

# CAE 463/524

## Building Enclosure Design

Spring 2016

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**Week 13: April 5, 2016**

Energy simulation and enclosure design

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# Last week

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- Campus enclosure assessment presentations
- Take-home exam given
  - Due today
- Introduced final individual project expectations

# Project 2: Topic selection

- **Email me** your topics by **Friday April 8, 2016**

Name	Project topic
Blat Tatay, Andrea	
Curioni, Dina P.	
Jarma, David A.	
Jordan, Taylor L.	
Kane, Benjamin M.	Double skin façades and energy
Lim, Keonho	
Mitchell, Alexander R.	
Panczak, Bianca J.	Smart glass
Rice, Lindsey E.	
Townley, Nina V.	
Ashayeri Jahan Khanemloo, Mehdi	
Babaei Sonbolabadi, Kamal	
Cueto, Patrick Kevin M.	
Del Pino Torres, Julia Del Rosario	
Faramarzi, Afshin	
Foss, Stephen M.	Smart glazing
Qiu, Luanzhizi	Green roofs
Sharghi, Ali	
Sudhakaran, Naveen	
Zhang, Xu	
Castro, Jose L.	
Dipietro, Salvatore D.	
Lee, JiWan	

# Today's objectives

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- Introduce energy simulation in building enclosure design
  - And applications for enclosure design

# **WHOLE BUILDING ENERGY SIMULATION**

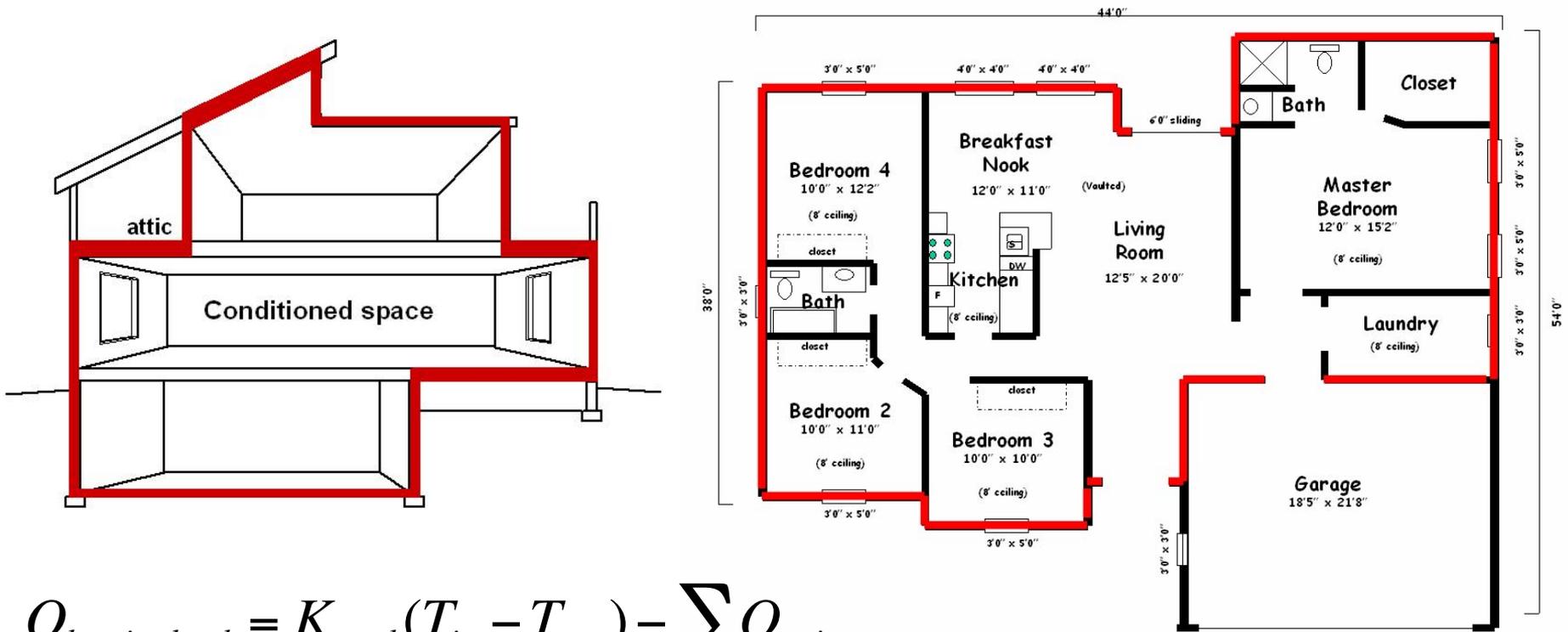
# Energy simulation and enclosure design

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- In CAE 331/513 Building Science we discussed using sizing programs to determine peak hourly loads during heating and cooling seasons and size equipment
- Heating loads: easy →  $Q = UA\Delta T$  method
- Cooling loads: more complex (involves radiation and storage) → CLTD, RTS, HB methods, etc.
  - You can influence loads and size of equipment early in the design process by specifying certain envelope characteristics

# Heating load calculations

- Define the building envelope, calculate transmission losses and internal gains, find design conditions, and use the simple equations below



$$Q_{\text{heating load}} = K_{\text{total}} (T_{\text{in}} - T_{\text{out}}) - \sum Q_{\text{gains}}$$

$$Q_{\text{heating load}} = \left( \sum UA + \dot{V}_{\text{OA}} \rho_{\text{OA}} C_{p,\text{air}} \right) (T_{\text{in}} - T_{\text{out}}) - \sum Q_{\text{gains}}$$

# Cooling load calculations

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- Cooling load calculations are more complicated than heating load calculations
- Peak cooling loads will occur during the day when solar radiation is present
  - People and equipment can also be highly variable
- Radiation varies throughout the day and the building's **thermal mass** affects the time release of this heat energy
  - Calculations must be **dynamic** to account for **storage**

$$Q_{sensible\ load} =$$

$$Q_{envelope\ transmission} + Q_{air\ exchange} - Q_{solar} - Q_{people} - Q_{equipment} - Q_{lights} \pm Q_{storage}$$

Remember:

Q is typically positive (+) when there is a heating load (cold outside)

Q is typically negative (-) when there is a cooling load (hot outside)

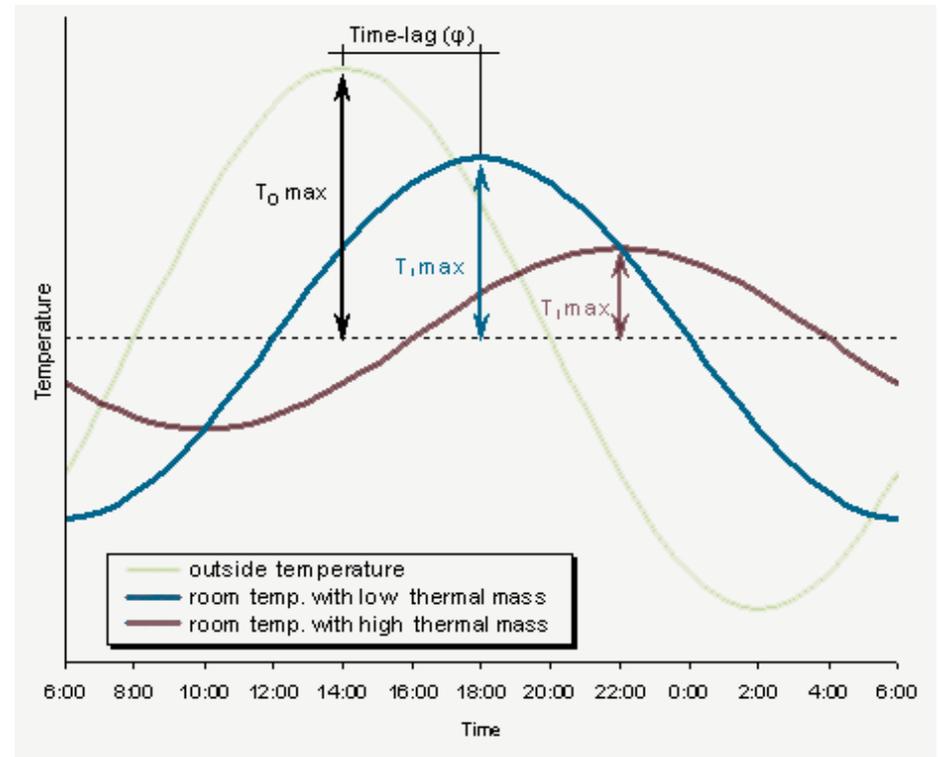
# Dynamic response for **cooling** loads

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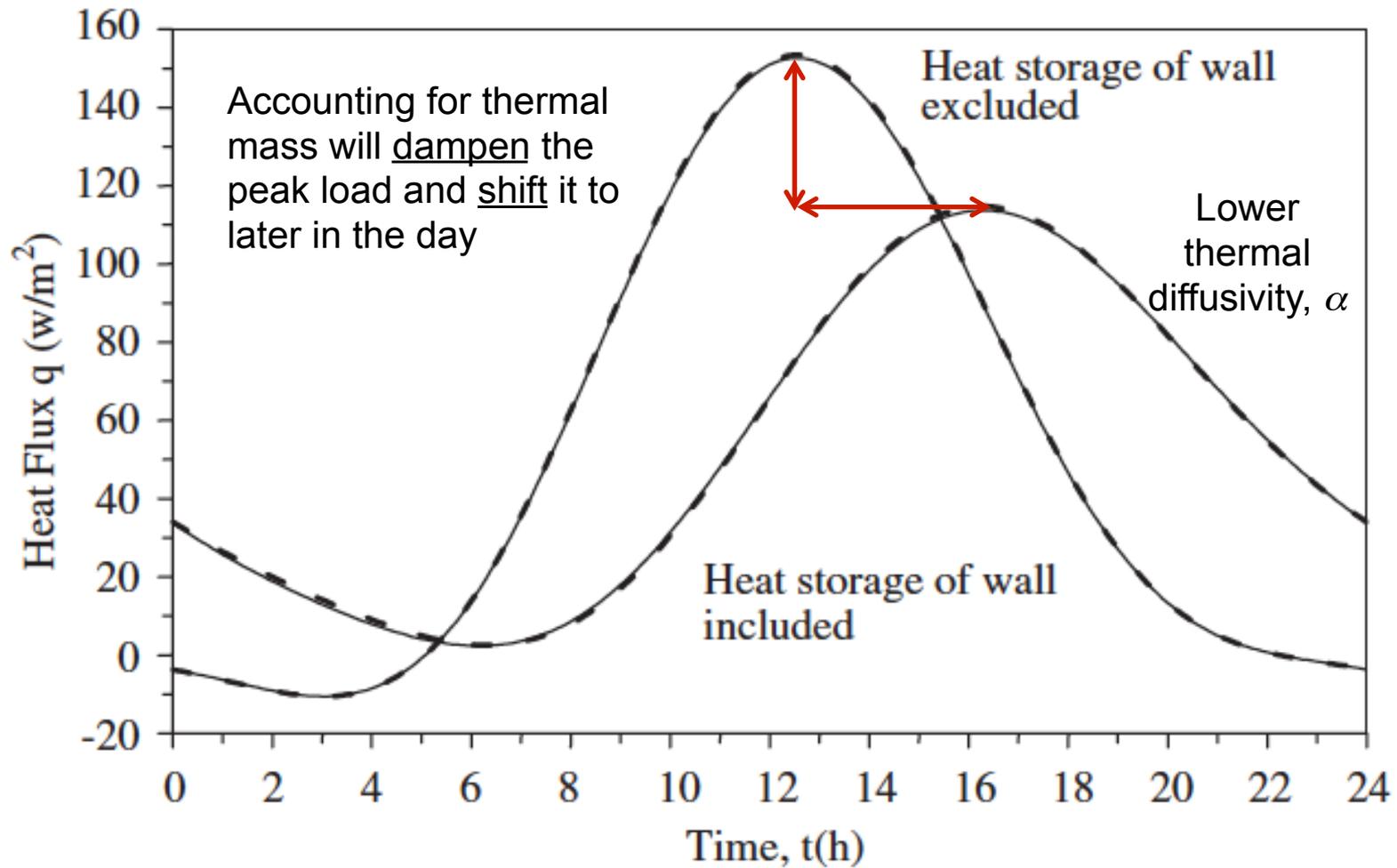
- Cooling load calculations differ because gains from **radiation** do not directly heat up the air in the space
  - Only **convection** from interior surfaces contributes to an immediate temperature rise in the air space
- Radiation through windows, from interior surfaces, and from internal sources (e.g., lights) will be absorbed by other interior surfaces, and then those surfaces will eventually transfer that heat energy to the air by convection
  - But the addition of radiative heat does not occur immediately
- Because radiative heating is not direct, **heat storage** through **thermal mass** can create a thermal lag, which can have a large effect on cooling loads

# Thermal mass (more on this later)

- Thermal mass refers to materials that have the capacity to store thermal energy for extended periods of time
- Thermal mass can absorb daytime heat gains
  - Reduces peak cooling load
  - Releases heat during the night (can reduce heat load or can extend cooling load)



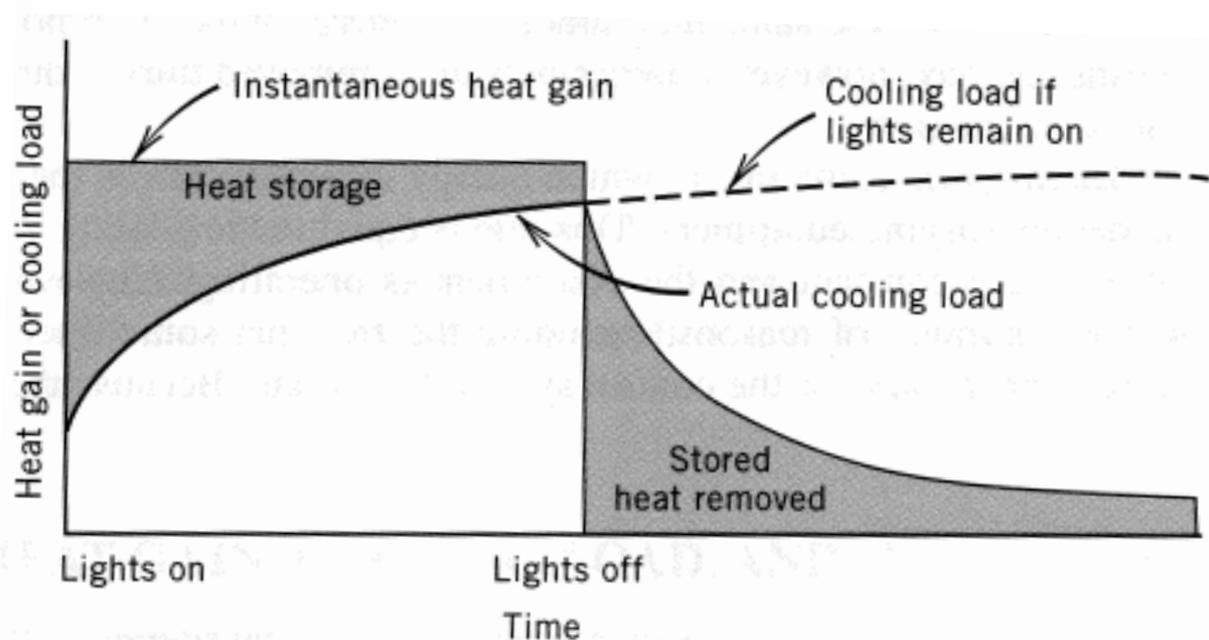
# Accounting for thermal mass impacts



# Accounting for thermal mass is necessary for other types of loads as well

- Need to account for heat capacity of building materials and the fraction of radiative versus convective heat given off by systems and equipment

	Radiative, percent	Convective, percent
Fluorescent lights	50	50
People	33	67
External walls and roofs	60	40
Appliance and machines	20–80	80–20



**Figure 8-3** Actual cooling load from fluorescent lights.

# Whole building energy simulation

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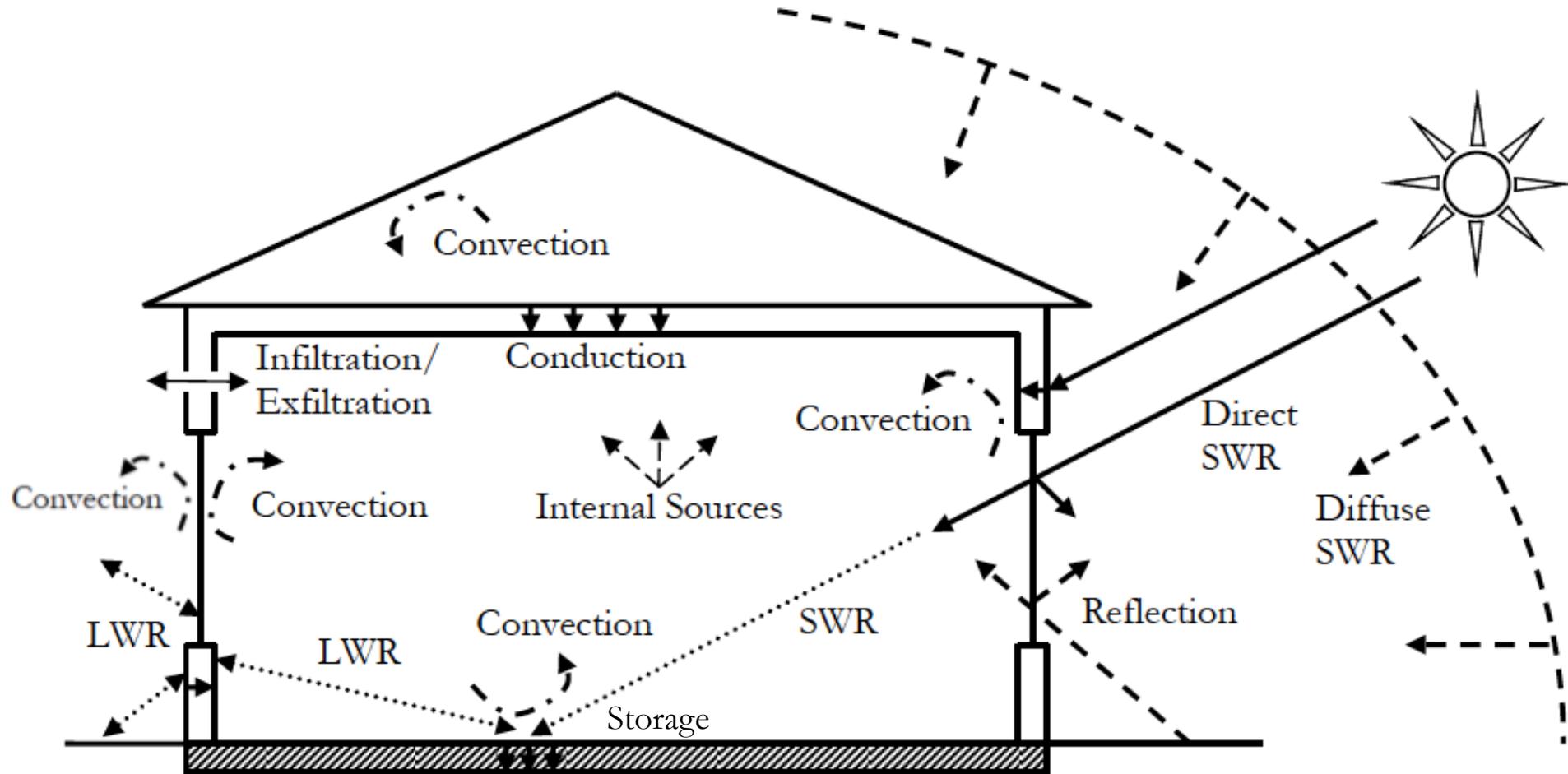
- Whole building energy simulation programs are used to predict annual energy consumed by a building
- Essentially a continuation of design-day load calculation methods to the entire year
- Outcomes: annual BTUs, MJ, kWh, \$, associated pollutant emissions
  - Typically normalized per floor area (e.g., kBTU/ft<sup>2</sup>)
- You can influence annual energy consumption (and costs) early in the design process, again by specifying certain envelope characteristics

