CAE 463/524 Building Enclosure Design

Spring 2015

Lecture 10: March 31, 2015

Finish windows and daylighting

Energy simulation and enclosure design

Built Environment Research





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Last time

- Finished air leakage
- Windows and daylighting
 - U values
 - SHGC
 - Solar transmittance
 - Visible transmittance
- Take-home exam given
 - Due today
- Discussed final project expectations

Final project topic selection

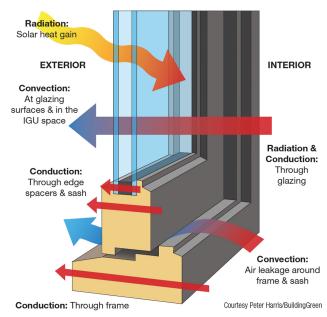
• Email me your topics by Friday April 3, 2015

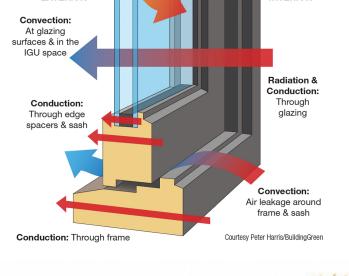
Name	Project topic	
Behrens, Maria C.		
Geoghegan, Thomas	Double skin facade	
Irazabal, Carlos H.	Cool roofs	
Jung, Yun Joon		
Lis, Kimberly A.		
Ng, Yin Ling		
Theisen, Whitney A.		
Carrillo Garcia, Jose		
Dorn, Lawrence E.	Electrochromic glass	
Erukulla, Dilip Kumar		
Liang, Jinzhe	Double skin facade	
Mullin, Elizabeth M.	Straw bale construction (or earthen materials)	
Tuz, Oleg	BioSkin evaporative panel?	
Chandler, Julie A.		
Chung, Allan		
Fortune, Roger G.	Brooklyn Trust building	
Gadani, Dhaval S.		
Jarosz, Michelle M.		
Linn, Rebecca C.		

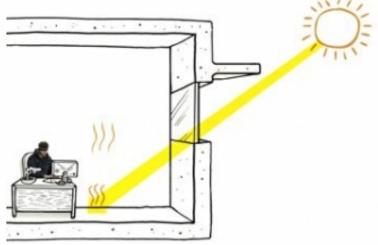
Today's objectives

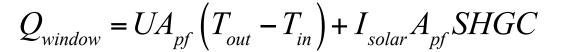
- Finish windows and daylighting
- Introduce energy simulation in building enclosure design

Review of window heat transfer











World's Best Window Co.

Millennium 2000+ Vinyl-Clad Wood Frame Double Glazing • Argon Fill • Low E Product Type: Vertical Slider

ENERGY PERFORMANCE RATINGS

U-Factor (U.S./I-P)

Solar Heat Gain Coefficient

ADDITIONAL PERFORMANCE RATINGS

Visible Transmittance

Air Leakage (U.S./I-P)

Manufacturer stipulates that these ratings conform to applicable NFRC procedures for determining whole product performance. NFRC ratings are determined for a fixed set of environmental conditions and a specific product size. Consult manufacturer's literature for other product performance information. www.nfrc.org

Some methods of achieving daylighting efficiently

- Skylights
- Light pipes and fiber optic daylighting systems
- Light shelves
- All need to be used with dimming ballasts or other advanced lighting controls to achieve savings

Skylights

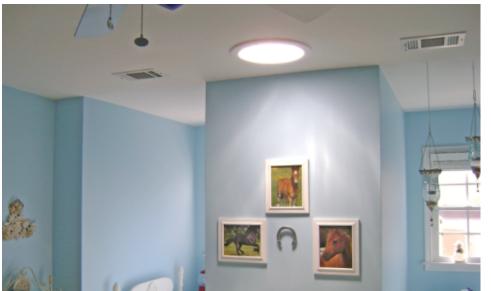
Typically limited to low-rise structures





Solar tubes





Daylighting Technology



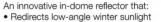
Capture

Raybender® 3000 Technology

A patented daylight-capturing dome lens that:

- Redirects low-angle sunlight for maximum light capture
- Rejects overpowering midday summer sunlight
- Provides consistent daylighting throughout the day

LightTracker™ Reflector



- for maximum light capture

 Increases light input for greater light
- Delivers unsurpassed year-round performance

Transfer 4

Spectralight® Infinity Tubing

Tubing made of the world's most reflective material that:

- Delivers 99.7% * specular reflectivity for maximum sunlight transfer
- Provides the purest color rendition possible so colors are truer, brighter
- Allows for run lengths over 30 feet to deliver sunlight to lower floors





Stylish Daylight Delivery

Form and function combine for optimal daylight diffusion with:

- Solatube Decorative Fixtures
- Warming and Softening Effect Lenses
- Ventilation, dimmer and nighttime lighting options

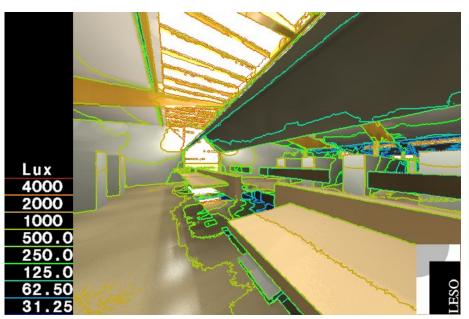
* Specular reflectance greater than 99% with wavelength specific reflectance up to 99.7% for the visible spectrum.

