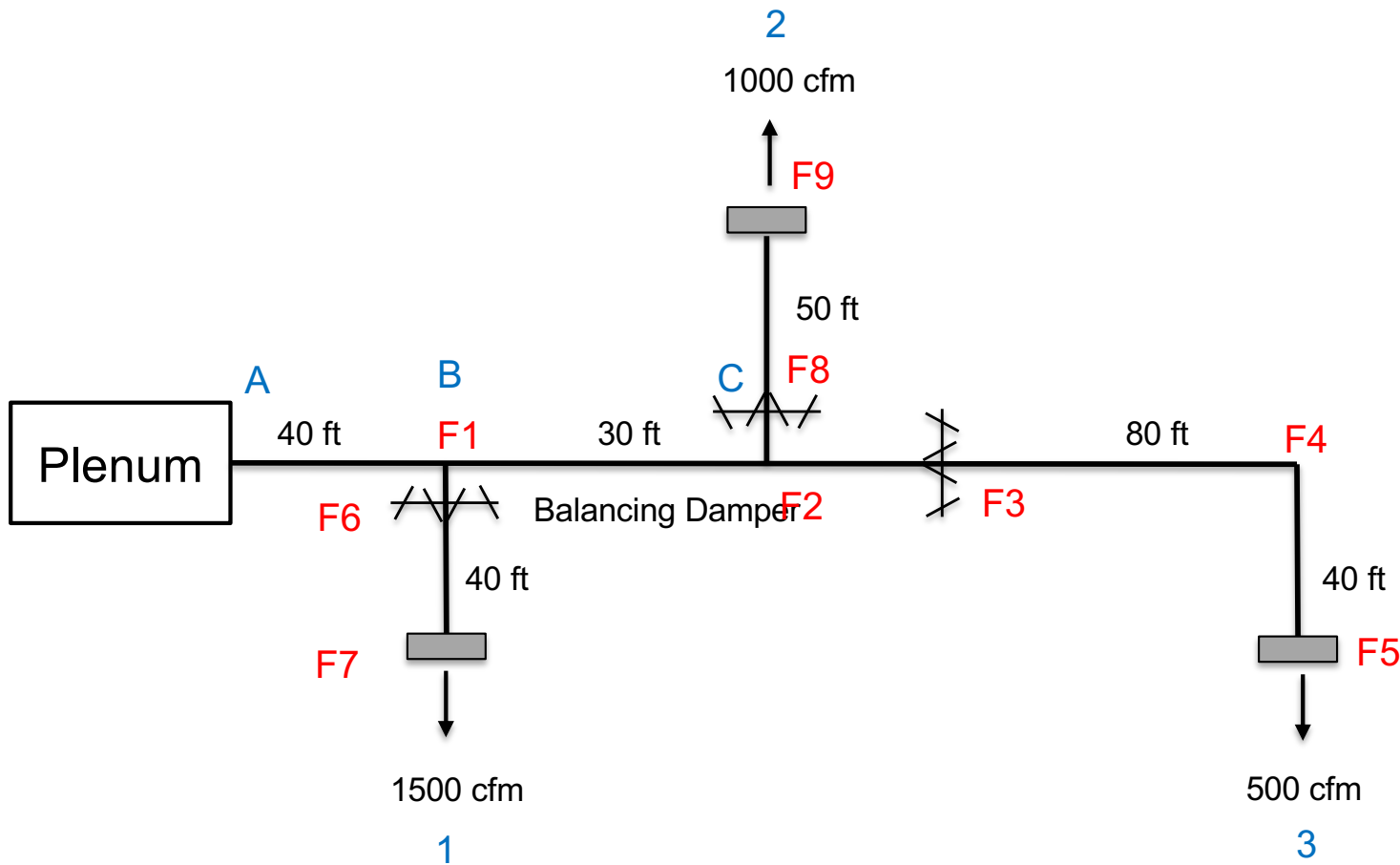
$$P_{total} = \Delta p_2 + \Delta p_4 + \Delta p_9 + \Delta p_7 + \Delta p_5$$