# Whole building energy simulation

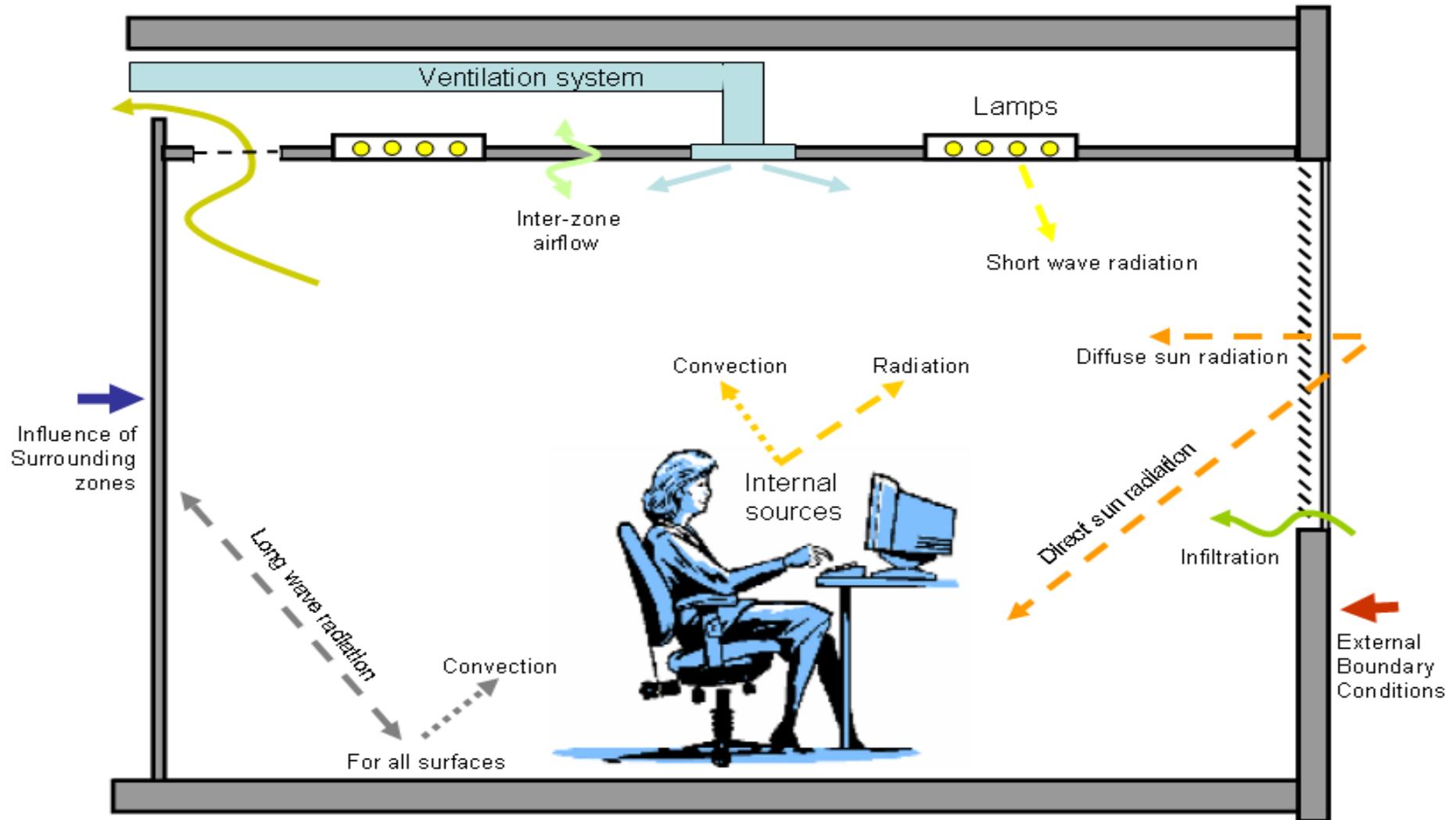
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- We've covered individual **surface energy balances** before
  - Surfaces are all connected
- We can build a **system of equations** linking energy balances at a series of “nodes”
  - Each node has an equation accounting for all modes of heat transfer
- Whole building energy simulation
  - Involves linking the nodes and predicting hourly indoor air temperatures (or HVAC loads) as the primary unknown(s)
    - Include HVAC system capacity and efficiency to get HVAC energy
  - Also includes interior heat gains
    - People, lights, equipment, etc.
    - Direct power draw + indirect heat gains

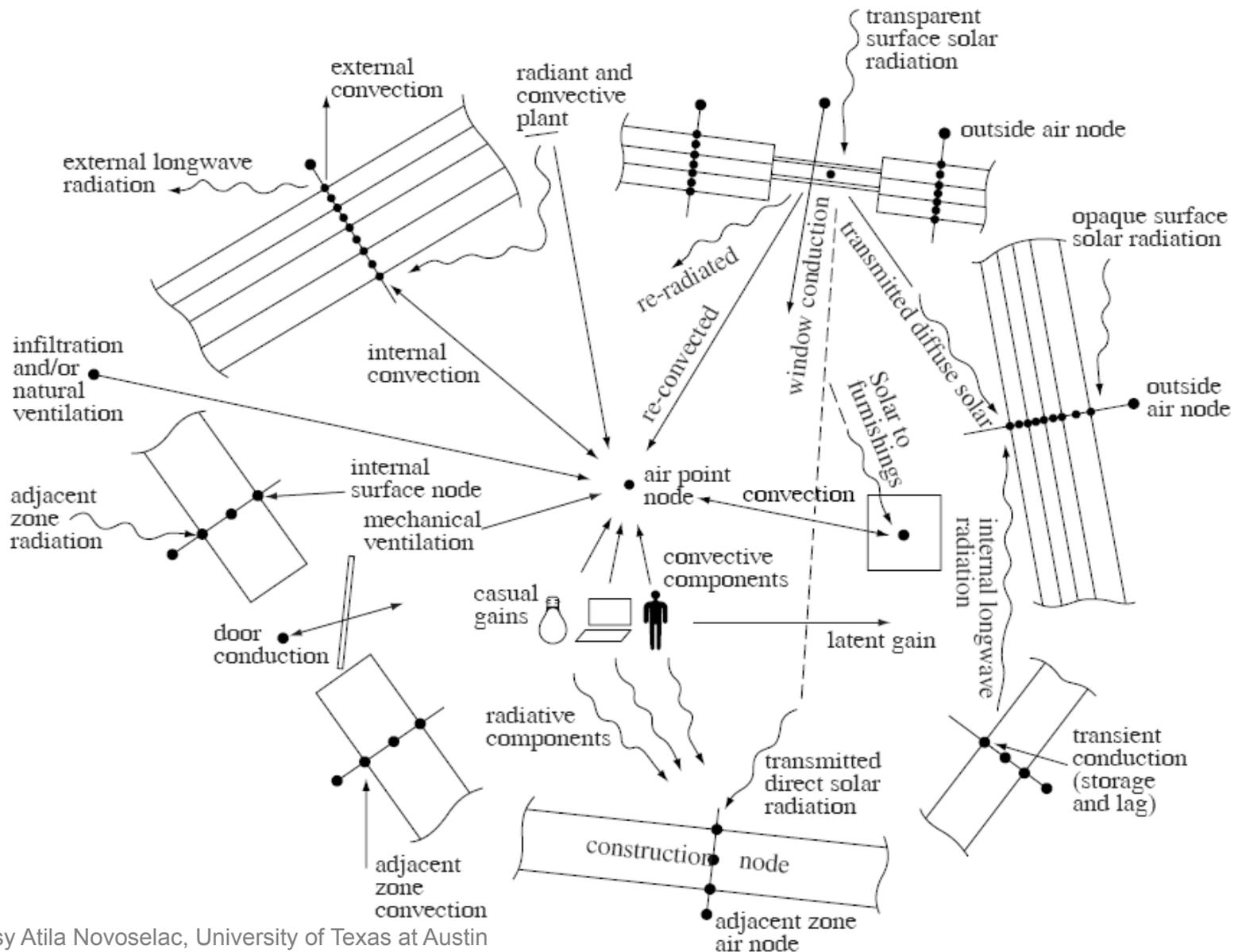
# Whole building energy simulation



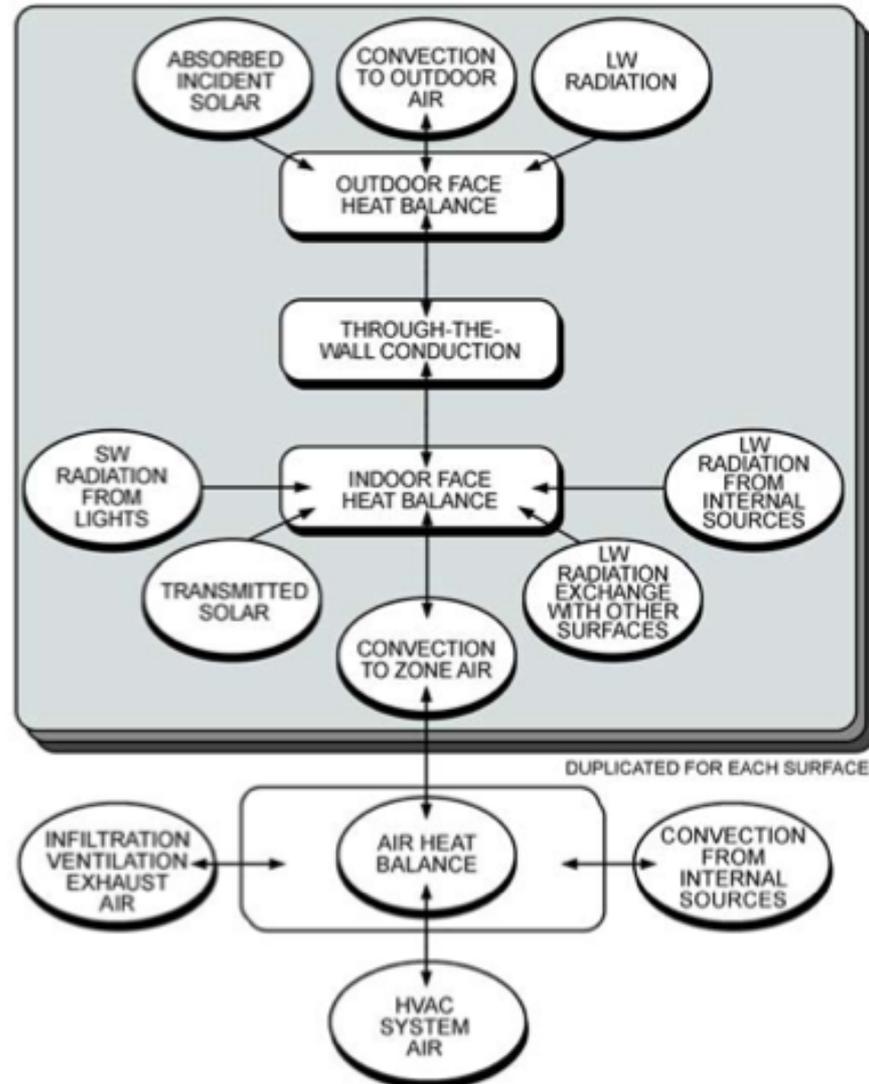
# Whole building energy simulation



# Whole building energy simulation



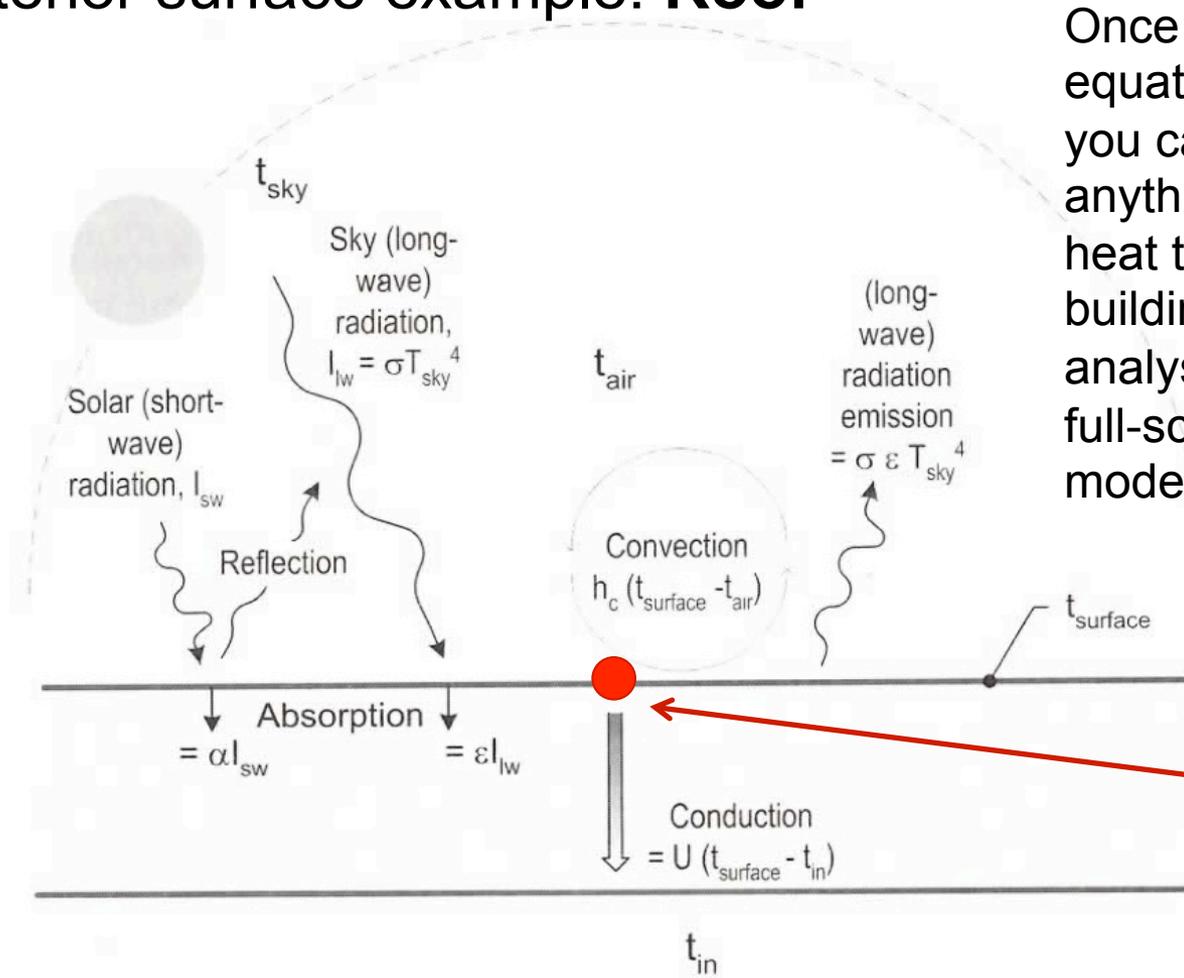
# Whole building energy simulation



*An extension of the Heat Balance Method (HBM)*

# Surface energy balance: Bringing all the modes together

- Exterior surface example: **Roof**



Once you have this equation described, you can do just about anything regarding heat transfer in building enclosure analysis, leading into full-scale energy modeling

**Steady-state energy balance at this exterior surface:**  
What enters must also leave (no storage)

$$q_{solar} + q_{longwaveradiation} + q_{convection} - q_{conduction} = 0$$

# Surface energy balance: Bringing all the modes together

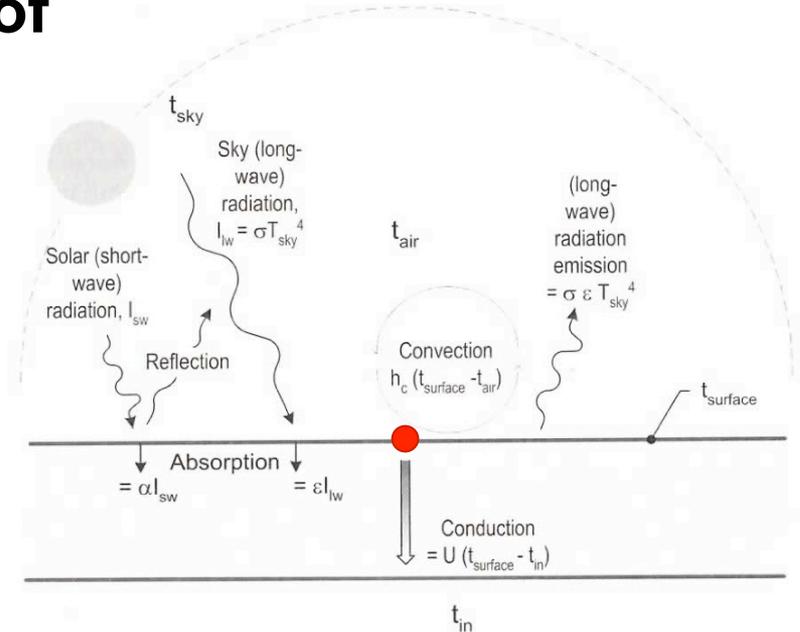
- Exterior surface example: **Roof**

$$\sum q = 0$$

We can use this equation to estimate indoor and outdoor surface temperatures

At steady state, net energy balance is zero

- Because of  $T^4$  term, often requires iteration



Solar gain

$$\alpha I_{solar}$$

$$q_{sw,solar}$$

Surface-sky radiation

$$+\epsilon_{surface} \sigma F_{sky} (T_{sky}^4 - T_{surface}^4)$$

$$+q_{lw,surface-sky}$$

Convection on external wall

$$+h_{conv} (T_{air} - T_{surface})$$

$$+q_{convection}$$

Conduction through wall

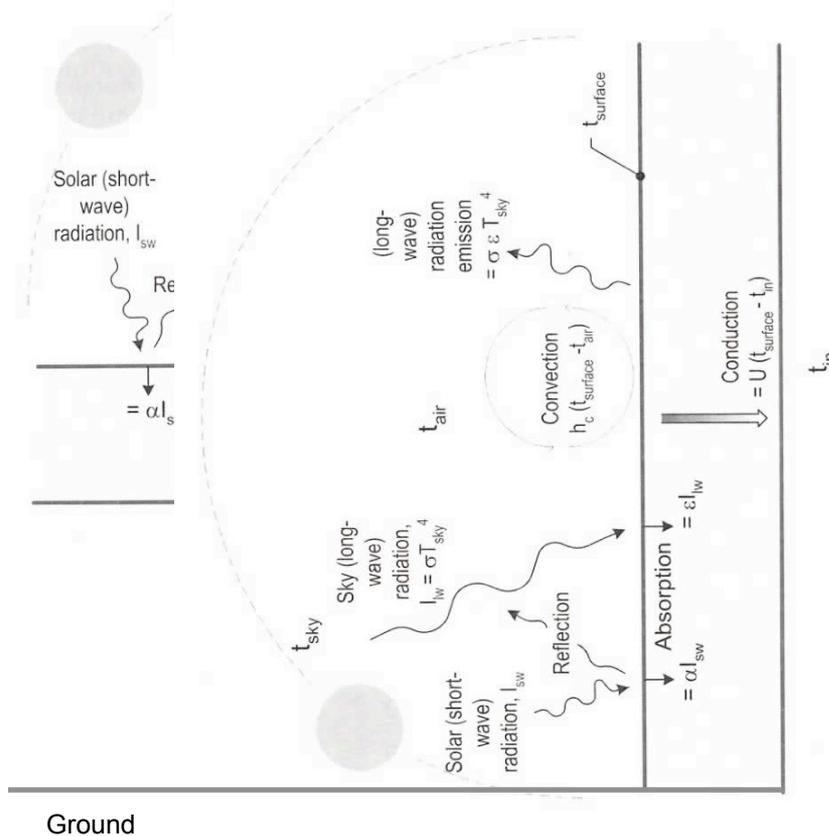
$$-U(T_{surface} - T_{surface,interior}) = 0$$

$$-q_{conduction} = 0$$

# Surface energy balance: Bringing all the modes together

- Similarly, for a vertical surface:

$$q_{solar} + q_{lwr} + q_{conv} - q_{cond} = 0$$



$$\begin{aligned} & \alpha I_{solar} \\ & + \epsilon_{surface} \sigma F_{sky} (T_{sky}^4 - T_{surface}^4) \\ & + \epsilon_{surface} \sigma F_{ground} (T_{ground}^4 - T_{surface}^4) \\ & + h_{conv} (T_{air} - T_{surface}) \\ & - U (T_{surface} - T_{surface,interior}) = 0 \end{aligned}$$