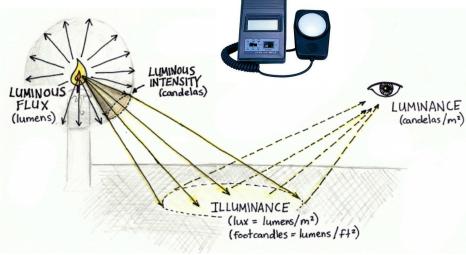
Light shelves





Combining software and hardware for investigating daylighting

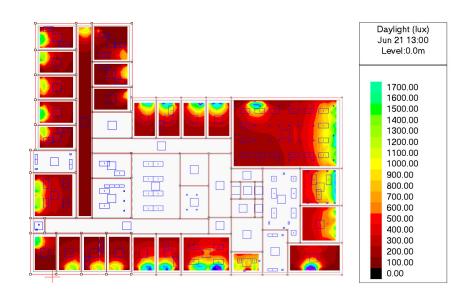




Hardware: Light sensors

Software: Radiance

http://floyd.lbl.gov/deskrad/download.htm



Designing with glass

- There are many methods used to compensate for its poor thermal properties
 - Insulated windows with double & triple glazing
 - Low E coatings
 - Low conductivity gas fills
 - Tinting
 - Reflective coatings
 - Curtains and shutters
 - Window sizing & orientation on the building
 - Shading or overhangs

New technologies are pushing the boundaries on thermal performance of fenestration

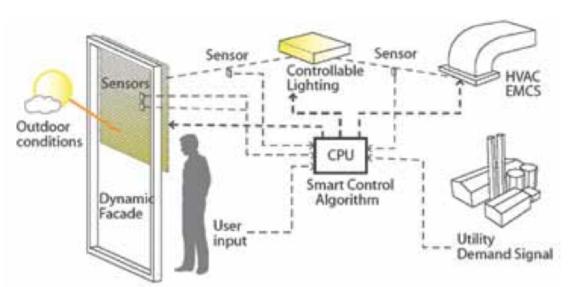
- Building integrated photovoltaics (BIPV)
 - Photovoltaic (PV) cells provide shading and generate electricity
- Vacuum insulated windows
 - Removing air eliminates conduction and convection
 - Effective but expensive to manufacturer
- Aerogel
 - Transparent silica gel with a very low density
 - Very high insulating properties
 - Very good sound absorption properties

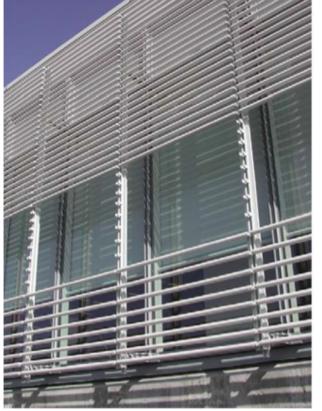


Designing with glass for daylighting: Controls



Systems need to be used with dimming ballasts or other advanced lighting controls



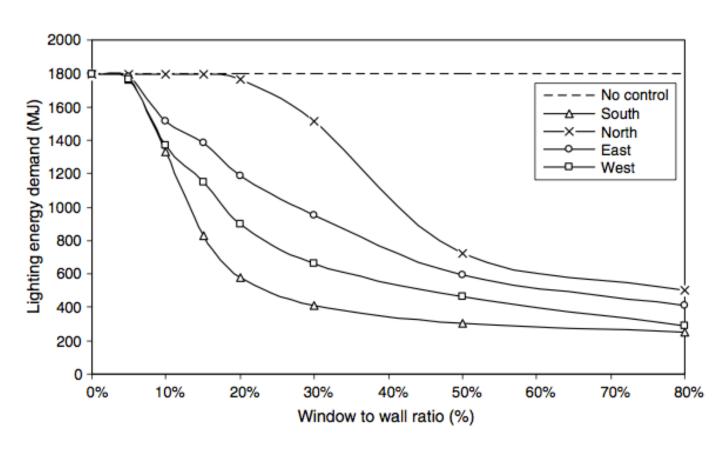


Lee and Selkowitz **2006** Energy and Buildings

Selkowitz 2011 Journal of Building Enclosure Design

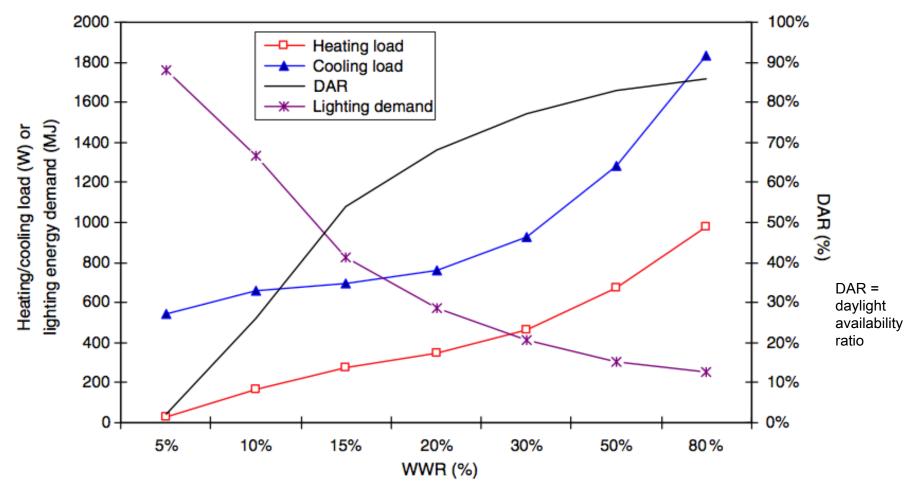
Energy impacts of glazing

Increased daylighting can save **lighting energy** depending on WWR and orientation:



Energy impacts of glazing

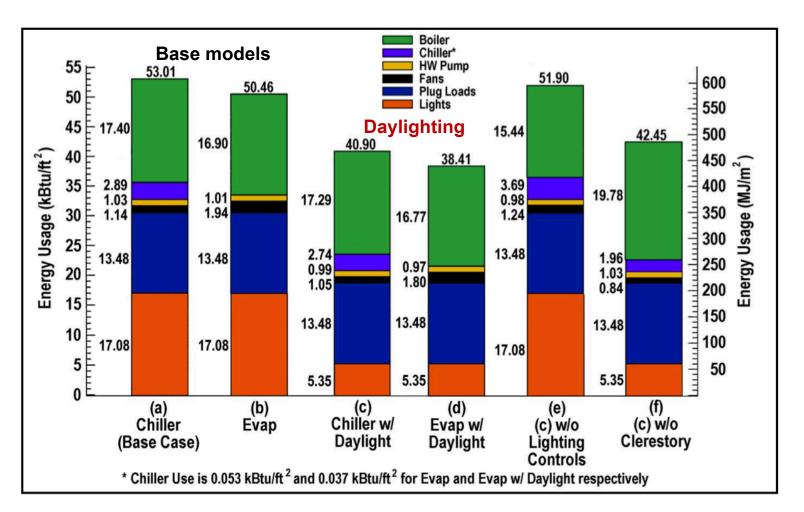
But daylighting also affects heating and cooling loads...



...so how do we find the right balance?

Energy impacts of glazing: Energy modeling

Example project: Energy modeling w/ daylighting in Colorado:



What about in a warmer climate?

WHOLE BUILDING ENERGY SIMULATION

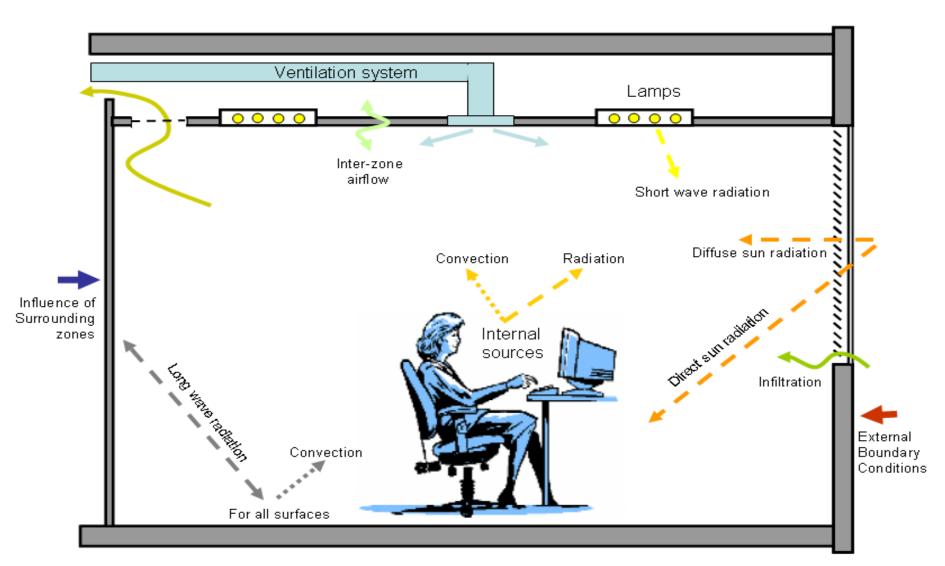
Energy simulation and enclosure design

- In Building Science we discussed using sizing programs to determine peak hourly loads during heating and cooling seasons and size equipment
 - Heating loads: easy (U*A*dT)
 - Cooling loads: more complex (radiation) CLTD, RTS, HB, etc.
 - You can influence loads and size of equipment early in the design process by specifying certain envelope characteristics
- More advanced: Whole building energy simulation programs are used to predict annual energy consumed by a building
 - Outcomes: annual BTUs, MJ, kWh, \$, associated pollutant emissions
 - Typically normalized per floor area (e.g., MBTU/ft²)
 - You can influence annual energy consumption (and costs) early in the design process, again by specifying certain envelope characteristics