$$P_{total} = \Delta p_2 + \Delta p_4 + \Delta p_9 + \Delta p_7 + \Delta p_6$$

$$P_{total} = \Delta p_2 + \Delta p_4 + \Delta p_9 + \Delta p_8$$

Balanced Capacity Method

- Satisfy all the possible pressure drops



$$Q_1 = 1500 \text{ cfm}$$

$$Q_2 = 1000 \text{ cfm}$$

$$Q_3 = 500 \text{ cfm}$$

$$\Sigma Q = 3000 \text{ cfm}$$

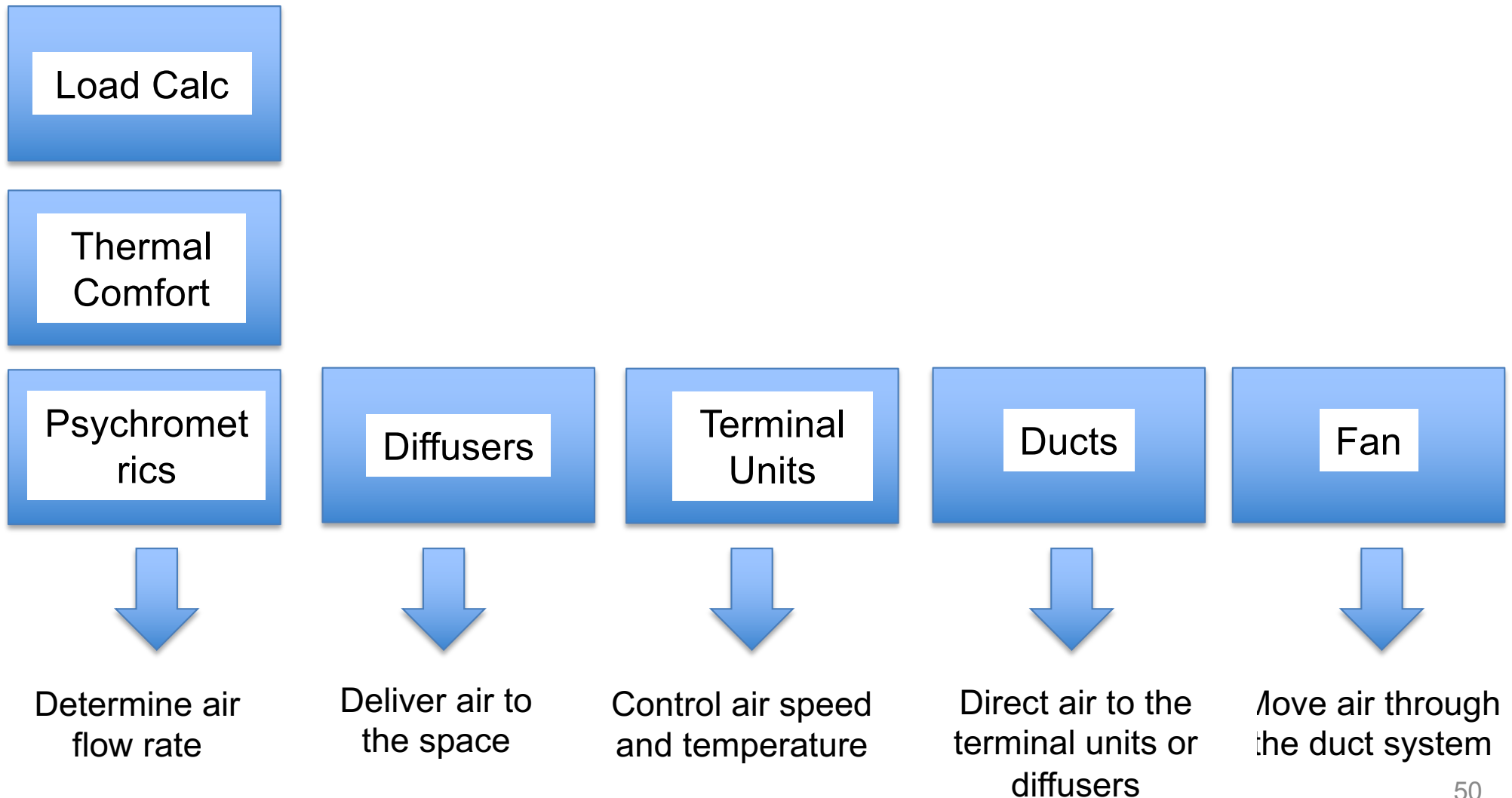
$$\Delta P_{A1} = \Delta P_{A2}$$

$$\Delta P_{A1} = \Delta P_{A3}$$

SYSTEM CHARACTERISTICS CURVE

System Characteristics Curve

- There are a couple of components required for the design of an air distribution



System Characteristics Curve

- Overall system resistance can be written as:

$$\begin{aligned}\Delta P_{total} &= \sum \Delta P_{Ductwork} + \sum \Delta P_{fittings} = \\ &= \sum f \frac{L}{D} \left(\frac{\rho V^2}{2g_c} \right) + \sum K \left(\frac{\rho V^2}{2g_c} \right)\end{aligned}$$