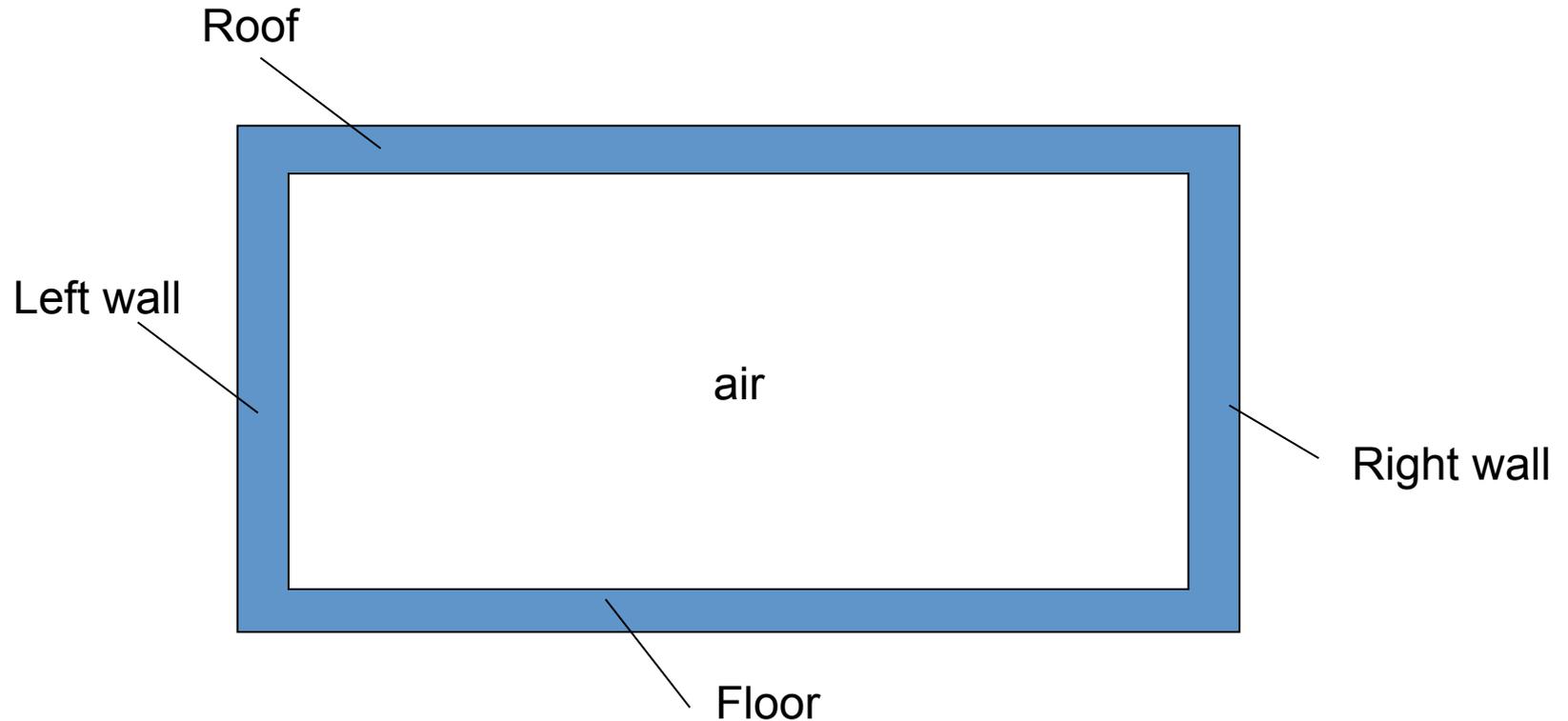
# Whole building energy modeling steps

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- Define the domain
- Analyze the most important phenomena and define the most important elements
- Discretize the elements and define connections
- Write the energy and mass balance equations
  - Include any assumptions for indoor sources
- Solve the equations
  - Use numerical methods or analytical solutions
  - Time-varying analysis over an entire year
- Present the results
  - kWh electricity; BTU or MJ of other fuels
  - Hourly, daily, monthly, yearly

# Simplest 'box' model

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Elements are connected by:

- 1) Convection – air node
- 2) Radiation – surface nodes



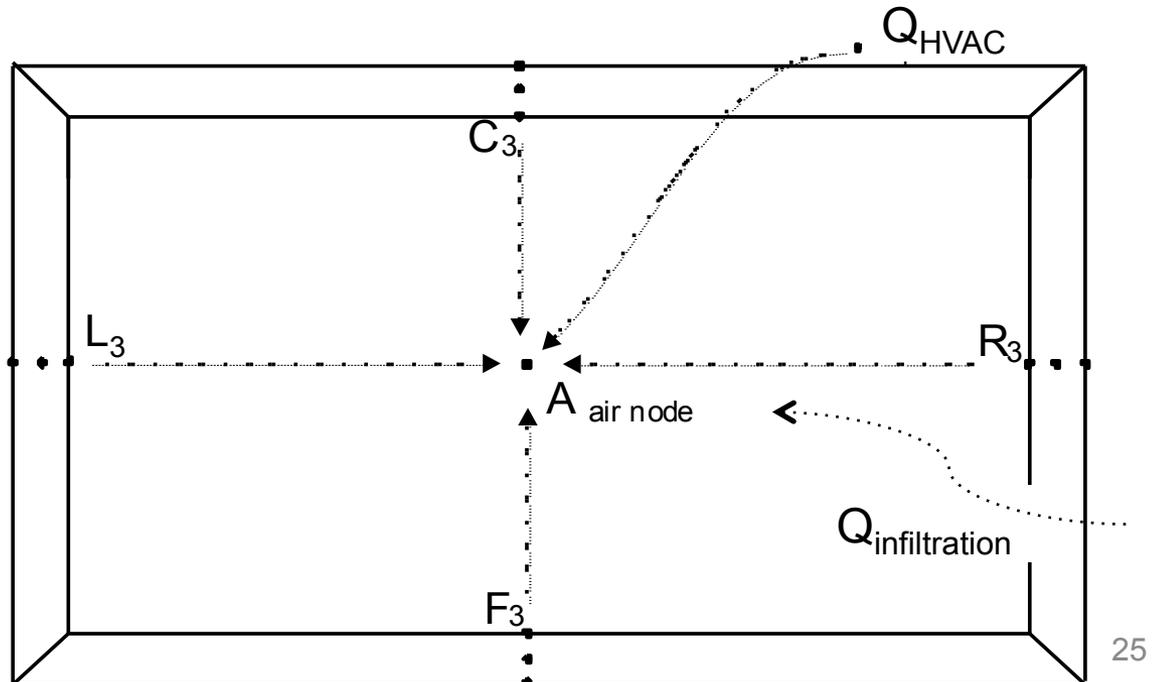
# Unsteady energy balance for air node

- To get the impact on indoor air temperature (and close the system of equations)
  - Write an energy balance on the indoor air node
  - Air impacted directly only by convection (bulk and surface)

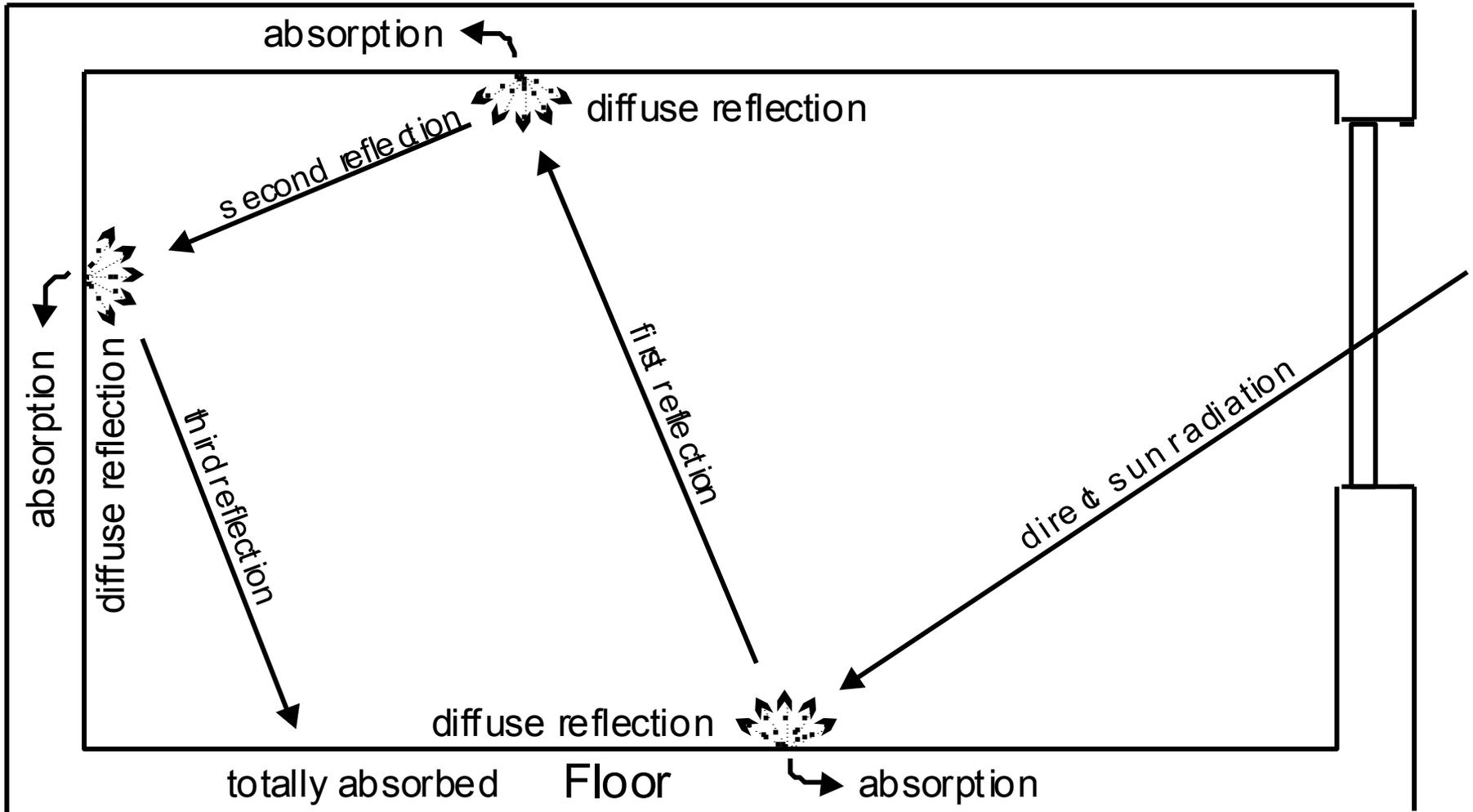
$$(V_{room} \rho_{air} c_{p,air}) \frac{dT_{air,in}}{dt} = \sum_{i=1}^n h_i A_i (T_{i,surf} - T_{air,in}) + \dot{m} c_p (T_{out} - T_{air,in}) + Q_{HVAC}$$

## In plain English:

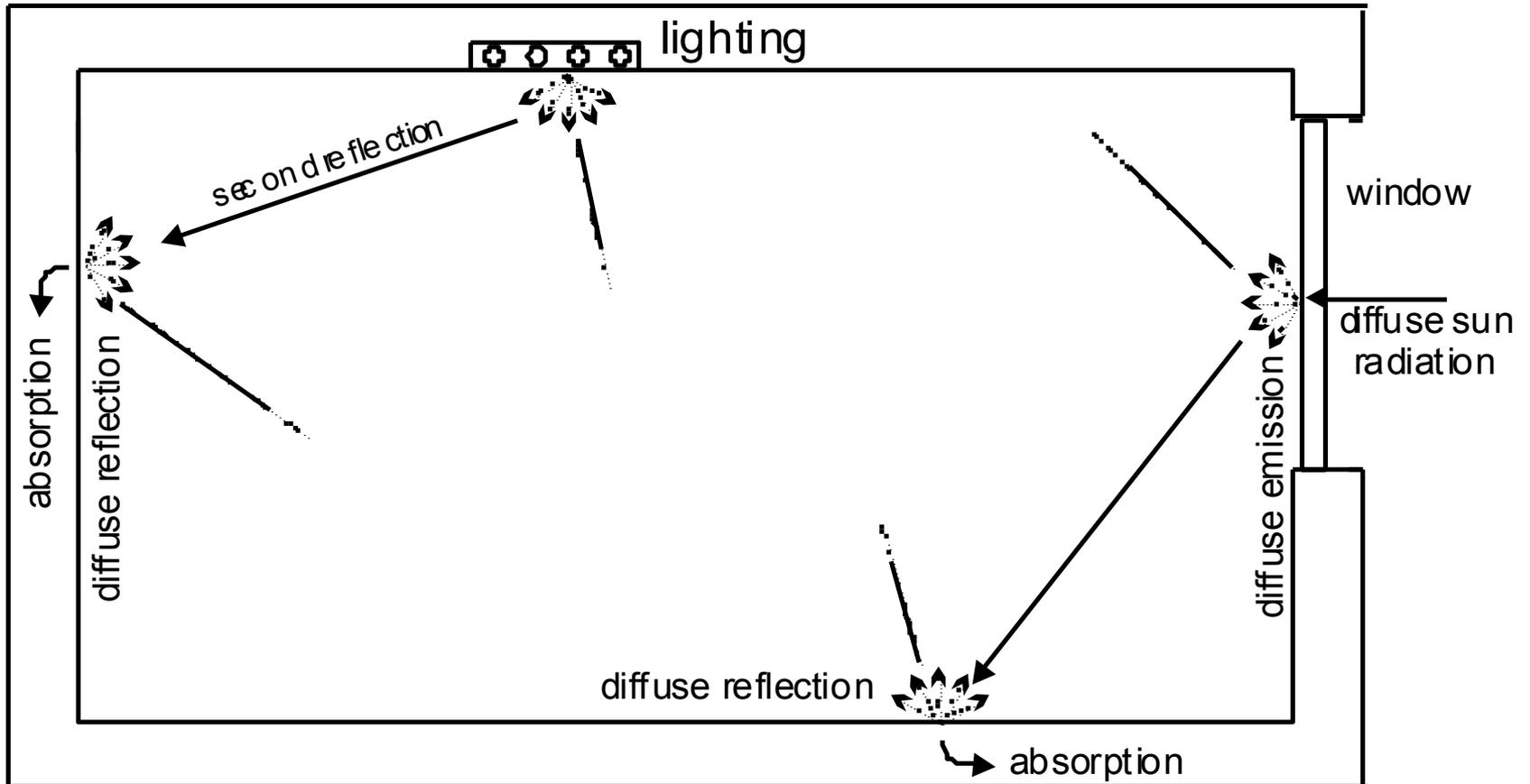
The change in indoor air temperature is equal to the sum of convection from each interior surface plus outdoor air delivery (by infiltration or dedicated outdoor air supply), plus the bulk convective heat transfer delivered by the HVAC system