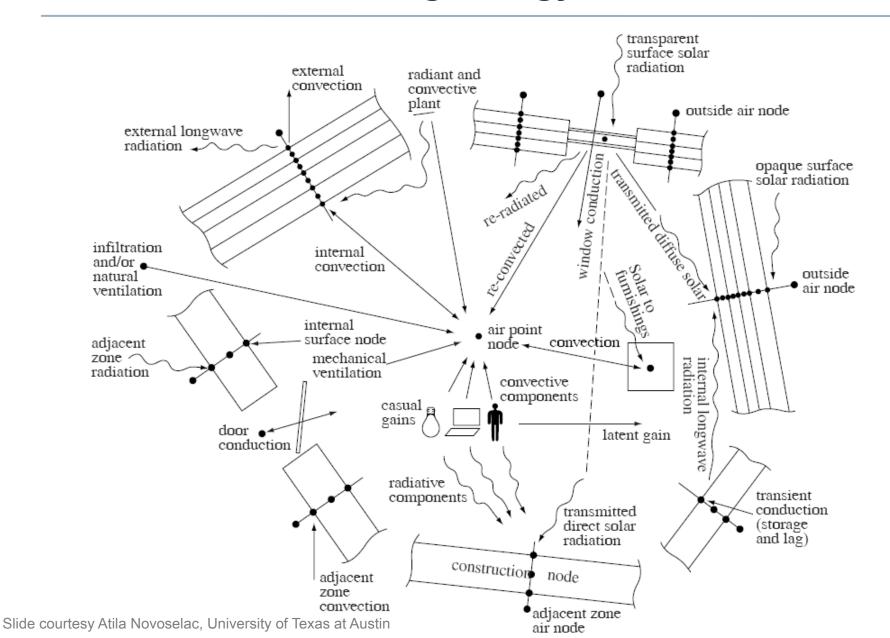
Whole building energy simulation

- We've covered individual surface energy balances before
 - Surfaces are all connected
- We can build a system of equations linking energy balances at a series of "nodes"
 - Each node has an equation accounting for all modes of heat transfer
- Whole building energy simulation
 - Involves linking the nodes and predicting hourly indoor air temperatures (or HVAC loads) as the primary unknown
 - Include HVAC system capacity and efficiency to get HVAC energy
 - Also includes interior heat gains
 - People, lights, equipment, etc.
 - Direct power draw + indirect heat gains

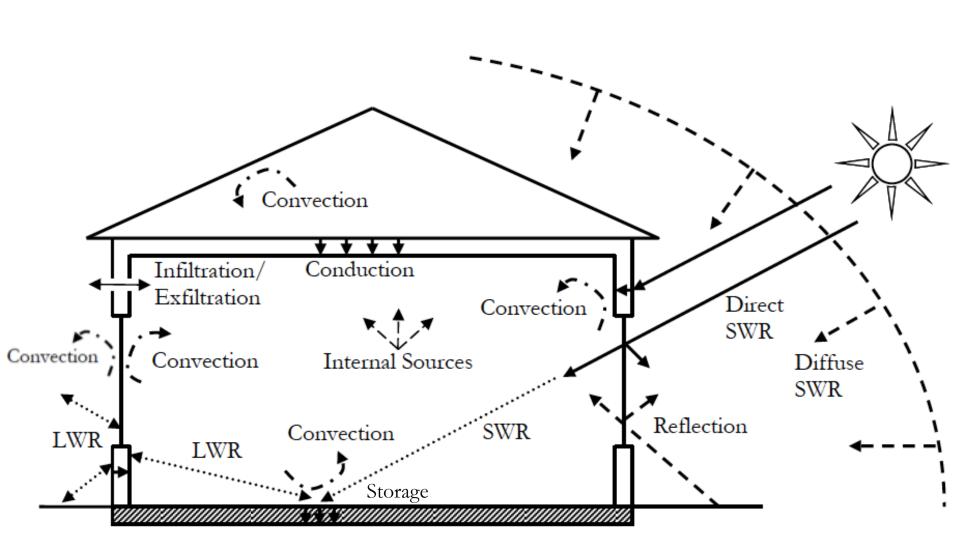
Whole building energy simulation



Whole building energy simulation



Building enclosures and heat transfer, visualized



Heat transfer in building science: Summary

Conduction

$$q = \frac{k}{L} \left(T_{surf,1} - T_{surf,2} \right)$$

$$\frac{k}{L} = U = \frac{1}{R}$$

$$R_{total} = \frac{1}{U}$$

$$R_{total} = R_1 + R_2 + R_3 + \dots$$

For thermal bridges and combined elements:

$$U_{total} = \frac{A_1}{A_{total}} U_1 + \frac{A_2}{A_{total}} U_2 + \dots$$

Convection

$$q_{conv} = h_{conv} \left(T_{fluid} - T_{surf} \right)$$

$$R_{conv} = \frac{1}{h_{conv}}$$

Radiation

Long-wave

$$R_{conv} = \frac{1}{h_{conv}}$$

$$q_{1 \to 2} = \frac{\sigma \left(T_{surf,1}^4 - T_{surf,2}^4\right)}{\frac{1 - \varepsilon_1}{\varepsilon_1} + \frac{A_1}{A_2} \frac{1 - \varepsilon_2}{\varepsilon_2} + \frac{1}{F_{12}}}$$

$$q_{rad,1\rightarrow 2} = h_{rad} \left(T_{surf,1} - T_{surf,2} \right)$$

$$h_{rad} = \frac{4\sigma T_{avg}^3}{\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1} \qquad R_{rad} = \frac{1}{h_{rad}}$$

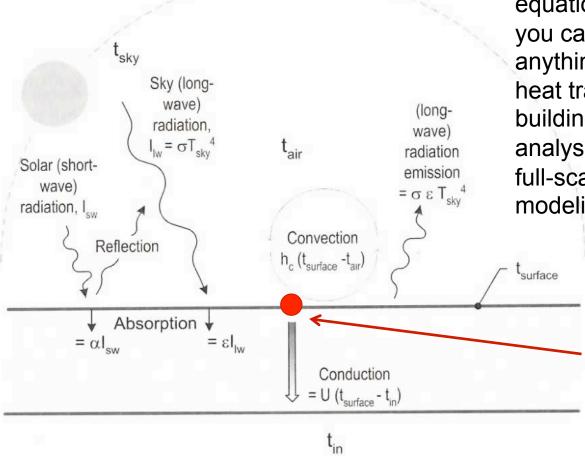
Or more simply: $q_{1\rightarrow 2} = \varepsilon_{surf} \sigma F_{12} \left(T_{surf,1}^4 - T_{surf,2}^4 \right)$

Solar radiation: $q_{solar} = \alpha I_{solar}$ (opaque surface)