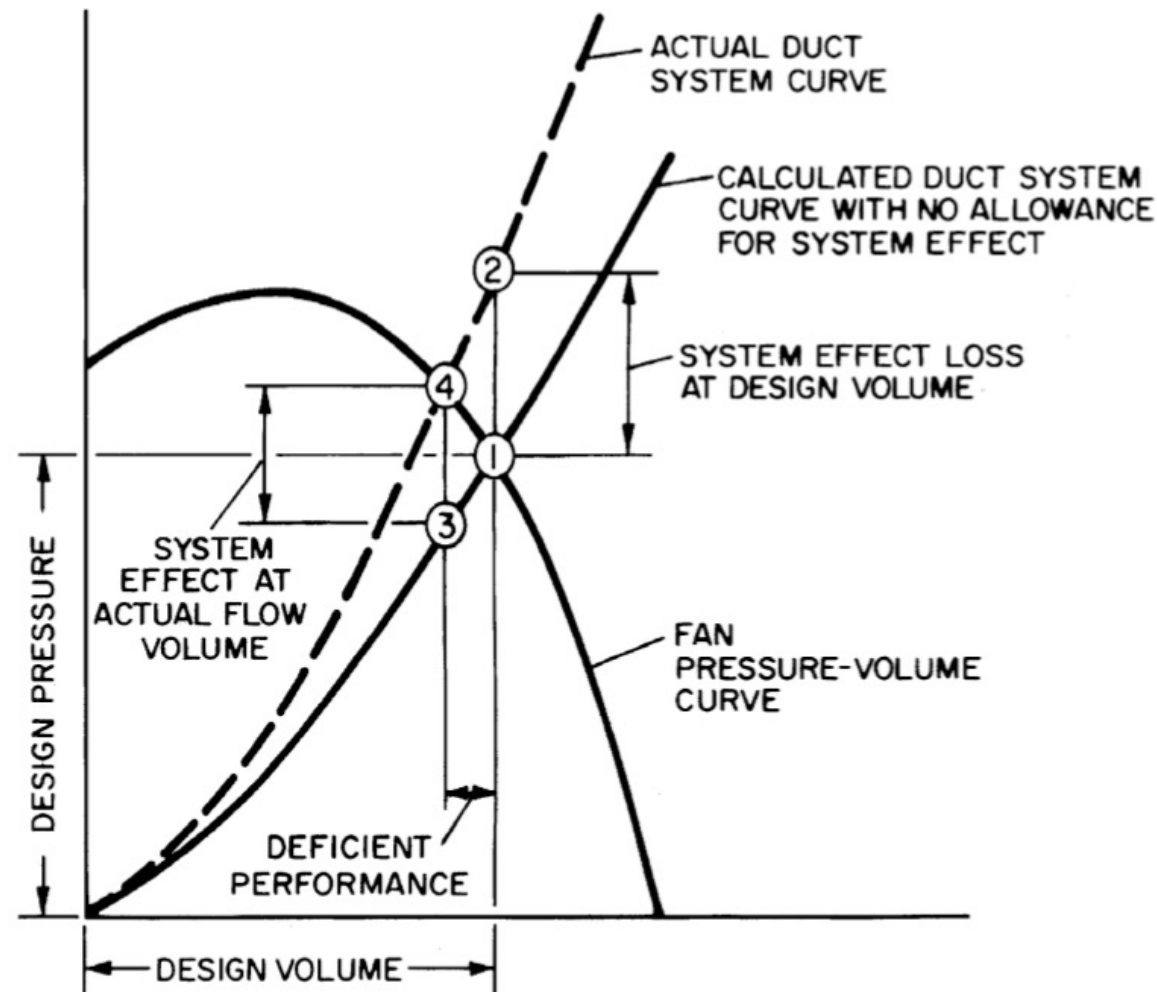
System Characteristics Curve

- Overall system resistance can be written as:

$$\Delta P_{total} = (Constant) \times \dot{Q}^2$$

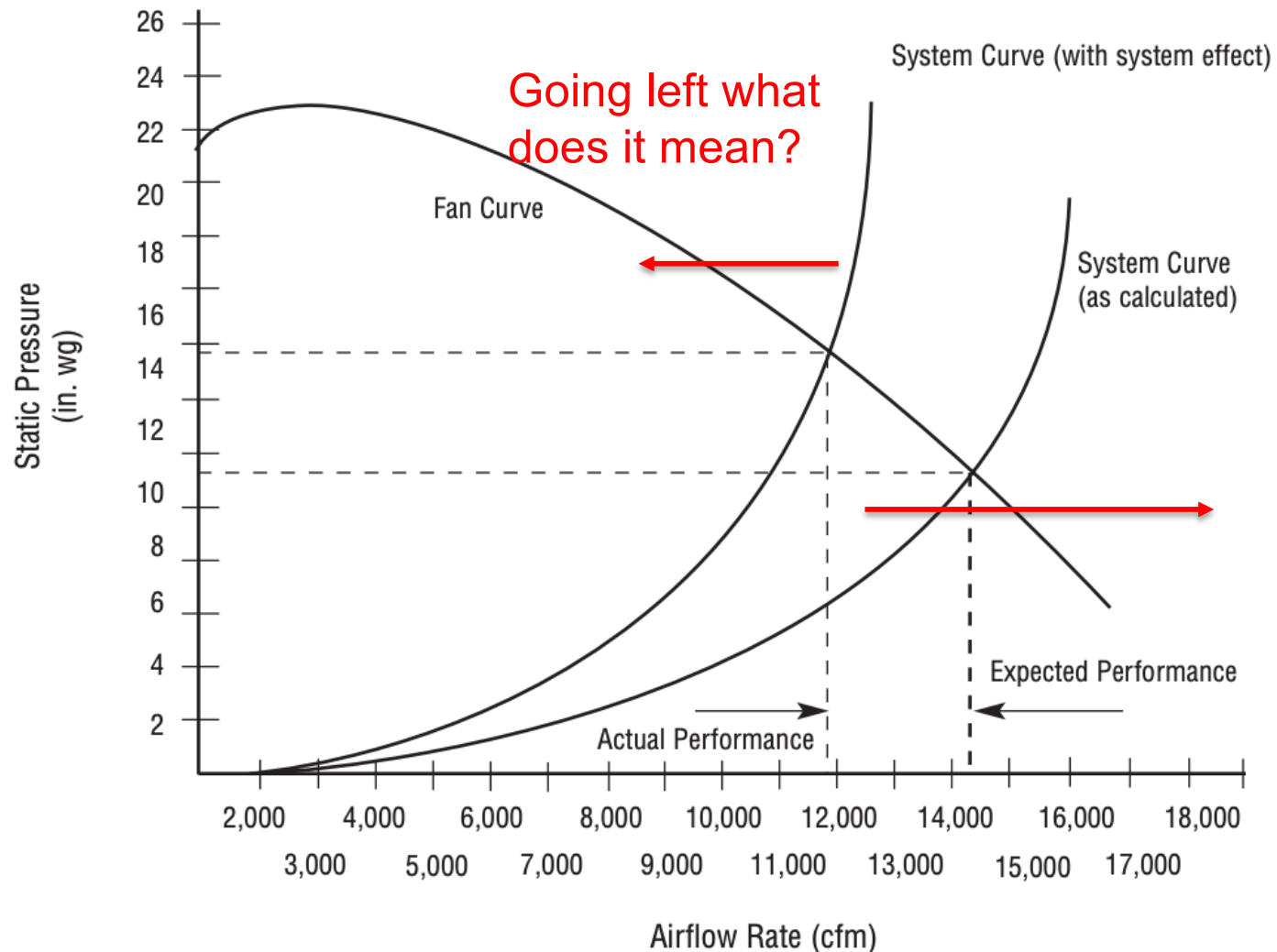
System Characteristics Curve

- Flow through any resistance (i.e., duct and fittings) is proportional to the square root of the pressure causing the flow