# Adding a window: Direct solar radiation

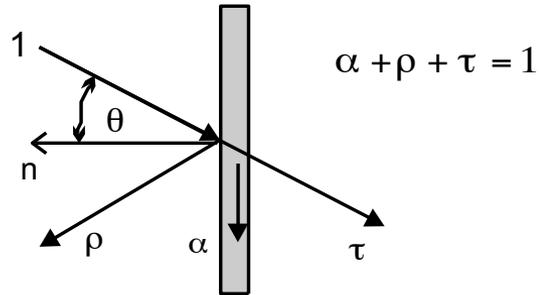


# Adding a window: Diffuse solar radiation

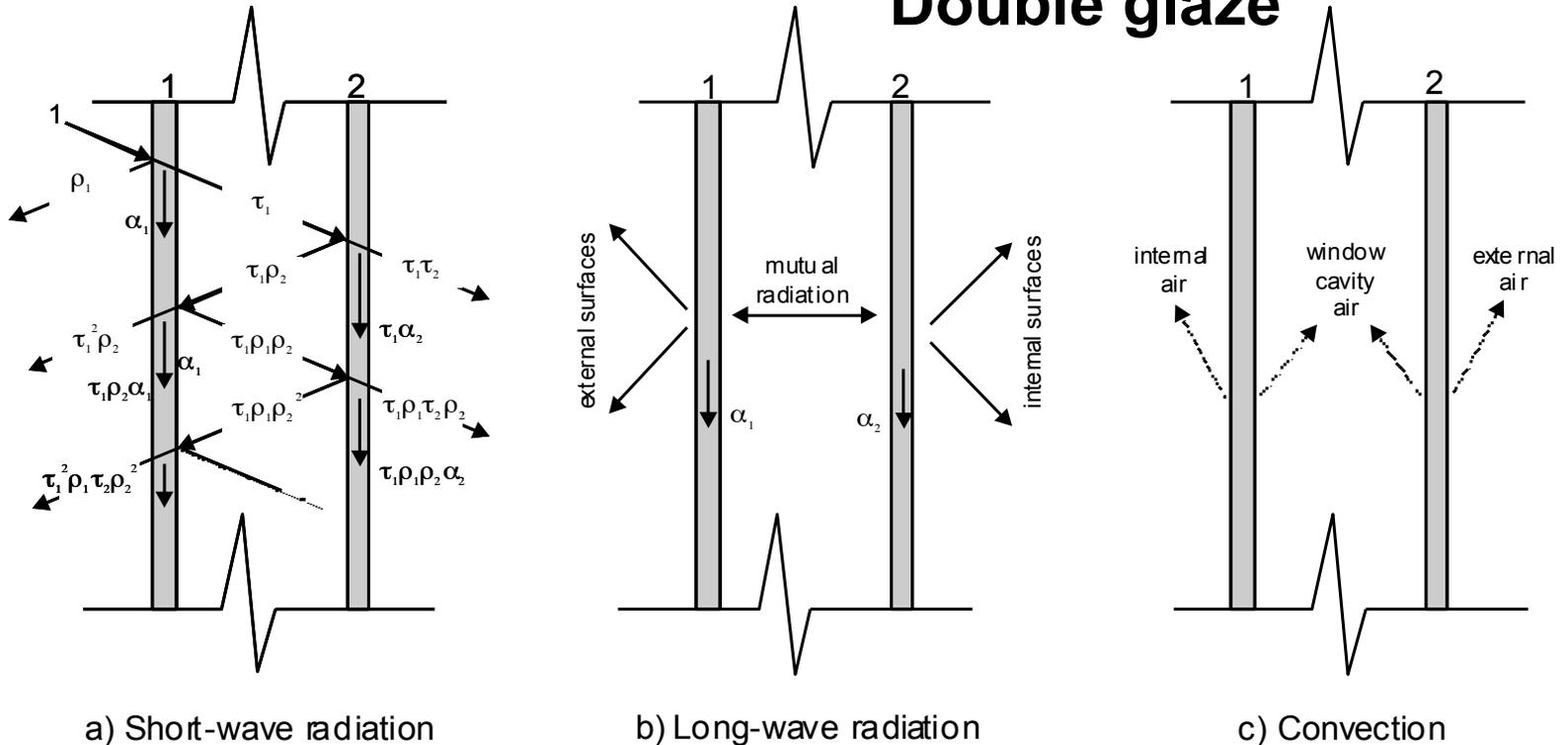


# Heat transfer in windows

## Single glaze

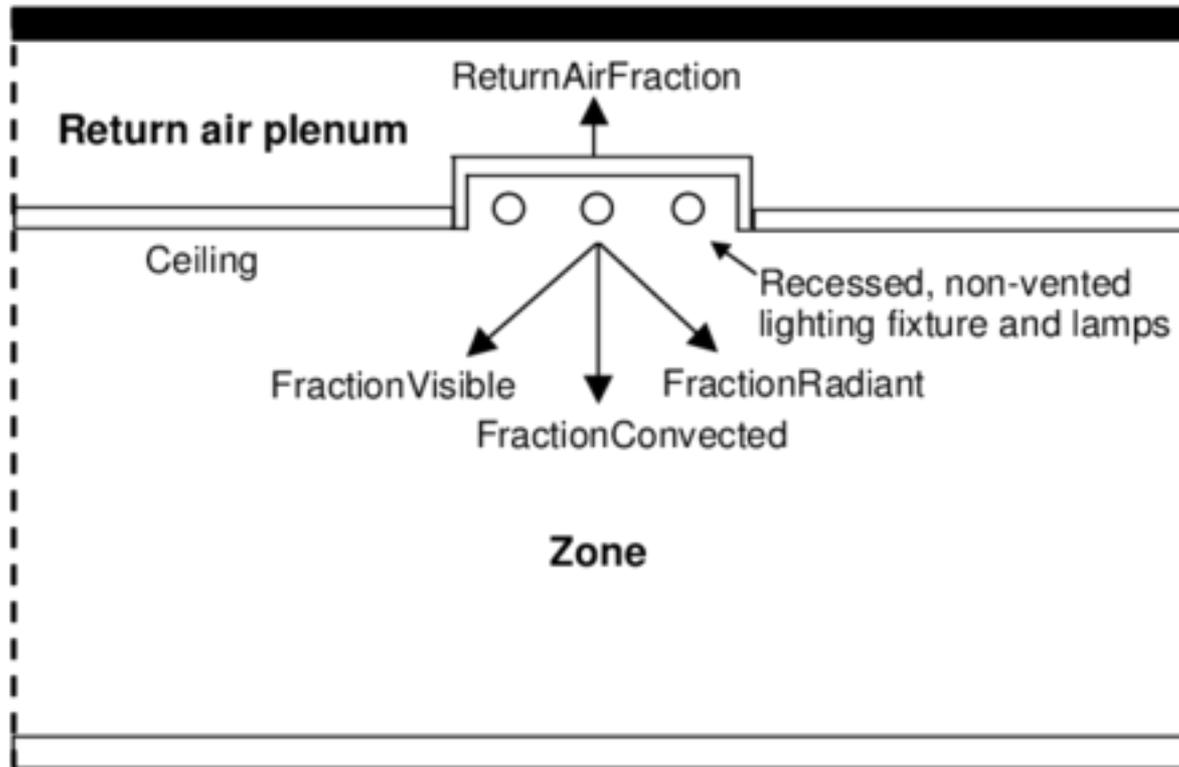


## Double glaze



# Internal heat sources (e.g., lighting)

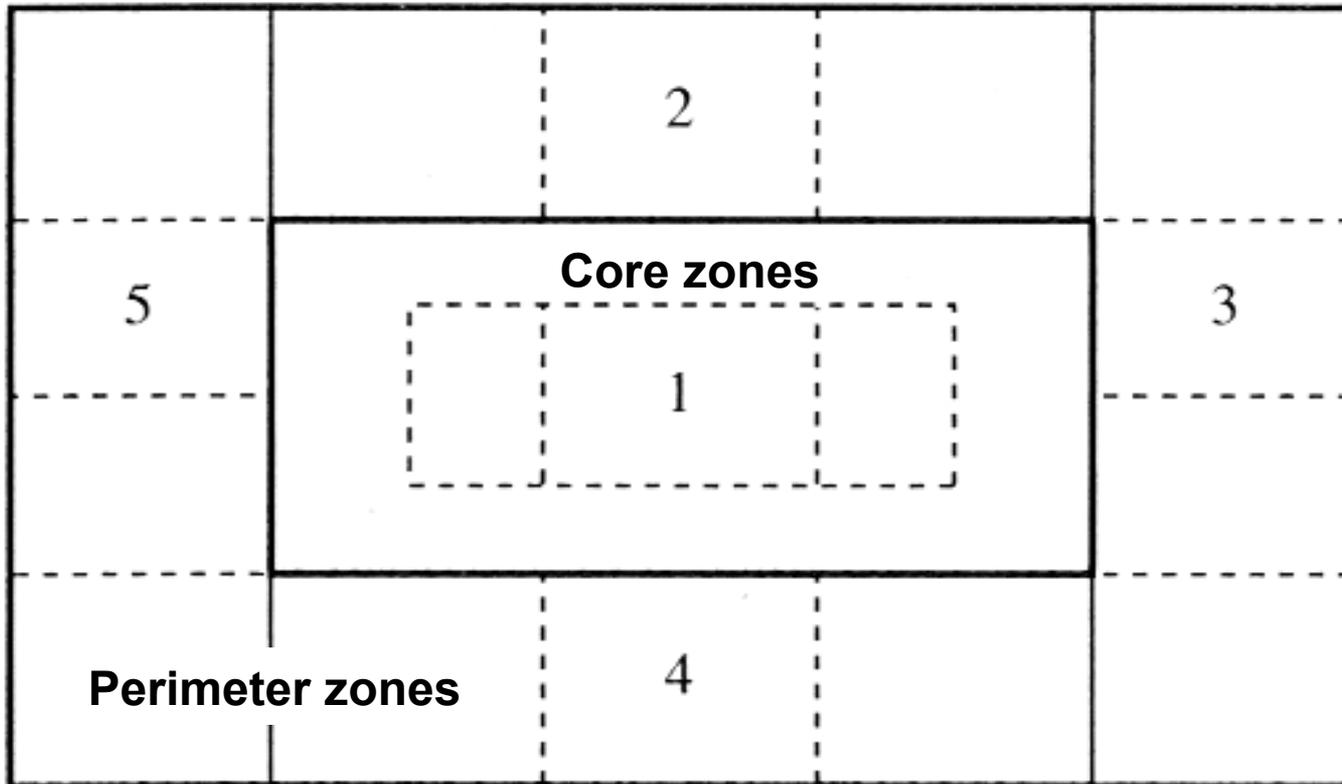
- Sources of both convective and radiative heat flux



# Zoning

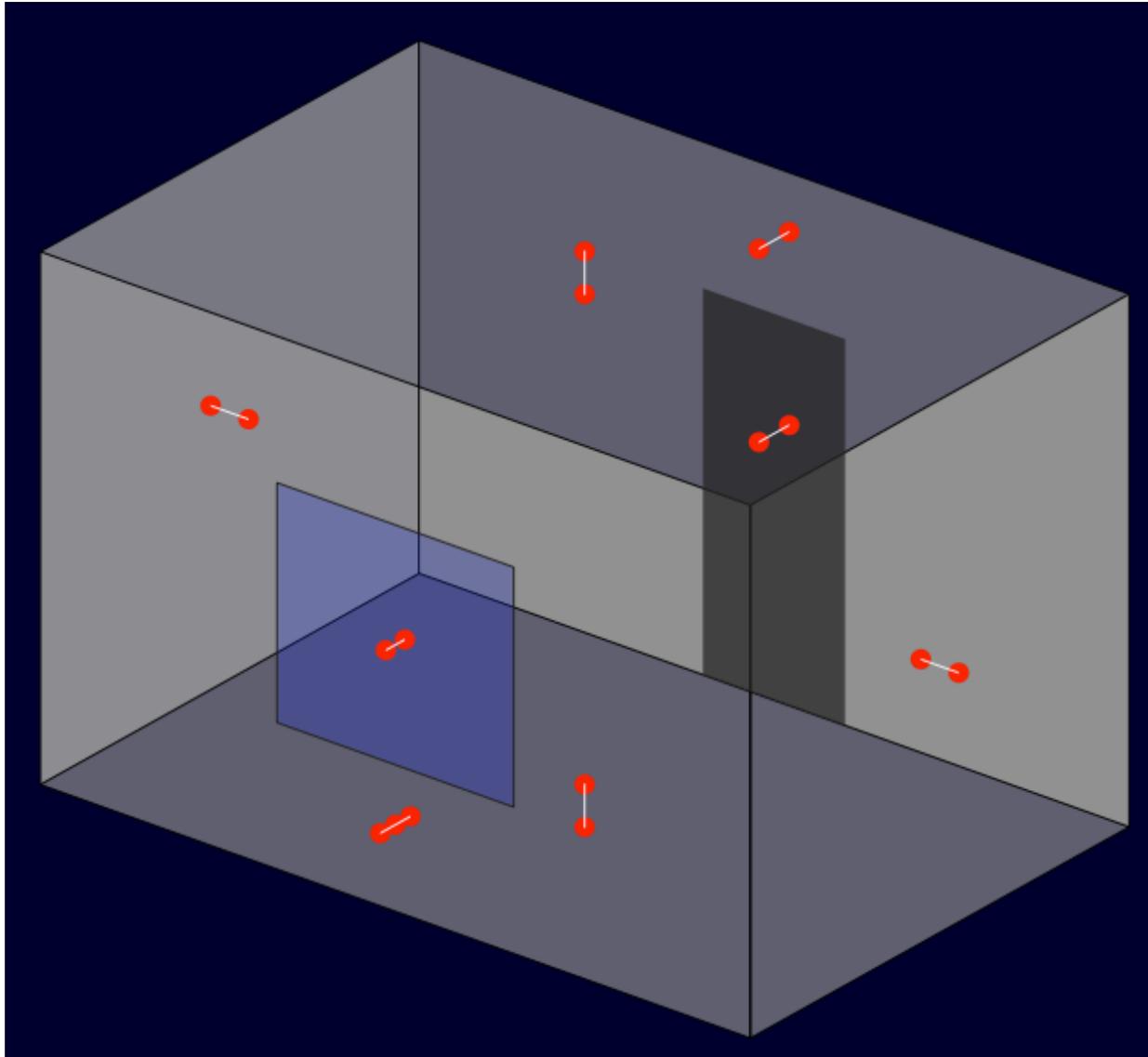
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Cooling load calculations (and heating load calculations) can be done room-by-room or zone-by-zone, and summed up for the whole building

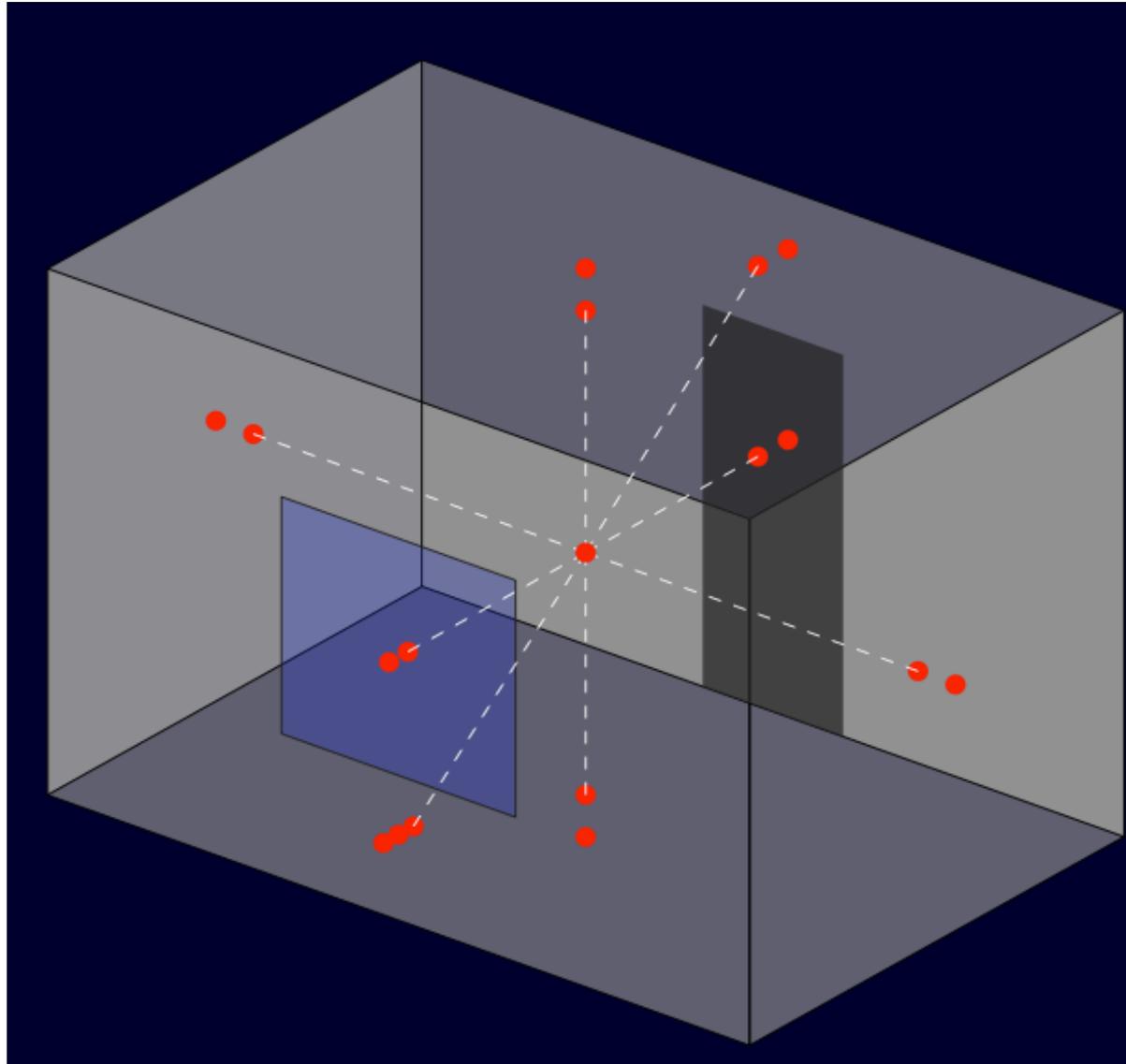


# Simplest 'box' model: **Conduction** elements

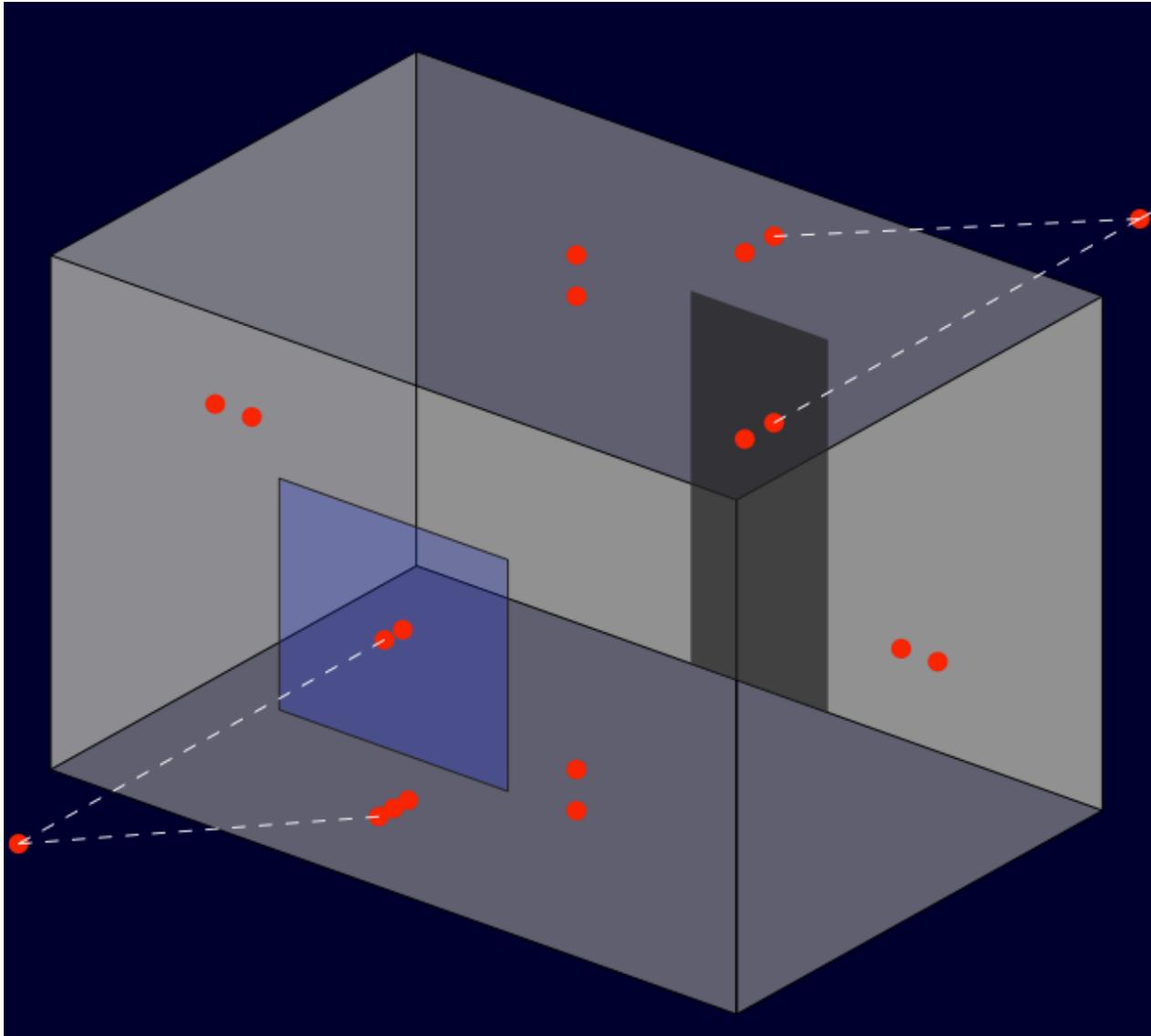
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# Simplest 'box' model: **Interior convection** elements