Transmitted solar radiation: $q_{solar} = \tau I_{solar}$ (transparent surface)

Surface energy balance: Bringing all the modes together

Exterior surface example: Roof



Once you have this equation described, you can do just about anything regarding heat transfer in building enclosure analysis, leading into full-scale energy modeling

Steady-state energy balance at this exterior surface: What enters must also leave (no storage)

$$q_{solar} + q_{longwaveradiation} + q_{convection} - q_{conduction} = 0$$

Surface energy balance: Bringing all the modes together

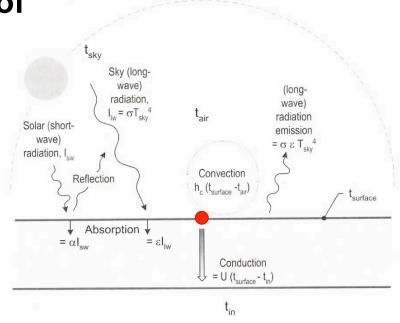
Exterior surface example: Roof

$$\sum q = 0$$

We can use this equation to estimate indoor and outdoor surface temperatures

At steady state, net energy balance is zero

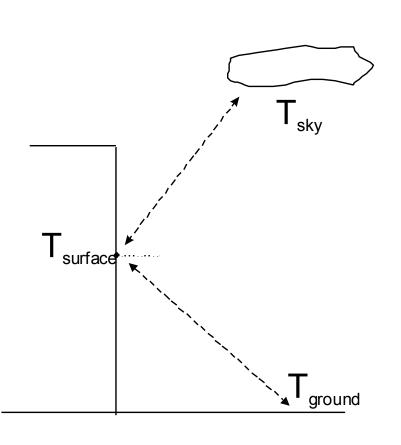
Because of T⁴ term, often requires iteration



Solar gain	$lpha I_{solar}$	$q_{\mathit{sw,solar}}$
Surface-sky radiation	$+ \varepsilon_{surface} \sigma F_{sky} (T_{sky}^4 - T_{surface}^4)$	$+q_{lw,surface-sky}$
Convection on external wall	$+h_{conv}(T_{air}-T_{surface})$	$+q_{convection}$
Conduction through wall	$-U(T_{surface} - T_{surface,interior}) = 0$	$-q_{conduction} = 0$

Typical view factors, F_{1-2}

Some typical view factors from surfaces to ground or sky



View ("shape") factors for:

Vertical surfaces:

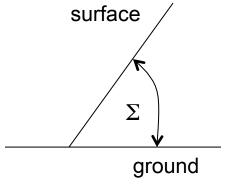
- To sky (F_{surface-sky}) 0.5
- To ground (F_{surface-ground}) 0.5

Horizontal surfaces:

- To sky (F_{surface-sky})
- To ground (F_{surface-ground}) 0
- 3) Tilted surfaces
- To sky $(1+\cos\Sigma)/2$
- To ground $(1-\cos\Sigma)/2$

Typically assume:

$$T_{ground} = T_{air}$$

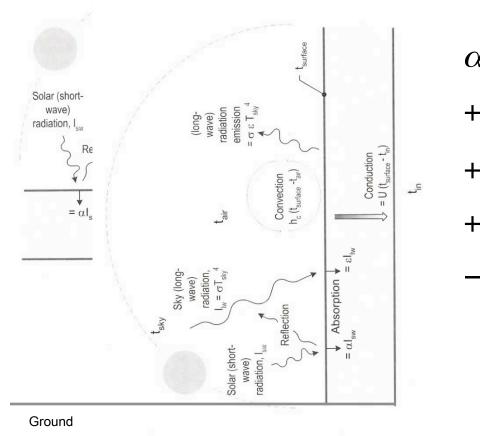


^{*}Note that other surrounding buildings complicate view factors, but their net temperature differences probably aren't that different so long-wave radiation can be negligible

Surface energy balance: Bringing all the modes together

Similarly, for a vertical surface:

$$q_{solar} + q_{lwr} + q_{conv} - q_{cond} = 0$$

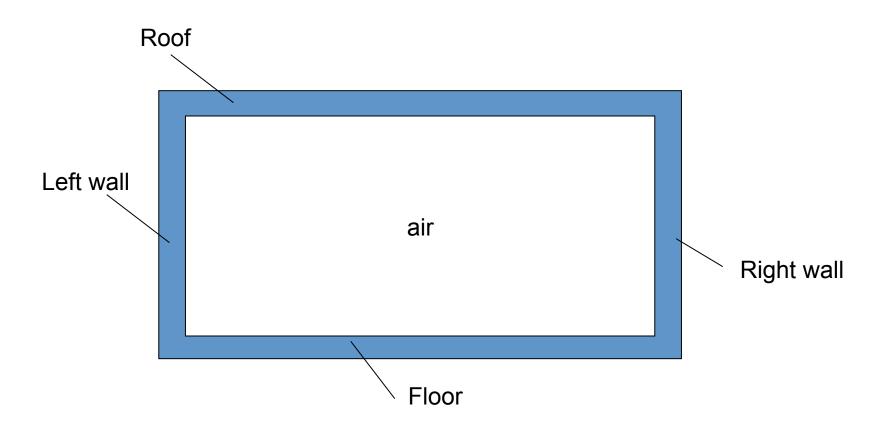


$$\begin{split} &\alpha I_{solar} \\ &+ \varepsilon_{surface} \sigma F_{sky} (T_{sky}^4 - T_{surface}^4) \\ &+ \varepsilon_{surface} \sigma F_{ground} (T_{ground}^4 - T_{surface}^4) \\ &+ h_{conv} (T_{air} - T_{surface}) \\ &- U (T_{surface} - T_{surface,interior}) = 0 \end{split}$$