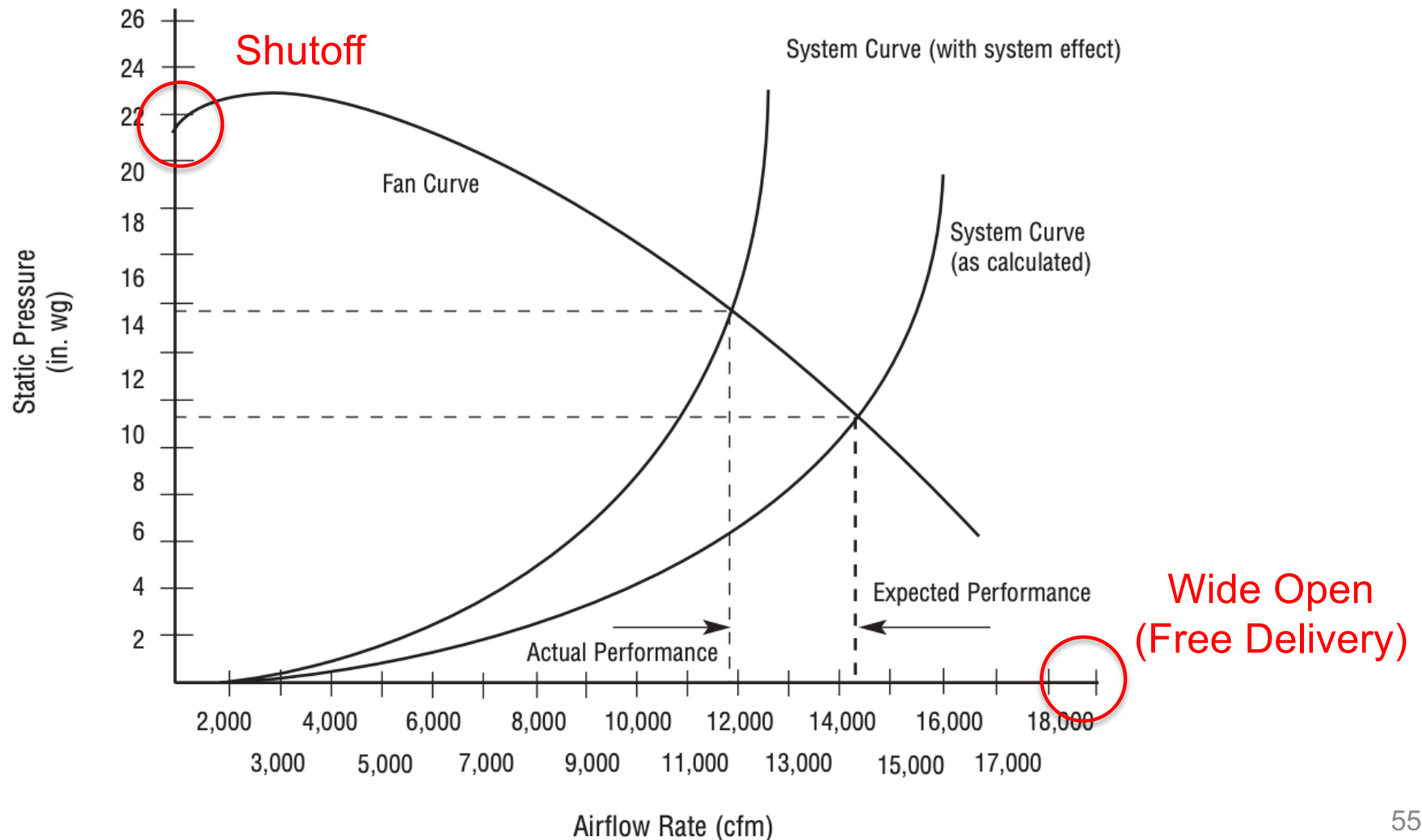
System Characteristics Curve

- This relationship defines the flow versus pressure characteristics of a system



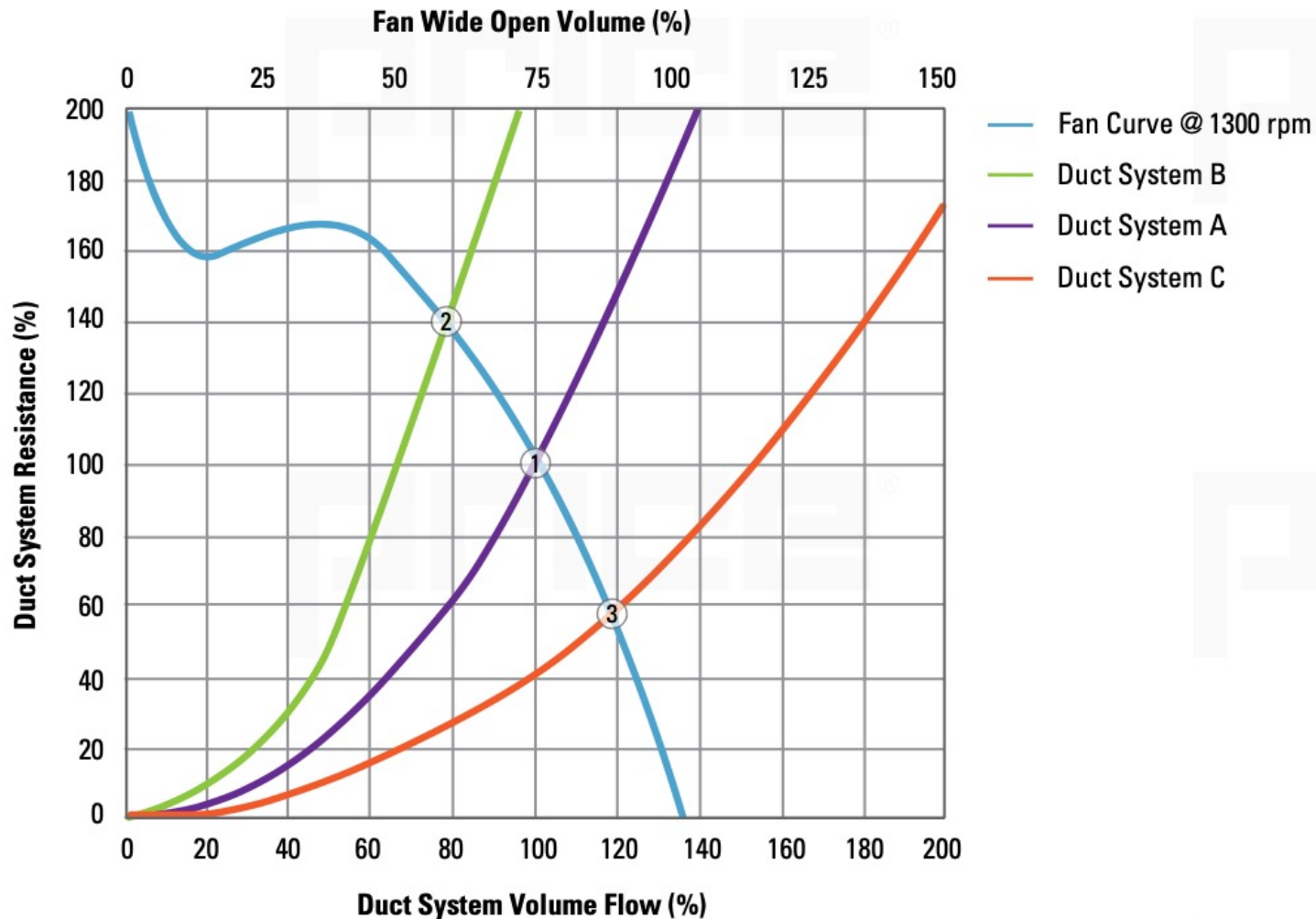
System Characteristics Curve

- This relationship defines the flow versus pressure characteristics of a system



System Characteristics Curve

- The best operating point varies based on the resistance in the system (i.e., system curves)