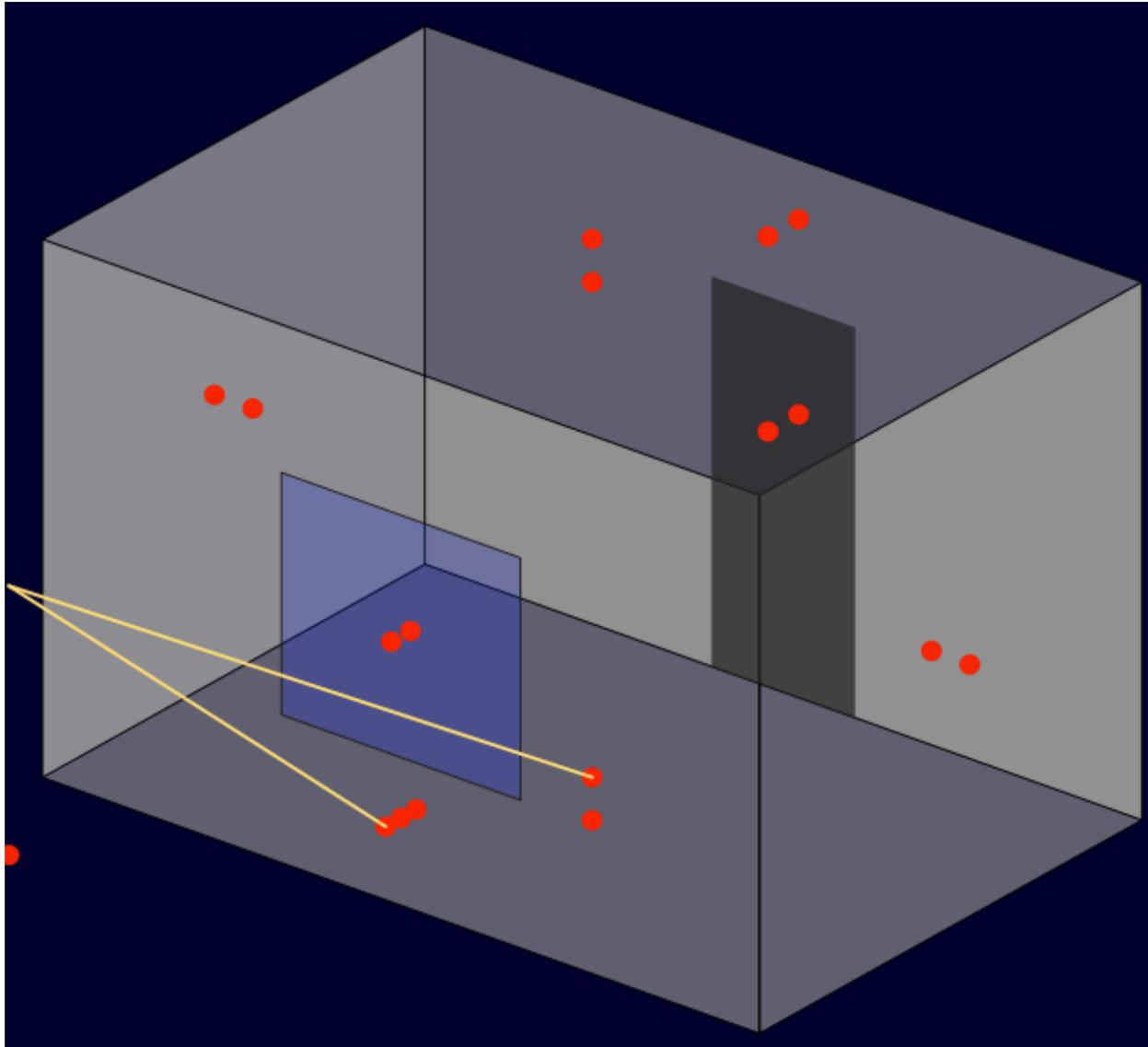


# Simplest 'box' model: **Exterior convection** elements

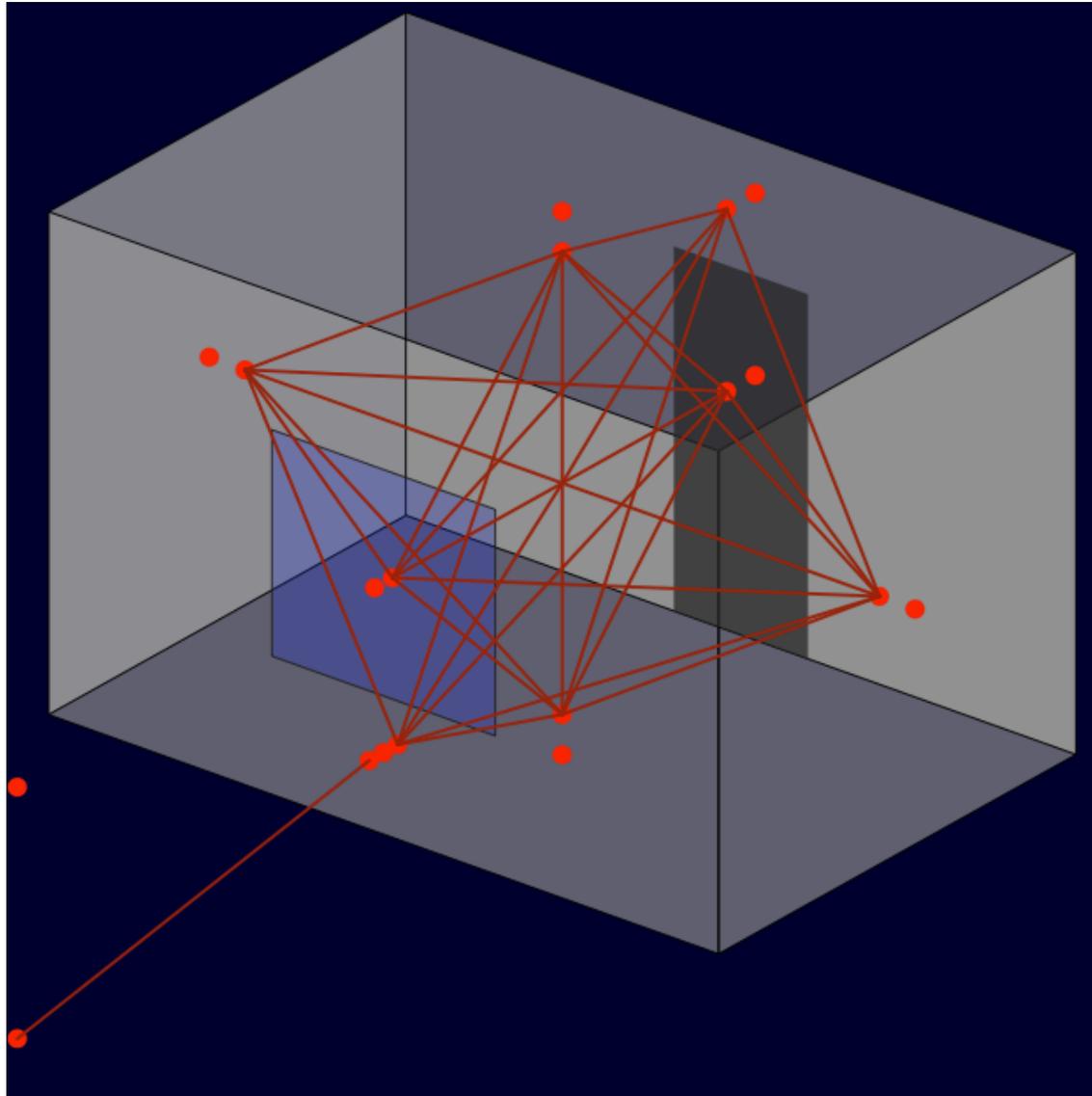


# Simplest 'box' model: **Solar (direct + diffuse)**

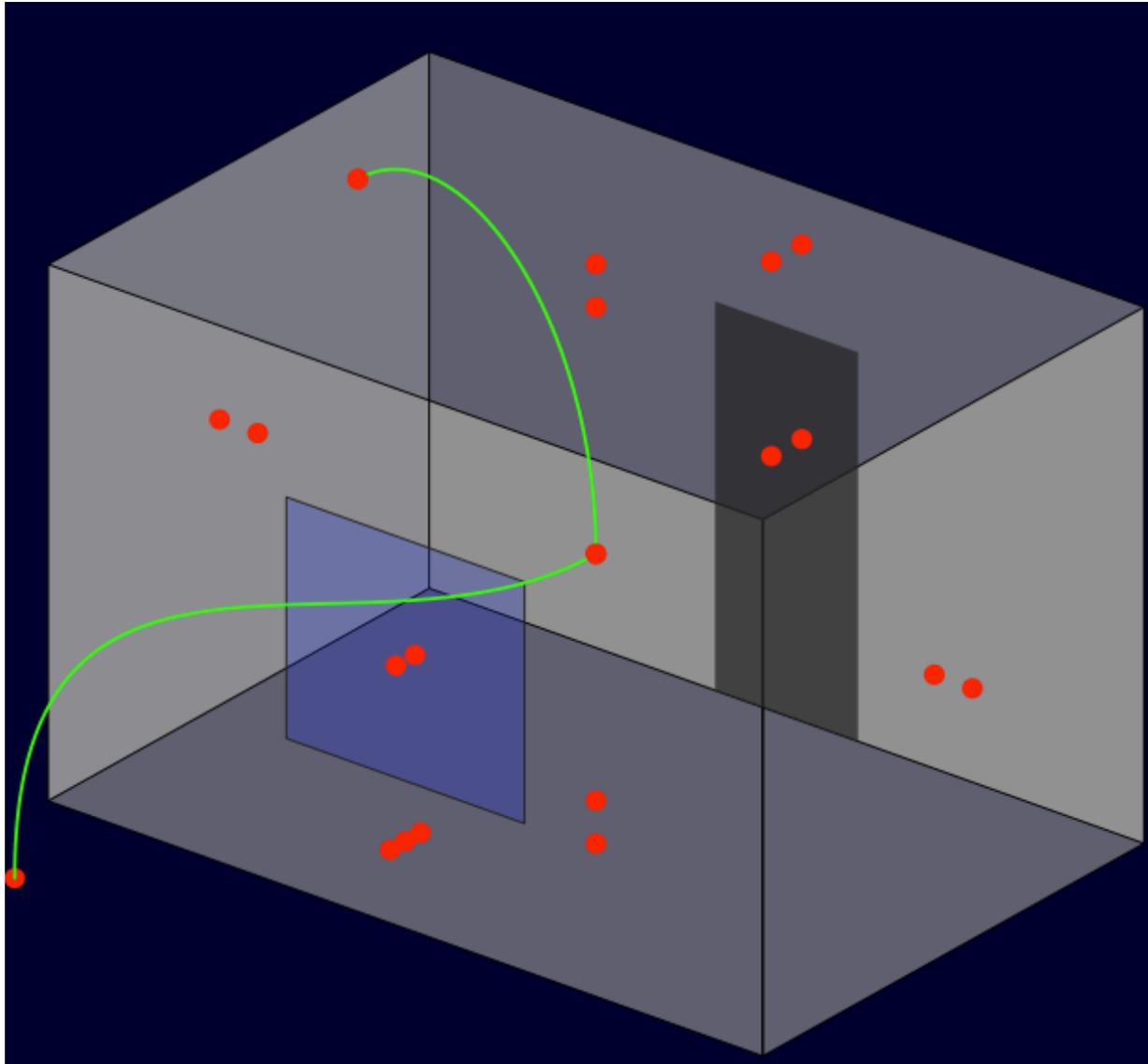
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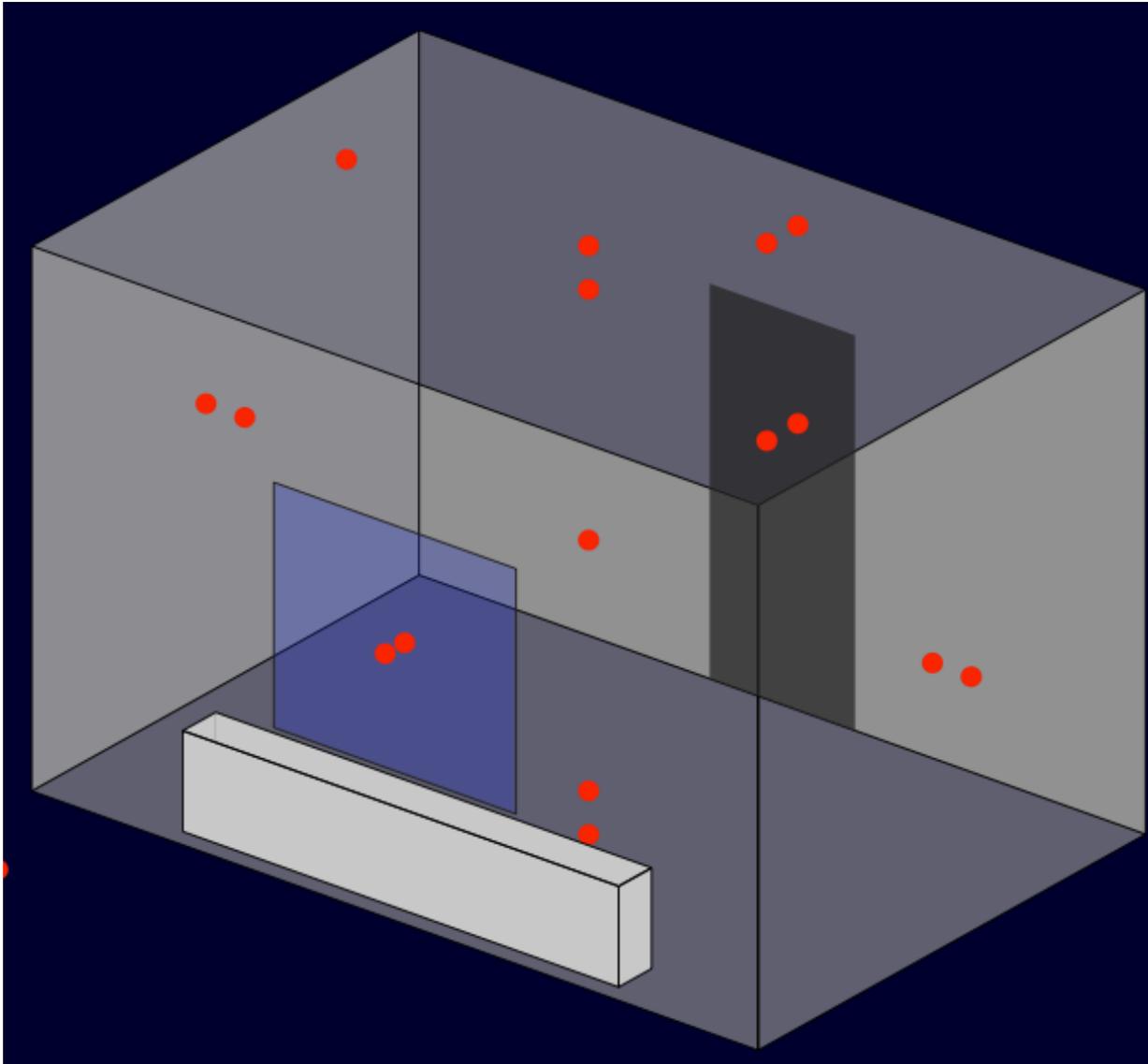
# Simplest 'box' model: Long wave radiation elements



# Simplest 'box' model: **Ventilation/infiltration** elements



# Simplest 'box' model: **Internal mass** (e.g., furniture)

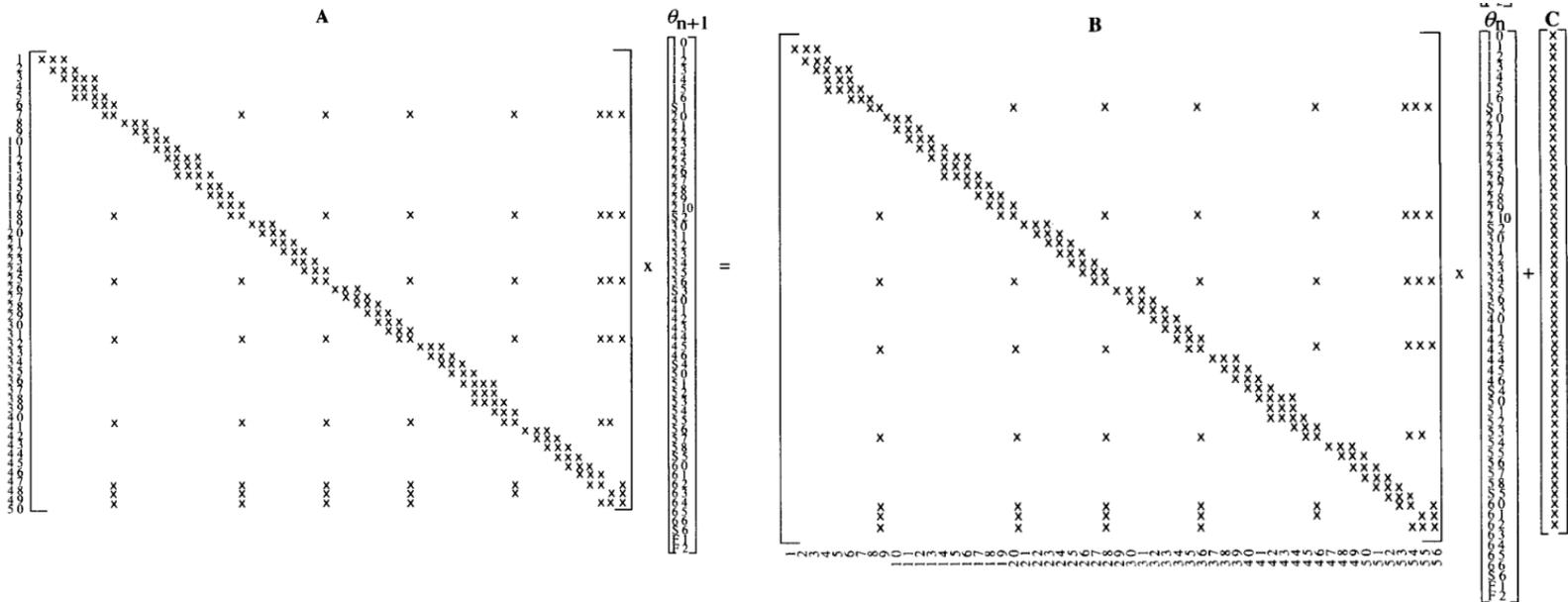


# Solving the system of equations

In matrix notation, the system of equations can be expressed as

$$\mathbf{A}\theta_{n+1} = \mathbf{B}\theta_n + \mathbf{C} = \mathbf{Z} \quad (4.1)$$

where  $\mathbf{A}$  is a sparse matrix of future time-row coefficients of the nodal temperature or heat injection terms of the conservation equations,  $\mathbf{B}$  the corresponding matrix established at the present time-row,  $\mathbf{C}$  a column matrix of known boundary excitations relating to the present and future time-rows,  $\theta$  a column matrix of nodal temperatures and heat injections,  $n + 1$  refers to the future time-row,  $n$  the present time-row, and  $\mathbf{Z}$  is a column matrix. Initial conditions are given by  $\theta(0) = \theta_0$ .



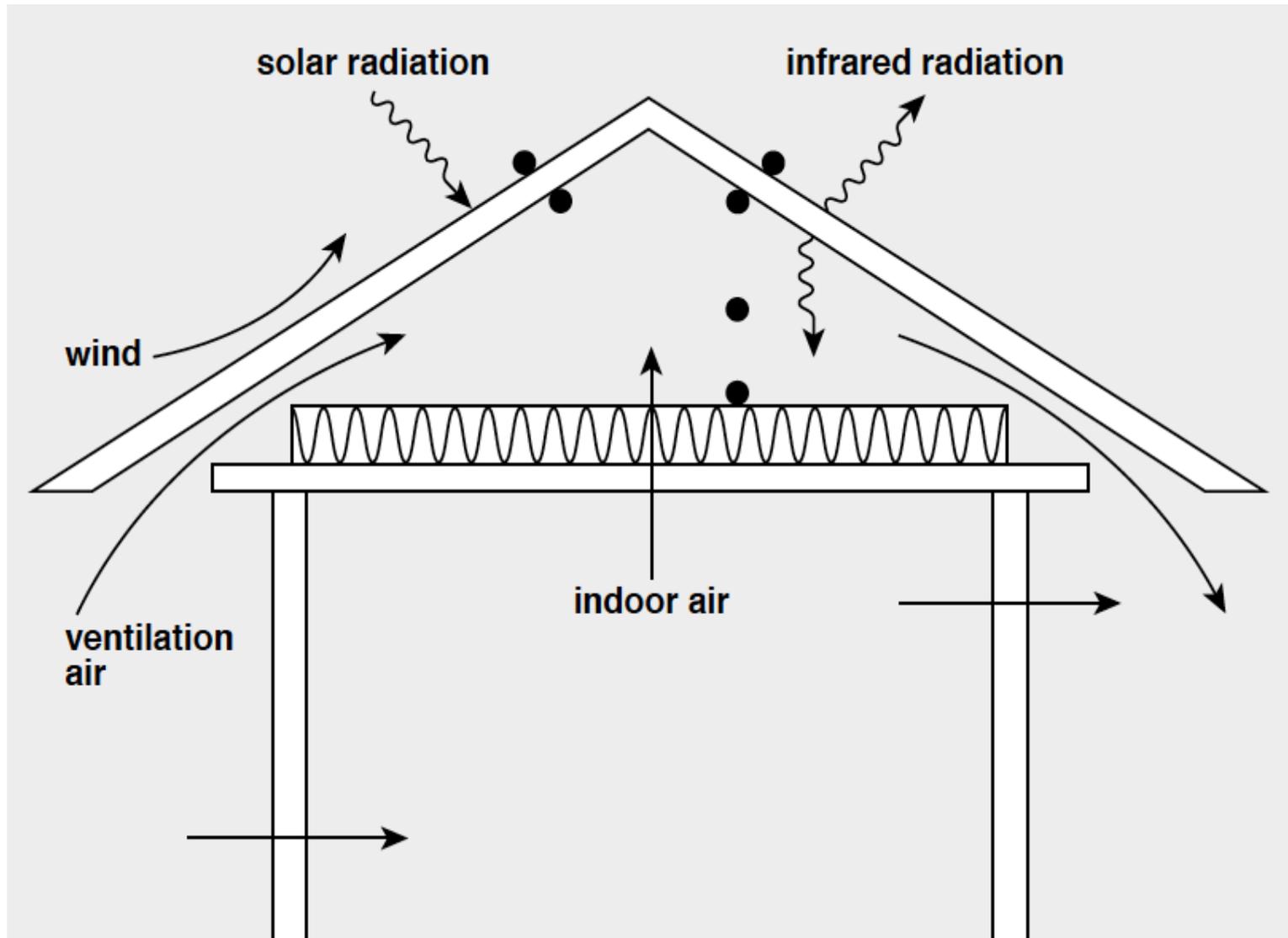
# Important input parameters for energy simulation

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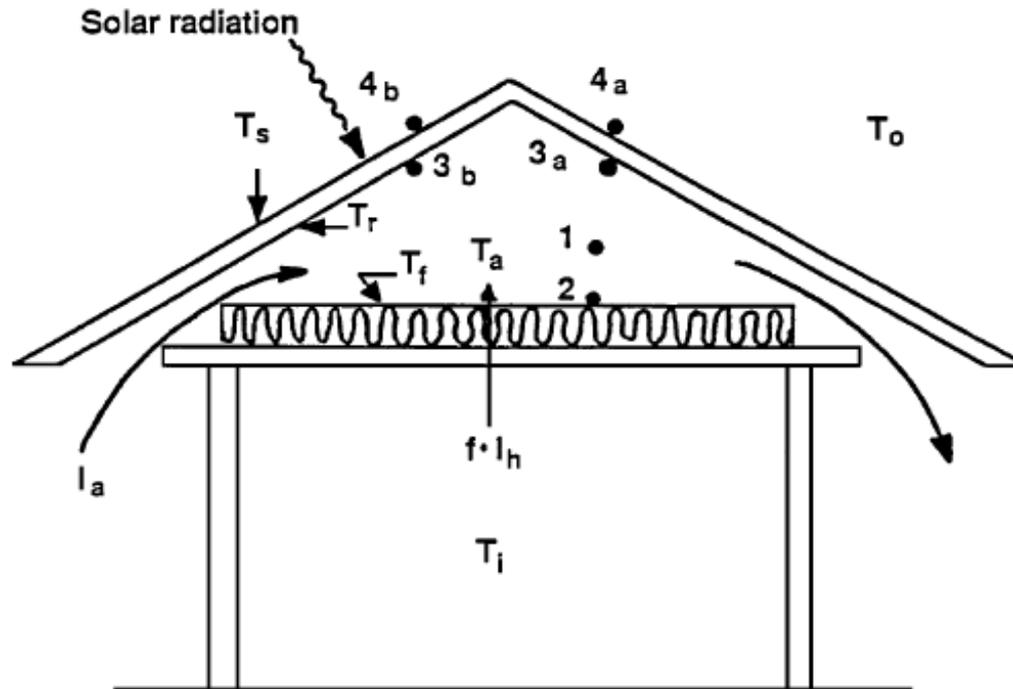
- Conduction (and storage) solution method
  - Finite difference (explicit, implicit)
  - Response functions techniques
- Time steps
  - Too short and calculations take forever
  - Too long and solutions diverge
- Meteorological data (TMY, AMY)
  - Temperature, wind speed, solar radiation, cloud cover
- Radiation and convection models
  - Internal and external
- Windows and shading
- Air infiltration models
- Conduction to the ground
- HVAC system and control models