Whole building energy modeling steps

- Define the domain
- Analyze the most important phenomena and define the most important elements
- Discretize the elements and define connections
- Write the energy and mass balance equations
 - Include any assumptions for indoor sources
- Solve the equations
 - Use numeric methods or discrete solutions
 - Time-varying analysis over an entire year
- Present the results
 - kWh electricity; BTU or MJ of other fuels
 - Hourly, daily, monthly, yearly

Simplest 'box' model



Elements are connected by:

- 1) Convection air node
- 2) Radiation surface nodes

Bringing all modes (and nodes) together

- For an example room like this, you would setup a system of equations where the temperature at each node (either a surface or within a material) is unknown
 - 12 material nodes + 1 indoor air node

Heat Xfer @ external surfaces: Radiation and convection

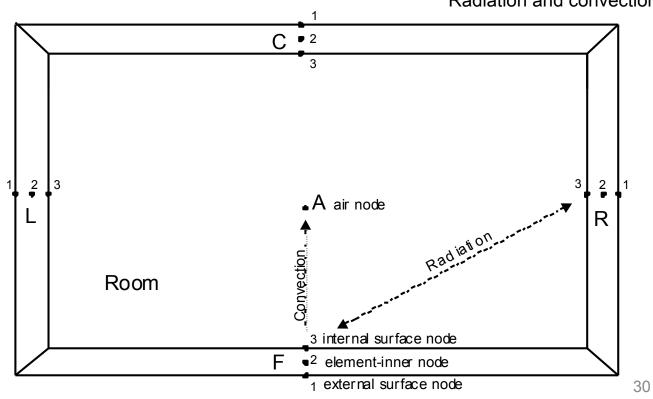
At surface nodes:

$$\sum q = 0$$

At nodes inside materials:

$$mc_p \frac{dT}{dt} = \sum q_{at \ boundaries}$$

Based on density and heat capacity of material



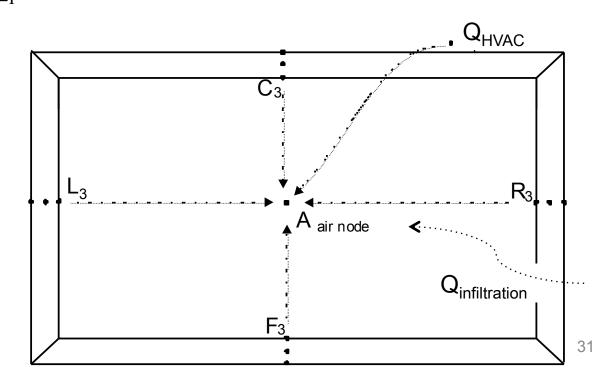
Unsteady energy balance for air node

- To get the impact on indoor air temperature (and close the system of equations)
 - Write an energy balance on the indoor air node
 - Air impacted directly only by convection (bulk and surface)

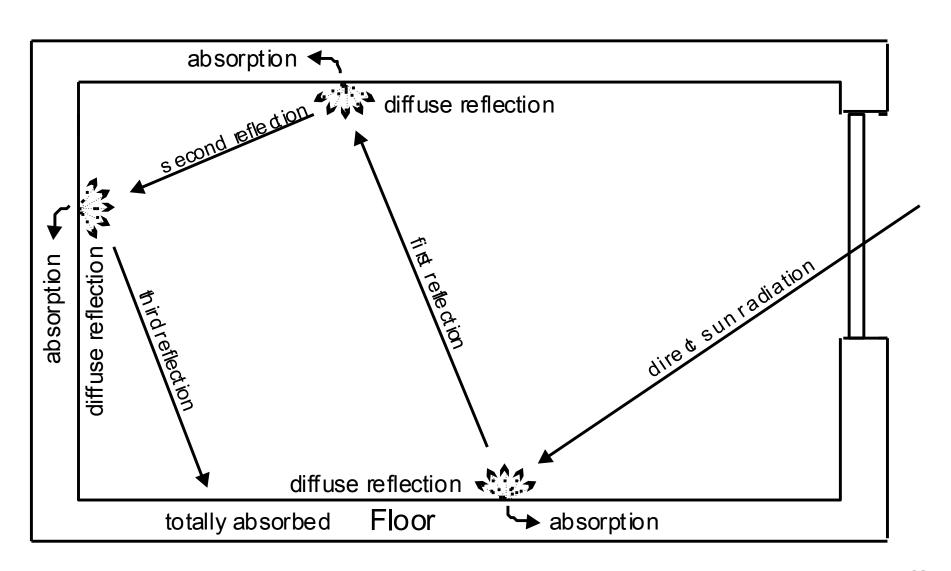
$$(V_{room}\rho_{air}c_{p,air})\frac{dT_{air,in}}{dt} = \sum_{i=1}^{n} h_i A_i \left(T_{i,surf} - T_{air,in}\right) + \dot{m}c_p \left(T_{out} - T_{air,in}\right) + Q_{HVAC}$$

In plain English:

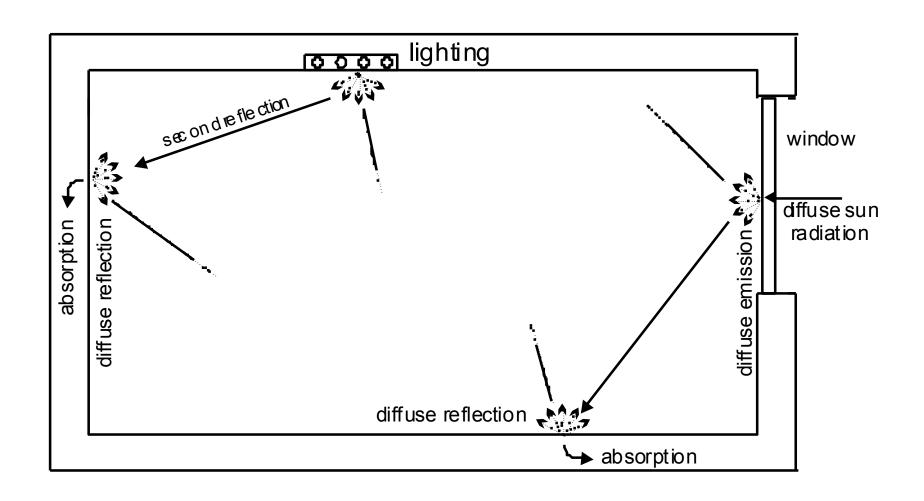
The change in indoor air temperature is equal to the sum of convection from each interior surface plus outdoor air delivery (by infiltration or dedicated outdoor air supply), plus the bulk convective heat transfer delivered by the HVAC system



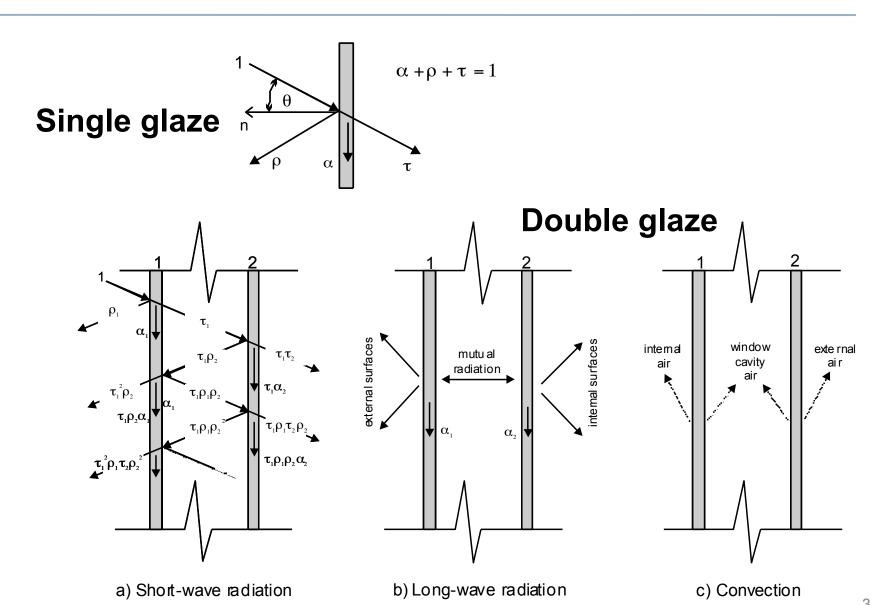
Adding a window: Direct solar radiation



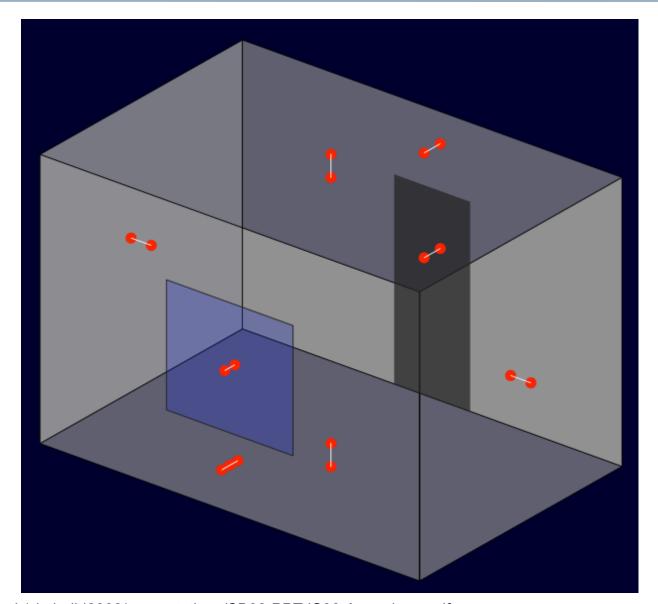
Adding a window: Diffuse solar radiation