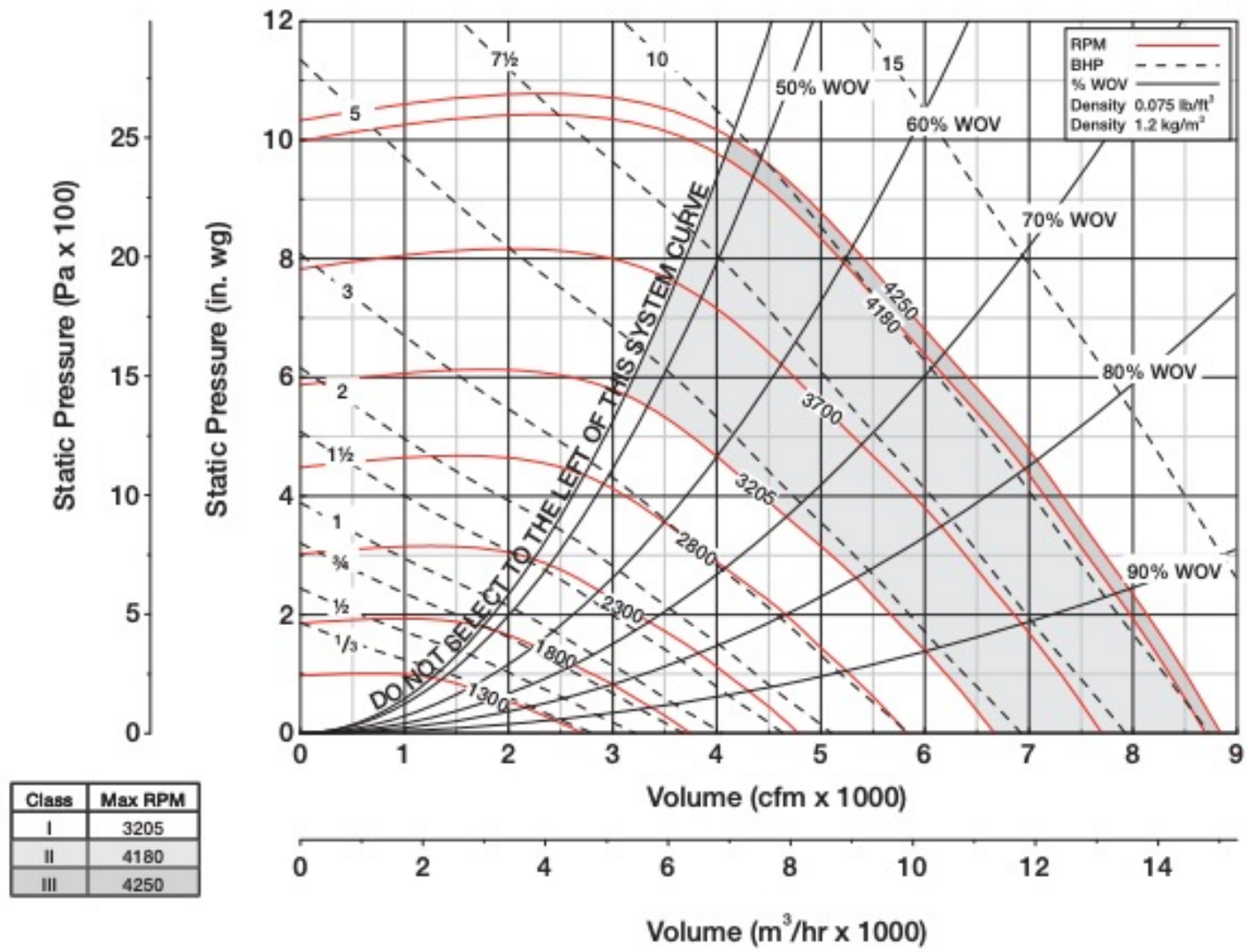


FAN PERFORMANCE CURVE

Fan Performance Curve

- An example of a fan curve:

12 BIDW



$$\% \text{ WOV} = (\text{CFM} \times 100) / (\text{RPM} \times 2.08)$$

Fan Performance Curve

- An example of a fan curve:

24 BIDW
Wheel Diameter = 24½ in.
Outlet Area = 6.21 ft. ²
Tip Speed = 6.41 x RPM
Maximum BHP = (RPM/599) ³

Minimum Starting HP = 1
Maximum RPM Class I = 1568
Maximum RPM Class II = 2045
Maximum RPM Class III = 2577

CFM	OV	STATIC PRESSURE (in. wg)																			
		0.25		0.50		0.75		1.00		1.25		1.50		1.75		2.00		2.25		2.50	
		RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP
5000	805	416	0.34	504	0.58	585	0.85	656	1.14												
6000	966	462	0.46	542	0.74	613	1.04	681	1.36	744	1.71	801	2.06								
7000	1127	512	0.62	586	0.94	650	1.26	711	1.62	769	1.99	826	2.39	878	2.79	927	3.20	972	3.63		
8000	1288	564	0.82	632	1.17	692	1.54	748	1.92	801	2.32	851	2.74	903	3.18	951	3.64	997	4.10	1040	4.57
9000	1449	619	1.07	679	1.46	737	1.87	789	2.28	838	2.70	886	3.16	931	3.62	977	4.11	1022	4.61	1065	5.11
10000	1610	675	1.36	730	1.79	783	2.23	833	2.70	879	3.15	923	3.62	968	4.12	1009	4.63	1049	5.16	1090	5.70