**BUILDING ENERGY SIMULATION**  
**EXAMPLE: ATTIC HEAT TRANSFER**

# Attic simulation example



# Attic heat transfer



● Nodes for heat balance

$T_a$ ,  $T_i$ ,  $T_f$     Temperatures of attic, indoor air, attic floor  
 $T_o$ ,  $T_r$ ,  $T_s$     outside air, underside of roof, surface of roof

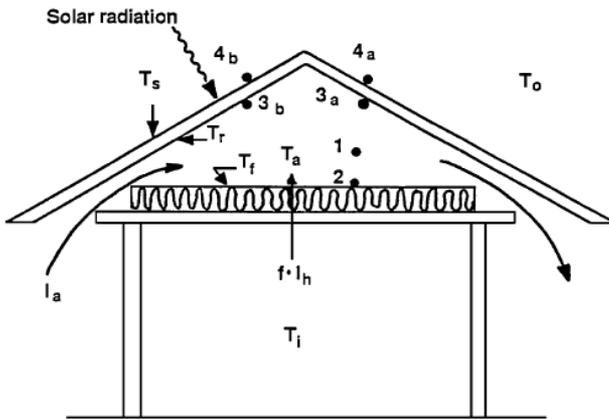
$f$     Fraction of air entering attic

$I_a$ ,  $I_h$     Ventilation rates for attic and house, vol. changes/hour

# Attic heat transfer

**Attic Air**—The heat balance for the attic air (node 1) is given by

$$\begin{aligned}
 & A_c h_f (T_f - T_a) + f I_h V_h \rho C_p (T_i - T_a) \\
 &= \frac{A_r}{2} h_{r,1} (T_a - T_{r,1}) + \frac{A_r}{2} h_{r,2} (T_a - T_{r,2}) + \frac{A_{es}}{R_{es}} (T_a - T_o) \\
 &+ I_a \rho C_p V_a (T_a - T_o)
 \end{aligned}$$



- Nodes for heat balance
- $T_a, T_i, T_f$  Temperatures of attic, indoor air, attic floor
- $T_o, T_r, T_s$  outside air, underside of roof, surface of roof
- $f$  Fraction of air entering attic
- $I_a, I_h$  Ventilation rates for attic and house, vol. changes/hour

where

- $A_c, A_r,$   
 $A_{es}$  = surface areas of ceiling, total roof area, and combined area of soffit and end walls ( $\text{ft}^2$ )
- $C_p$  = specific heat of air ( $\text{Btu}/\text{lb}\cdot^\circ\text{F}$ )
- $f$  = fraction of house exfiltration that transfers into attic
- $h_f, h_{r,n}$  = convective heat transfer coefficients at attic floor and underside of roof (surface  $n$ ), respectively ( $\text{Btu}/\text{h}\cdot\text{ft}^2\cdot^\circ\text{F}$ )
- $I_h$  = house exfiltration rate ( $\text{h}^{-1}$ )
- $I_a$  = attic ventilation rate, i.e., outdoor air entering attic ( $\text{h}^{-1}$ )
- $R_{e,s}$  = average thermal resistance of end walls and eaves ( $\text{h}\cdot\text{ft}^2\cdot^\circ\text{F}/\text{Btu}$ )
- $T_a$  = attic air temperature ( $^\circ\text{R}$ )
- $T_f$  = temperature of attic floor surface ( $^\circ\text{R}$ )
- $T_i$  = indoor air temperature ( $^\circ\text{R}$ )
- $T_o$  = outdoor air temperature ( $^\circ\text{R}$ )
- $T_{r,1}$  = temperature of roof sheathing underside  $a$  ( $^\circ\text{R}$ )
- $T_{r,2}$  = temperature of roof sheathing underside  $b$  ( $^\circ\text{R}$ )
- $V_a$  = volume of attic space ( $\text{ft}^3$ )
- $V_h$  = volume of house ( $\text{ft}^3$ )
- $\rho$  = density of air ( $\text{lb}/\text{ft}^3$ )

# Attic heat transfer

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*Attic Floor*—The heat balance for the attic floor (node 2) is

$$\frac{T_i - T_f}{R_c} = h_f(T_f - T_a) + \frac{F_1}{2}(T_f - T_{r,1}) + \frac{F_2}{2}(T_f - T_{r,2}) \quad (3)$$

where

$R_c$  = thermal resistance of attic floor (ceiling)  
(h·ft<sup>2</sup>·°F/Btu)

$F_1, F_2$  = radiative heat transfer coefficients between  
attic floor and undersides of roof  
(Btu/h·ft<sup>2</sup>·°F), with the following  
definition:

$$F_n = \frac{\sigma}{(1/\epsilon_f) + (1/\epsilon_r) - 1} (T_f^2 + T_{r,n}^2)(T_f + T_{r,n}) \quad n = 1, 2$$

where

$\epsilon_f$  = emissivity of attic floor surface  
(assumed to be 0.9)

$\epsilon_r$  = emissivity of roof sheathing surface  
(underside, assumed to be 0.9)

$\sigma$  = Stefan–Boltzman constant (Btu/h·ft<sup>2</sup>·°R<sup>4</sup>)

# Attic heat transfer

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*Sheathing*—The heat balance at the underside of sheathing (nodes 3a and 3b) is

$$\frac{T_{r,n} - T_{s,n}}{R_r} = h_r(T_a - T_{r,n}) + \frac{A_c}{A_r} F_n (T_f - T_{r,n}) + \frac{2}{A_r} L_h W_{r,n} \quad n = 1, 2 \quad (5)$$

where

- $L_h$  = latent heat of vaporization (1,050 Btu/lb)
- $R_r$  = thermal resistance of roof (h·ft<sup>2</sup>·°F/Btu)
- $T_{s,n}$  = temperature of outside roof surface (°R)
- $W_{r,n}$  = rate of moisture adsorption into sheathing (lb/h)

# Attic heat transfer

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The heat balance at the top surface of sheathing (nodes 4a and 4b) is

$$\frac{T_{s,n} - T_{r,n}}{R_r} = \alpha I_n + (h_{o,n} + h_{IR})(T_o - T_{s,n}) - L_{IR} \quad n = 1, 2 \quad (6)$$

where

- $h_{IR}, L_{IR}$  = adjustments for infrared radiation exchange with sky (see Eqs. (7), (8), and (9))
- $h_{o,n}$  = convective heat transfer coefficient at exterior roof surface  $n$  (Btu/h·ft<sup>2</sup>·°F)
- $I_n$  = total solar radiation incident on roof surface (Btu/h·ft<sup>2</sup>)
- $\alpha$  = solar absorptance

# Attic heat transfer

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$$h_{\text{IR}} = 4\varepsilon_s \sigma T_o^3 \quad (7)$$

$$L_{\text{IR}} = \varepsilon_s \sigma T_o^4 (1 - \varepsilon_{\text{IR}}) \quad (8)$$

where

$\varepsilon_s$  = emissivity of roof shingles (assumed to be 0.9)

$\varepsilon_{\text{IR}}$  = sky emissivity with clouds

The sky emissivity is calculated with equations from Martin and Berdahl (1984). The emissivity for a clear sky is

$$\varepsilon_0 = 0.711 + 0.56 \frac{T_d}{100} + 0.73 \left( \frac{T_d}{100} \right)^2 + 0.013 \cos \left( \frac{2\pi t}{24} \right) \quad (9)$$

where

$\varepsilon_0$  = emissivity of clear sky

$T_d$  = outdoor dew point temperature (°C)

$t$  = time (h)

and the emissivity of the sky with clouds is

$$\varepsilon_{\text{IR}} = \varepsilon_0 + 0.784C(1 - \varepsilon_0) \quad (10)$$

where  $C$  = total cloud cover as recorded by National Climatic Center (Asheville, NC). Values of  $C$  range from 0 to 10.

# Attic heat transfer

## Sheathing surface temperature: Measured vs. modeled

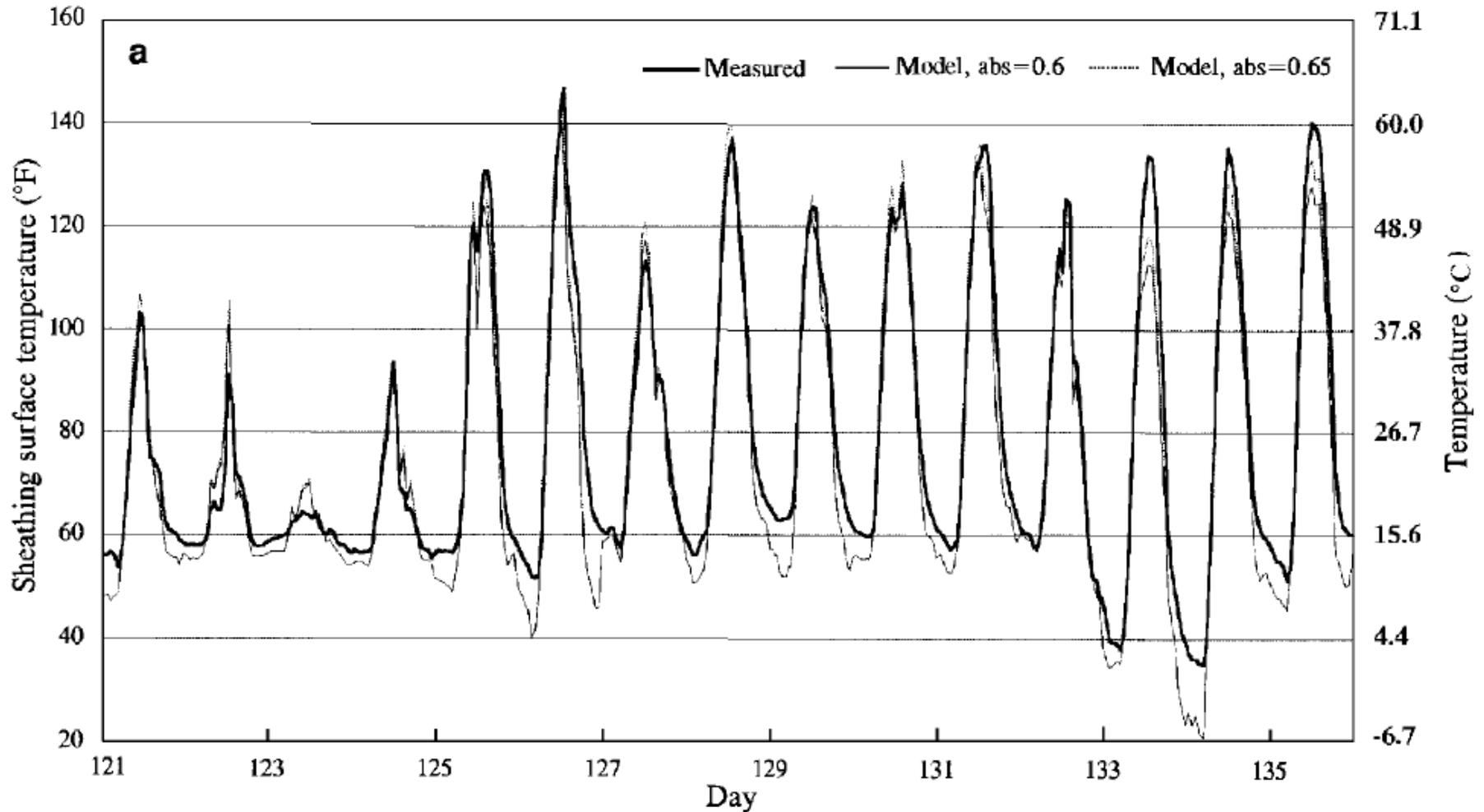


Figure 4—Exterior sheathing surface temperature, bay 2, May 1–15, 1993.

# Attic heat transfer

## Attic air temperature: Measured vs. modeled

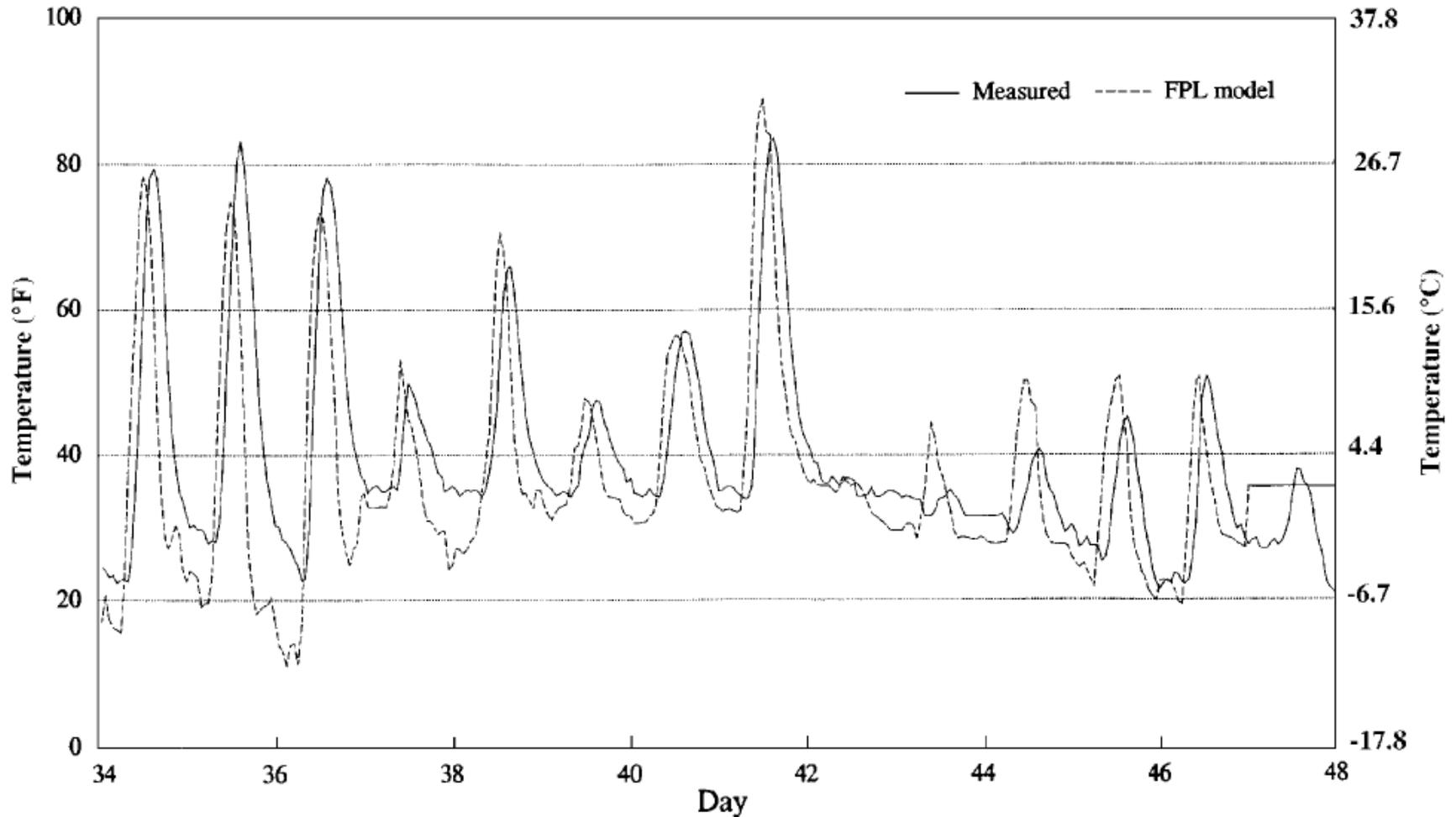


Figure 5—Attic air temperature, bay 2, February 3–16, 1993; absorptance = 0.65.

# Attic heat transfer summary

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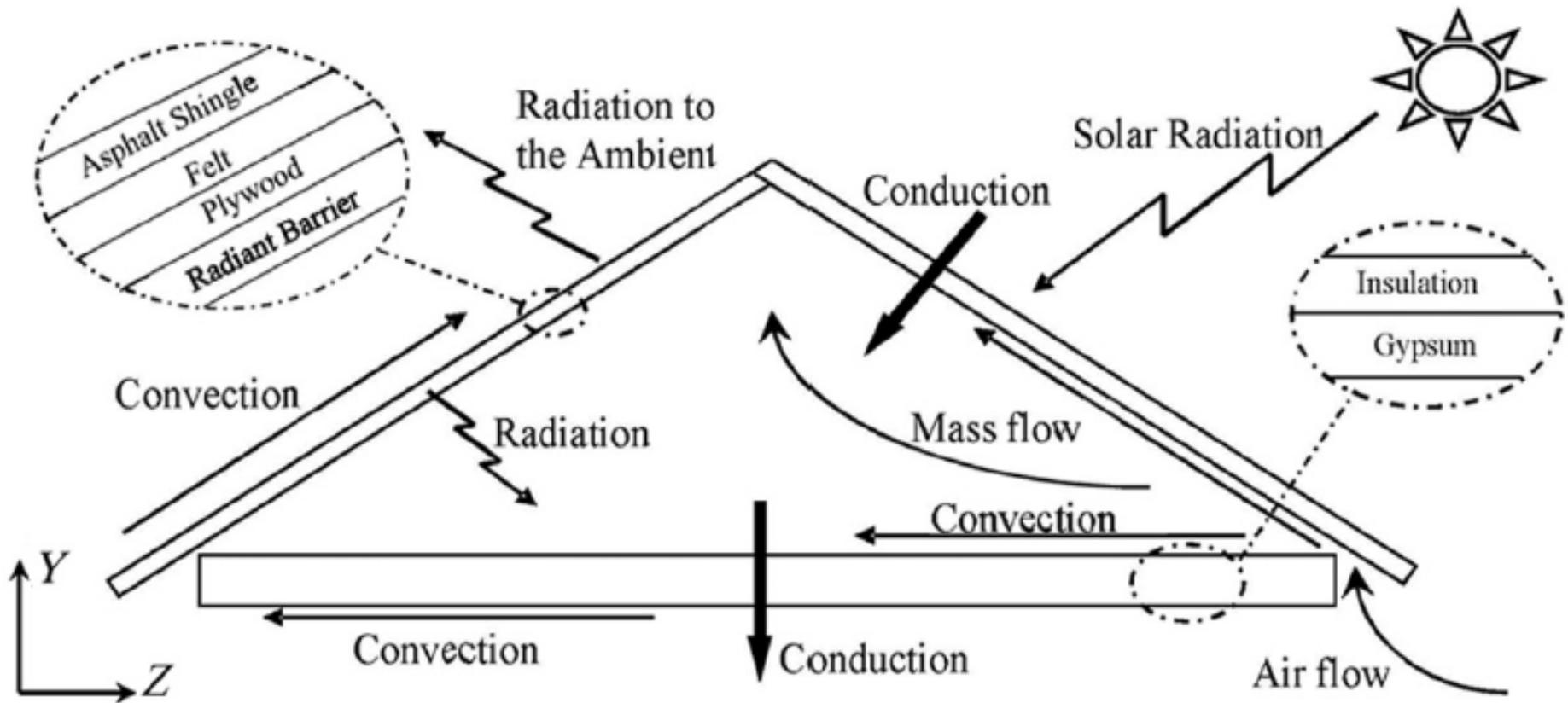
- Attic temperature is important
  - HVAC equipment is often located in attics
  - Impacts conduction across ceiling into interior space
- Ways to reduce attic temperatures?
  - Increase convective heat transfer
    - Attic ventilation
  - Reduce exterior roof surface temperature
    - ‘Cool roof’ low absorptivity materials on the exterior
  - Reduce attic floor surface and underside sheathing temperatures
    - Low-emissivity materials inside attic
      - Attic floor or underside of sheathing
    - Radiant barriers