11000	1771	731	1.72	782	2.19	831	2.66	879	3.16	924	3.68	965	4.17	1005	4.68	1046	5.23	1085	5.78	1122	6.35
12000	1932	789	2.14	836	2.64	882	3.16	925	3.69	969	4.24	1009	4.80	1048	5.34	1084	5.88	1122	6.47	1159	7.08
13000	2093	848	2.63	891	3.17	933	3.73	975	4.29	1015	4.87	1055	5.47	1092	6.08	1128	6.66	1162	7.25	1196	7.86
14000	2254	907	3.20	947	3.76	986	4.37	1025	4.97	1063	5.58	1101	6.21	1137	6.86	1172	7.51	1205	8.14	1237	8.78
15000	2415	967	3.85	1003	4.44	1040	5.08	1077	5.73	1113	6.37	1148	7.03	1183	7.71	1217	8.41	1250	9.11	1281	9.79
16000	2576	1027	4.58	1060	5.21	1095	5.88	1129	6.57	1164	7.26	1198	7.95	1230	8.66	1264	9.39	1295	10.1	1326	10.9
17000	2737	1087	5.41	1118	6.07	1151	6.78	1184	7.50	1216	8.24	1248	8.97	1280	9.71	1310	10.5	1342	11.2	1372	12.0
18000	2898	1147	6.34	1177	7.04	1207	7.77	1239	8.53	1269	9.31	1300	10.1	1330	10.9	1359	11.6	1388	12.4	1418	13.3
19000	3059	1208	7.38	1236	8.11	1264	8.86	1294	9.67	1323	10.5	1352	11.3	1381	12.1	1410	12.9	1437	13.8	1465	14.6
20000	3220	1269	8.52	1295	9.29	1321	10.1	1350	10.9	1378	11.8	1405	12.6	1433	13.5	1460	14.3	1487	15.2	1513	16.1