# Radiant barriers

- **Radiant barriers** typically have LW emissivity less than  $\sim 0.1$ 
  - Approximately 90% of materials have emissivity of 0.9
- Inhibits heat flow through radiation only
  - Doesn't directly impact convection or conduction



# Modeling the impacts of radiant barriers



# Modeling the impacts of radiant barriers

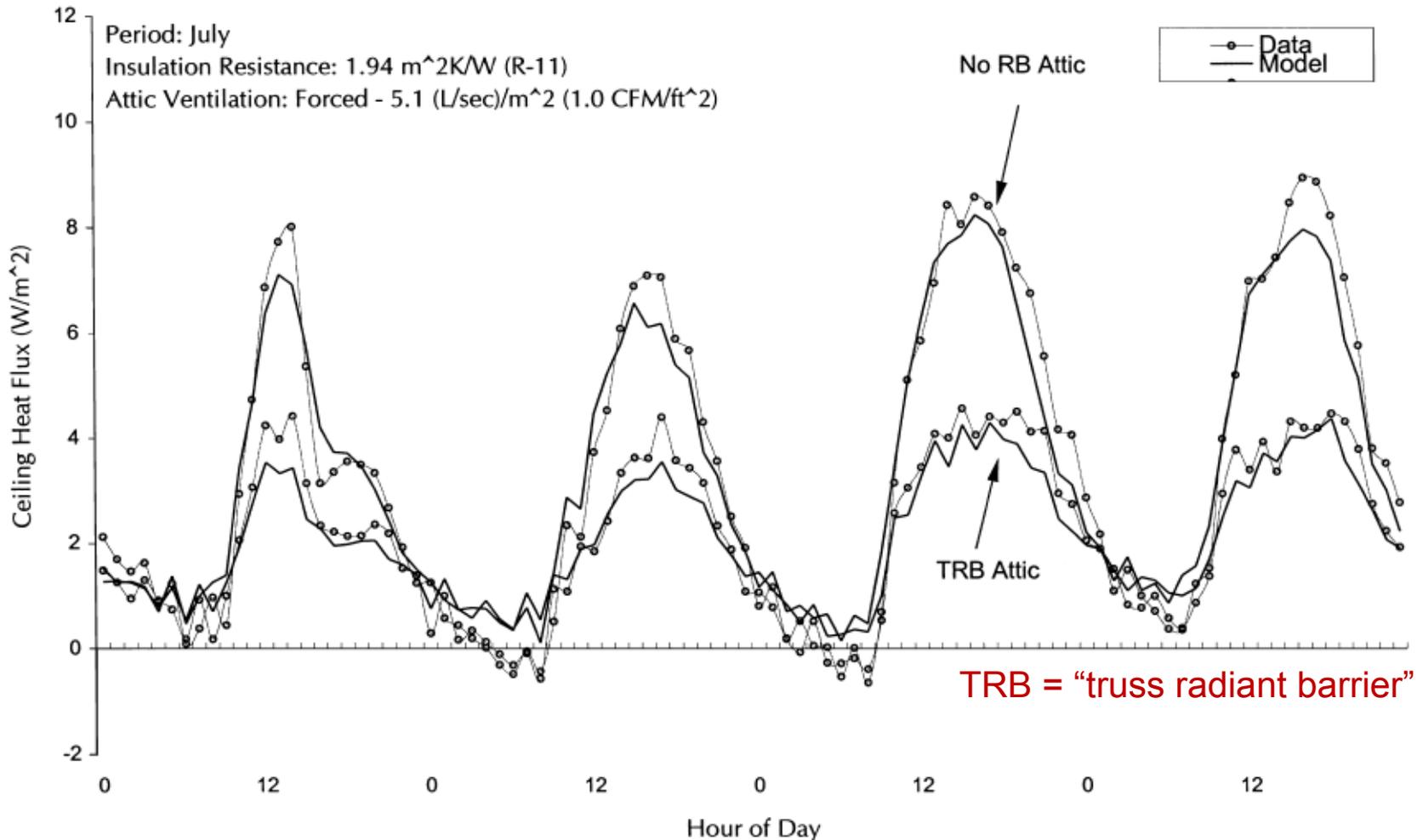


Fig. 6. Ceiling heat fluxes (TRB case, insulation resistance:  $1.94 \text{ m}^2 \text{ K/W}$ , R-11; with attic airflow rate:  $5.1 \text{ l/s/m}^2$ ,  $1.0 \text{ CFM/ft}^2$ ).

# Modeling the impacts of radiant barriers

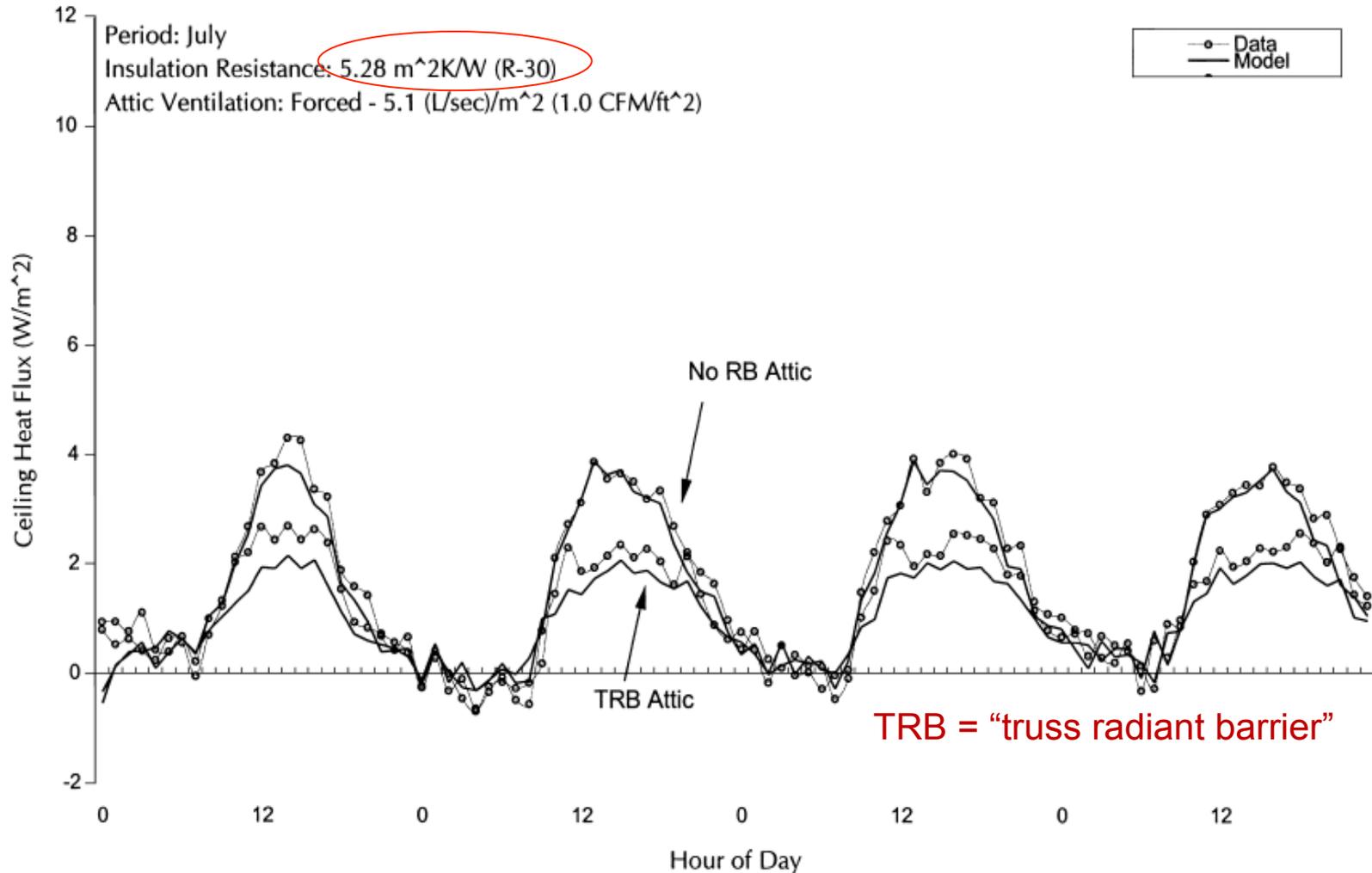
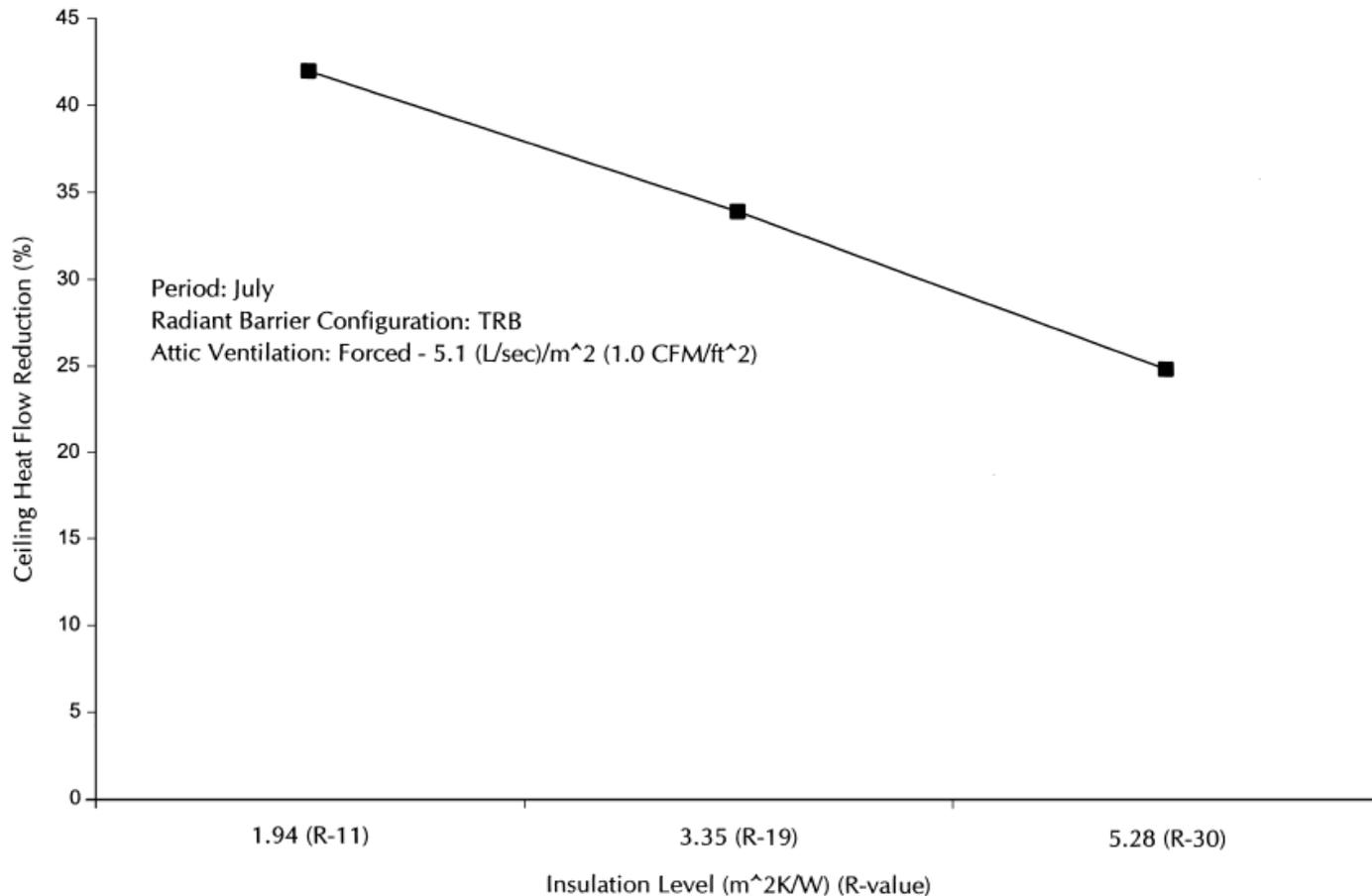


Fig. 7. Ceiling heat fluxes (TRB case, insulation resistance: 5.28 m<sup>2</sup> K/W, R-30; with attic airflow rate: 5.1 l/s/m<sup>2</sup>, 1.0 CFM/ft<sup>3</sup>).

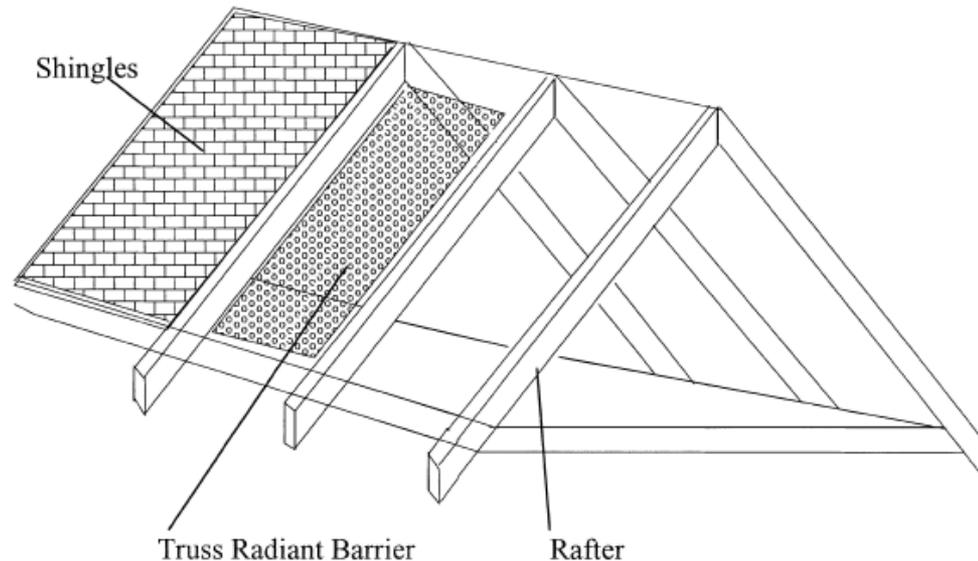
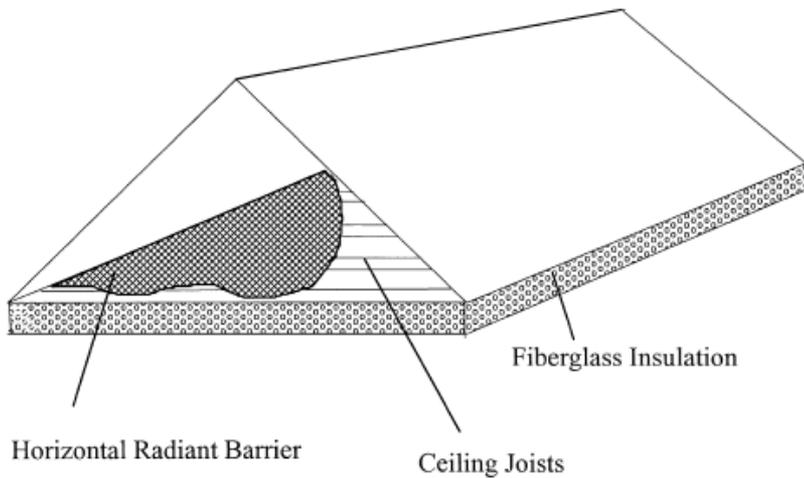
# Modeling the impacts of radiant barriers

- Radiant barriers have less of an impact on well-insulated roofs



# Modeling the impacts of radiant barriers

- Should we install radiant barriers on attic floors or underside of roof sheathing?



# Modeling the impacts of radiant barriers

- Should we install radiant barriers on attic floors or underside of roof sheathing?

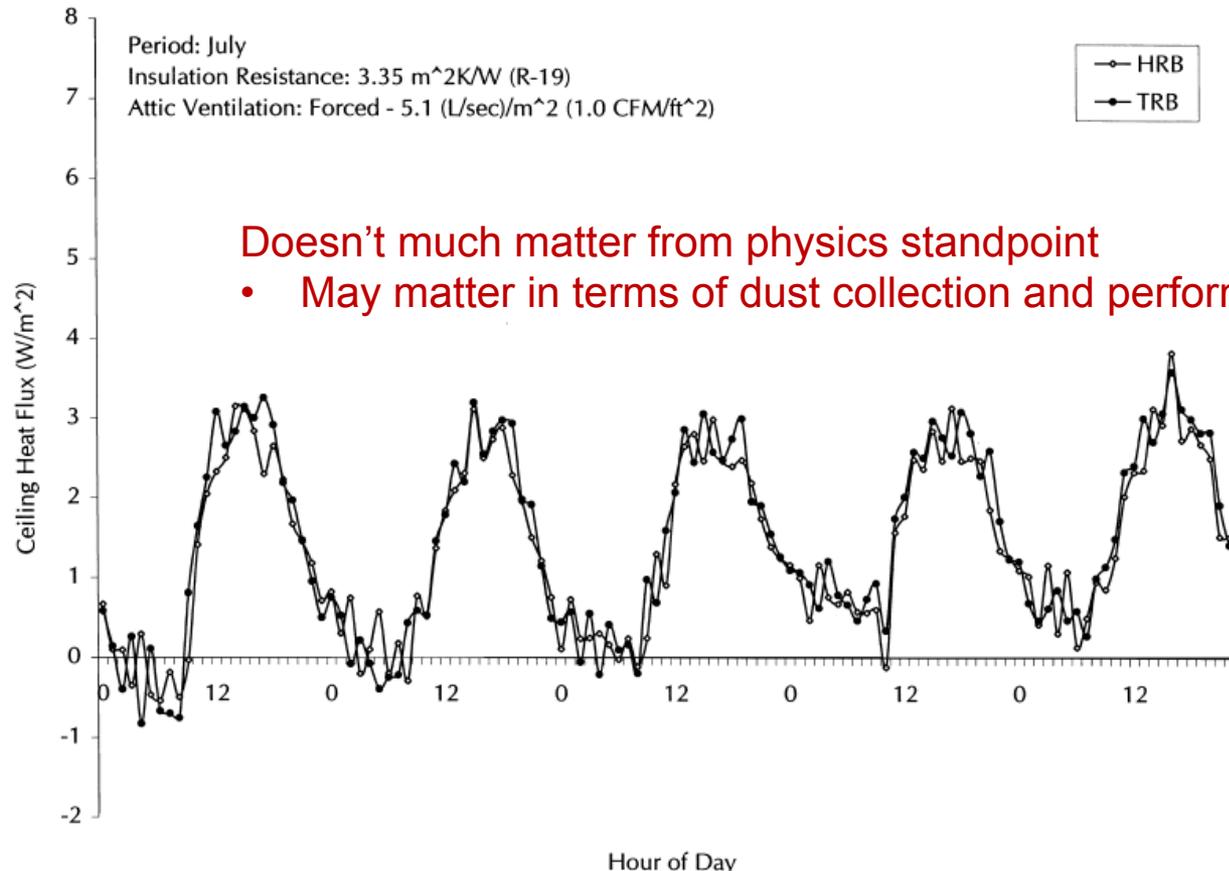


Fig. 9. Comparison between HRB and TRB configurations — experimental (insulation resistance: 3.35 m<sup>2</sup> K/W, R-19; with airflow rate: 5.1 l/s/m<sup>2</sup>, 1.0 CFM/ft<sup>2</sup>).

# Roof and attic heat transfer simulation summary

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- Roof surfaces can be extremely hot
  - Several energy and material longevity impacts
  - We can alter materials in design to reduce roof temperatures
- Attic air can also be very warm
  - Also has energy and comfort impacts
  - We now know what governs attic air temperatures
  - We know radiant barriers can help
    - Particularly if you have a poorly insulated roof
    - Better off just insulating roof if you can
- For both of these, we can use thermal modeling approaches in the design phase

# **WHOLE BUILDING ENERGY SIMULATION (BES) PROGRAMS**

# Energy simulation (BES) programs

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- A wide variety of programs exists
  - [http://apps1.eere.energy.gov/buildings/tools\\_directory/subjects\\_sub.cfm](http://apps1.eere.energy.gov/buildings/tools_directory/subjects_sub.cfm)
  - Different levels of functions, user interfaces, and pricing
  - Some have very good GUIs with less functionality
    - Some have the exact opposite
- Most commonly used BES programs:
  - eQUEST (DOE2 engine; free; easy GUI)
  - ESPr (free; difficult to use; research grade)
  - TRNSYS (modular; requires extensive inputs; expensive)
  - TRACE 700 (from Trane; HVAC focus; expensive)
  - EnergyGauge USA (residential only; user-friendly; cheap)
  - EnergyPlus (free; excellent capabilities; modular; difficult to use)
    - Ease of use is improving with DesignBuilder USA, OpenStudio (free), and Simergy (free)
  - IES-VE (expensive; free educational; many capabilities; easy to use)<sub>60</sub>

# Building energy simulation (BES) programs

An Architect's Guide to

## INTEGRATING ENERGY MODELING IN THE DESIGN PROCESS



THE AMERICAN INSTITUTE  
OF ARCHITECTS

MODELING TOOL	CALCULATION ENGINE	GRAPHIC INTERFACE FOR FRONT-END INPUT	GRAPHIC RESULTS PROVIDED	APPROPRIATE FOR EARLY DESIGN PHASE	APPROVED FOR CODE COMPLIANCE MODELING	FREWARE
<b>COMFEN (RESFEN – residential)</b>	EnergyPlus	Yes	Yes	Yes	No	Yes
<b>DesignBuilder</b>	EnergyPlus	Yes	Limited	Yes	Yes	No
<b>Ecotect</b>	CIBSE Admittance Method	Yes	Yes	Yes	No	No
<b>EMIT1.2</b>	None (spread-sheet)	No	Not specifically, (but s/s capability)	Yes	No	Yes
<b>EnergyPro</b>	DOE-2.1E	No	No(auto-generates compliance report)	No	Yes (easiest to use)	No
<b>eQUEST®</b>	DOE-2.2	Yes	No	Must be far enough along to input HVAC	Yes (most popular)	Yes
<b>Green Building Studio / Vasari</b>	DOE-2.2	Yes	Yes	Yes	No	No
<b>Hourly Analysis Program (HAP)</b>	Transfer Function Method	Limited	No	No	Yes	No
<b>IES Virtual Environment</b>	Apache	Yes	Yes	Gaia + Toolkit Yes Pro requires input of HVAC	Yes	No
<b>OpenStudio</b>	EnergyPlus	Yes (similar to SketchUp)	Yes	Must be far enough along to input HVAC	Yes	Yes
<b>Sefaira Concept</b>	Sefaira	Yes	Yes	Yes	No	No
<b>Simergy</b>	EnergyPlus	Yes	Limited	Not yet	Yes	Yes
<b>TAS</b>	TAS	Yes	Yes	Yes	Yes	No
<b>TRACE® 700</b>	TRACE	No	Limited	Must be far enough along to input HVAC	Yes	No
<b>TRNSYS</b>	TRNSYS	Yes	No	No	No	No

# Example engineering calculations for BES program

## Outside Surface Heat Balance

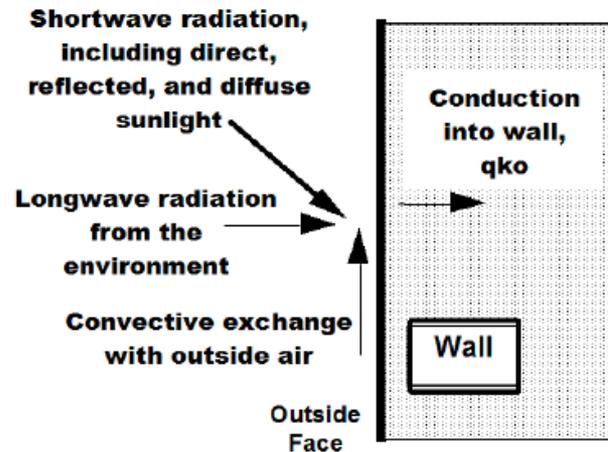


Figure 17. Outside Heat Balance Control Volume Diagram

The heat balance on the outside face is:

$$q''_{\alpha sol} + q''_{LWR} + q''_{conv} - q''_{ko} = 0 \quad (64)$$

where:

$q''_{\alpha sol}$  = Absorbed direct and diffuse solar (short wavelength) radiation heat flux.

$q''_{LWR}$  = Net long wavelength (thermal) radiation flux exchange with the air and surroundings.

$q''_{conv}$  = Convective flux exchange with outside air.

$q''_{ko}$  = Conduction heat flux ( $q/A$ ) into the wall.

- We know how to model all of these elements now
- Programs differ in how they select inputs, particularly heat transfer coefficients...

# Example engineering calculations for BES program

## **Simple Combined**

The simple algorithm uses surface roughness and local surface windspeed to calculate the exterior heat transfer coefficient (key:SimpleCombined). The basic equation used is:

$$h = D + EV_z + FV_z^2 \quad (82)$$

where

$h$  = heat transfer coefficient

$V_z$  = local wind speed calculated at the height above ground of the surface centroid

$D, E, F$  = material roughness coefficients

The roughness correlation is taken from Figure 1, Page 22.4, ASHRAE Handbook of Fundamentals (ASHRAE 1989). The roughness coefficients are shown in the following table:

Table 6. Roughness Coefficients D, E, and F.

<b>Roughness Index</b>	<b>D</b>	<b>E</b>	<b>F</b>	<b>Example Material</b>
1 (Very Rough)	11.58	5.894	0.0	Stucco
2 (Rough)	12.49	4.065	0.028	Brick
3 (Medium Rough)	10.79	4.192	0.0	Concrete
4 (Medium Smooth)	8.23	4.0	-0.057	Clear pine
5 (Smooth)	10.22	3.1	0.0	Smooth Plaster
6 (Very Smooth)	8.23	3.33	-0.036	Glass

# Example engineering calculations for BES program

## Inside Heat Balance

The heart of the heat balance method is the internal heat balance involving the inside faces of the zone surfaces. This heat balance is generally modeled with four coupled heat transfer components: 1) conduction through the building element, 2) convection to the air, 3) short wave radiation absorption and reflectance and 4) longwave radiant interchange. The incident short wave radiation is from the solar radiation entering the zone through windows and emittance from internal sources such as lights. The longwave radiation interchange includes the absorption and emittance of low temperature radiation sources, such as all other zone surfaces, equipment, and people.

The heat balance on the inside face can be written as follows:

$$q''_{LWX} + q''_{SW} + q''_{LWS} + q''_{ki} + q''_{sol} + q''_{conv} = 0 \quad (92)$$

where:

$q''_{LWX}$  = Net longwave radiant exchange flux between zone surfaces.

$q''_{SW}$  = Net short wave radiation flux to surface from lights.

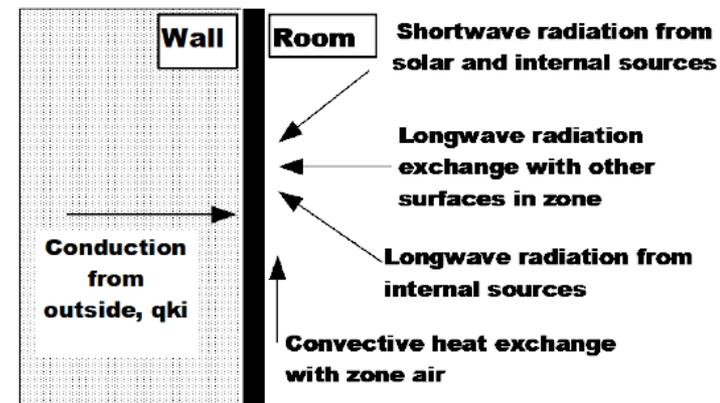
$q''_{LWS}$  = Longwave radiation flux from equipment in zone.

$q''_{ki}$  = Conduction flux through the wall.

$q''_{sol}$  = Transmitted solar radiation flux absorbed at surface.

$q''_{conv}$  = Convective heat flux to zone air.

Each of these heat balance components is introduced briefly below.



# Example engineering calculations for BES program

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- Choice of interior convection coefficients is complicated
  - Still a topic of ongoing research
  - Remember: Forced vs. laminar? Orientation? Cold or hot surface?
- Different equations for different surfaces
  - Simple buoyancy
    - Vertical walls, tilted surfaces, windows, etc.
  - In-floor heating or in-ceiling cooling
    - Vertical walls, heated floors, chilled ceilings, windows
  - Forced flow near diffusers
    - Ceiling diffusers, floor diffusers, near heated or cooled windows
  - Central mechanical fan circulation
    - Walls, horizontal flow
- EnergyPlus documentation has a great review of all of these

# Example engineering calculations for BES program

- These programs rely on the same equations we've been using

$$C_z \frac{dT_z}{dt} = \sum_{i=1}^{N_{sl}} \dot{Q}_i + \sum_{i=1}^{N_{surfaces}} h_i A_i (T_{si} - T_z) + \sum_{i=1}^{N_{zones}} \dot{m}_i C_p (T_{zi} - T_z) + \dot{m}_{inf} C_p (T_{\infty} - T_z) + \dot{Q}_{sys}$$

where:

$$\sum_{i=1}^{N_{sl}} \dot{Q}_i = \text{sum of the convective internal loads}$$

$$\sum_{i=1}^{N_{surfaces}} h_i A_i (T_{si} - T_z) = \text{convective heat transfer from the zone surfaces}$$

$$\dot{m}_{inf} C_p (T_{\infty} - T_z) = \text{heat transfer due to infiltration of outside air}$$

$$\sum_{i=1}^{N_{zones}} \dot{m}_i C_p (T_{zi} - T_z) = \text{heat transfer due to interzone air mixing}$$

$$\dot{Q}_{sys} = \text{air systems output}$$

$$C_z \frac{dT_z}{dt} = \text{energy stored in zone air}$$

$$C_z = \rho_{air} C_p C_T$$

$\rho_{air}$  = zone air density

$C_p$  = zone air specific heat

# Example engineering calculations for BES program

---

- Rearrange to solve for instantaneous HVAC system capacity:

$$-\dot{Q}_{sys} = \sum_{i=1}^{N_{sl}} \dot{Q}_i + \sum_{i=1}^{N_{surfaces}} h_i A_i (T_{si} - T_z) + \sum_{i=1}^{N_{zones}} \dot{m}_i C_p (T_{zi} - T_z) + \dot{m}_{inf} C_p (T_{\infty} - T_z)$$

- Instantaneous HVAC sensible capacity also equals:

$$\dot{Q}_{sys} = \dot{m}_{sys} C_p (T_{sup} - T_z)$$

- Once you have  $\dot{Q}_{sys}$  at each time step, you can calculate the energy required to deliver that rate of bulk heat transfer by knowing the efficiency/COP of your equipment

$$COP = \frac{\dot{Q}_{sys}}{P_{sys}} \longrightarrow P_{sys} = \frac{\dot{Q}_{sys}}{COP}$$

# Example engineering calculations for BES program

- Discretizing for time  $t$  versus time  $t - \delta t$ :

$$C_z \frac{T_z^t - T_z^{t-\delta t}}{dt} + T_z^t \left( \sum_{i=1}^{N_{surfaces}} h_i A_i + \sum_{i=1}^{N_{zones}} \dot{m}_i C_p + \dot{m}_{inf} C_p + \dot{m}_{sys} C_p \right) =$$

$$\sum_{i=1}^{N_{sl}} \dot{Q}_i^t + \dot{m}_{sys} C_p T_{supply}^t + \left( \sum_{i=1}^{N_{surfaces}} h_i A_i T_{si} + \sum_{i=1}^{N_{zones}} \dot{m}_i C_p T_{zi} + \dot{m}_{inf} C_p T_{\infty} \right)^{t-\delta t}$$

- If there is any **thermal mass** at any element, link to surface T:

$$C_p \rho \Delta X \frac{T_i^{j+1} - T_i^j}{\Delta t} = \frac{1}{2} \left[ \left( k_w \frac{(T_{i+1}^{j+1} - T_i^{j+1})}{\Delta X} + k_E \frac{(T_{i-1}^{j+1} - T_i^{j+1})}{\Delta X} \right) + \left( k_w \frac{(T_{i+1}^j - T_i^j)}{\Delta X} + k_E \frac{(T_{i-1}^j - T_i^j)}{\Delta X} \right) \right]$$

## Discretized conduction

BES programs vary in how they treat conduction and thermal mass

# Example engineering calculations for BES program

- Or use a lumped capacitance model (more detail next lecture):

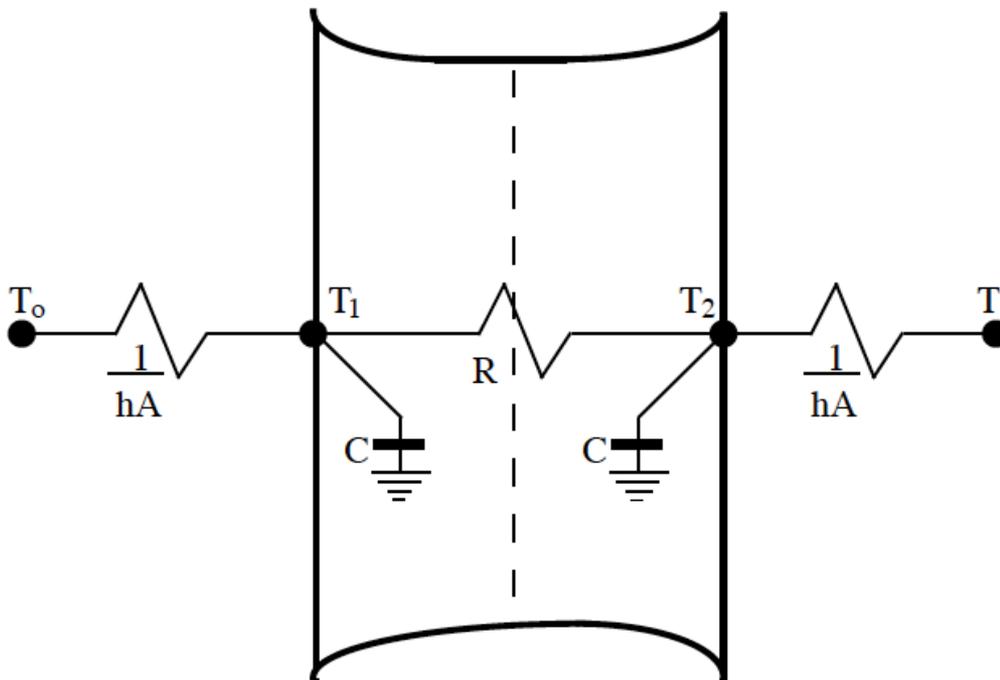


Figure 9. Two Node State Space Example.

$$C \frac{dT_1}{dt} = hA(T_o - T_1) + \frac{T_2 - T_1}{R}$$

$$C \frac{dT_2}{dt} = hA(T_i - T_2) + \frac{T_1 - T_2}{R}$$

where:

$$R = \frac{\ell}{kA},$$

$$C = \frac{\rho c_p \ell A}{2}$$

**BES programs vary in how they treat conduction and thermal mass**

# Lumped capacitance model for conduction

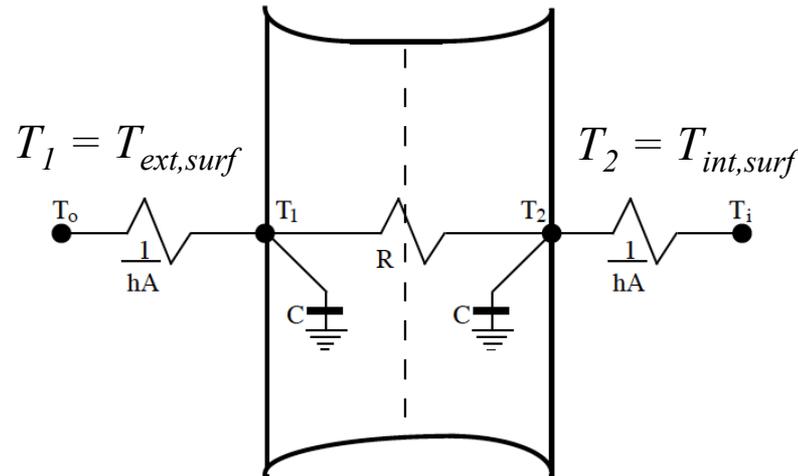


Figure 9. Two Node State Space Example.

## Steady state surface energy balance...

$$\alpha I_{solar} + \varepsilon_1 \sigma F_{sky} (T_{sky}^4 - T_1^4) + \varepsilon_1 \sigma F_{air} (T_{air}^4 - T_1^4) + \varepsilon_1 \sigma F_{ground} (T_{ground}^4 - T_1^4) + h_{conv} (T_{air} - T_1) - U(T_1 - T_2) = 0$$

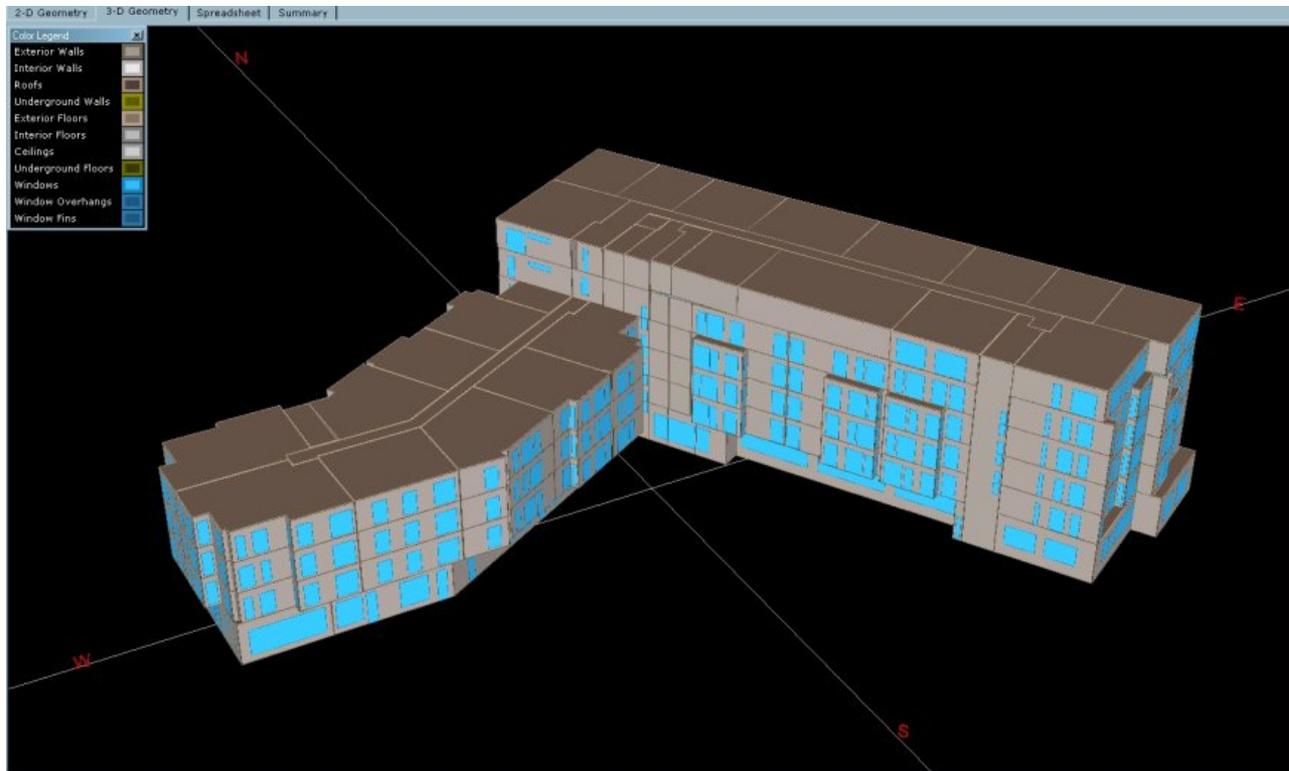
...becomes a **time-varying** surface energy balance:

$$\alpha I_{solar} + \varepsilon_1 \sigma F_{sky} (T_{sky}^4 - T_1^4) + \varepsilon_1 \sigma F_{air} (T_{air}^4 - T_1^4) + \varepsilon_1 \sigma F_{ground} (T_{ground}^4 - T_1^4) + h_{conv} (T_{air} - T_1) - U(T_1 - T_2) = \frac{\rho C_p L}{\Delta t} \frac{1}{2} (T_1^n - T_1^{n-1})$$

**BES programs vary in how they treat conduction and thermal mass**

# Demonstration of eQUEST

- eQUEST demonstration
  - Launch program



<http://www.buildingenergyexperts.com/wp-content/uploads/2010/08/Equest.jpg>

# HW #4

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- HW #4 involves modeling a commercial building in eQUEST
  - And making changes to the enclosure
  - Assigned today, due April 12
- <http://www.doe2.com/equest/>
- Current version: 3.65 (released March 2014)