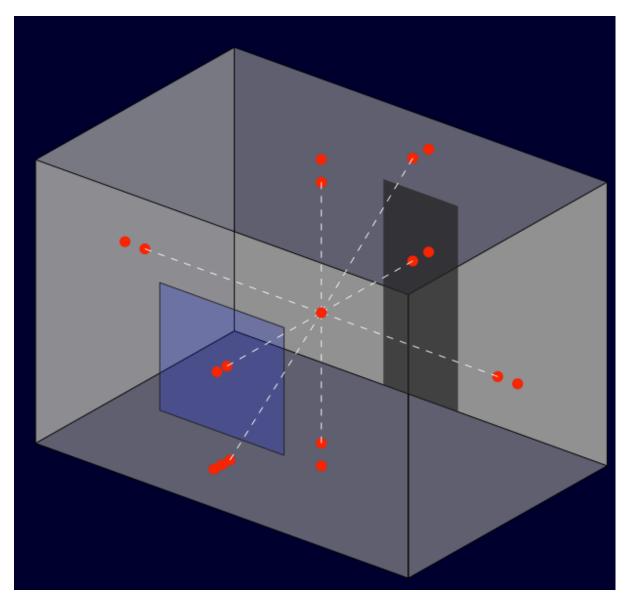
Heat transfer in windows



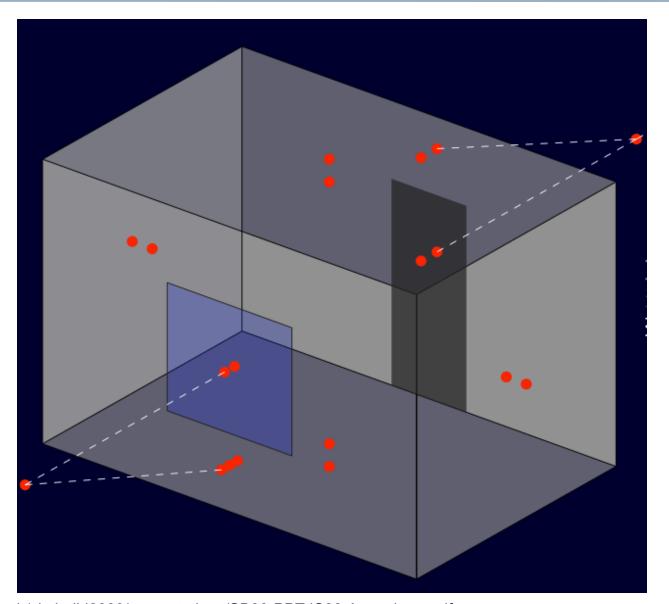
Simplest 'box' model: Conduction elements



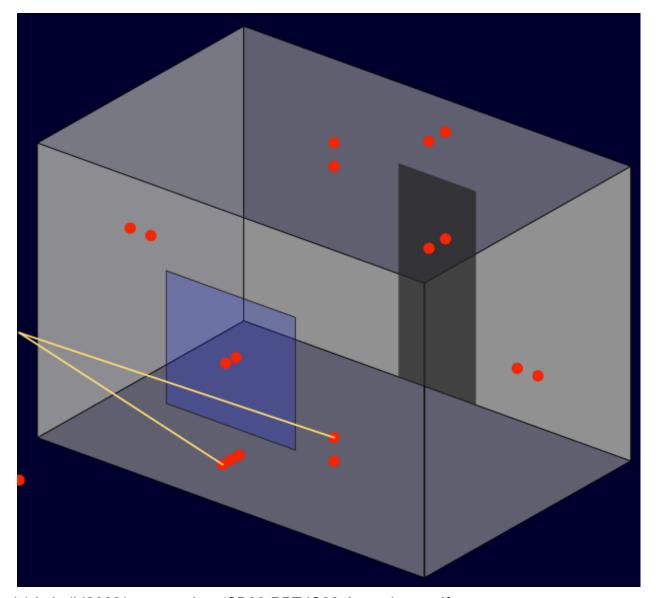
Simplest 'box' model: Interior convection elements



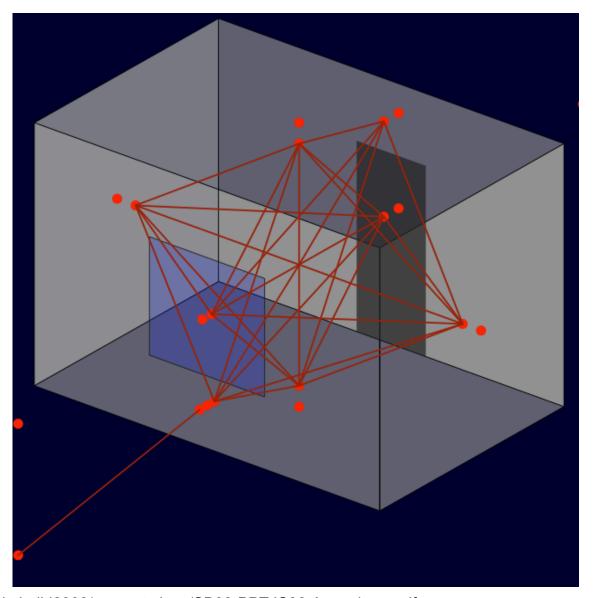
Simplest 'box' model: Exterior convection elements



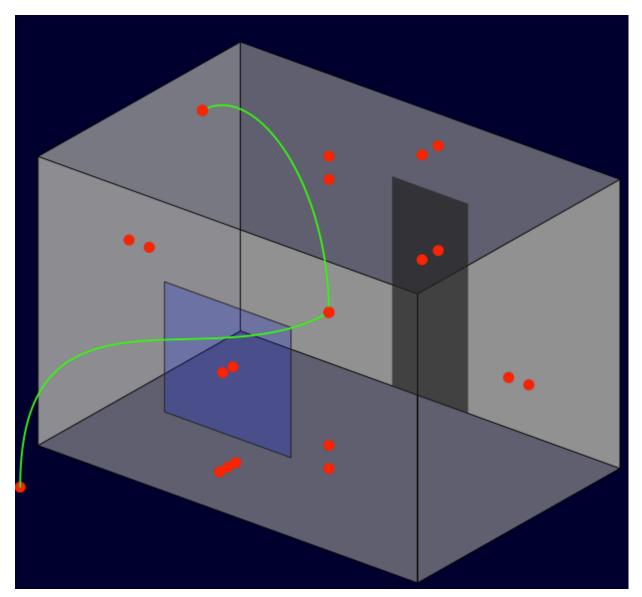
Simplest 'box' model: Solar (direct + diffuse)



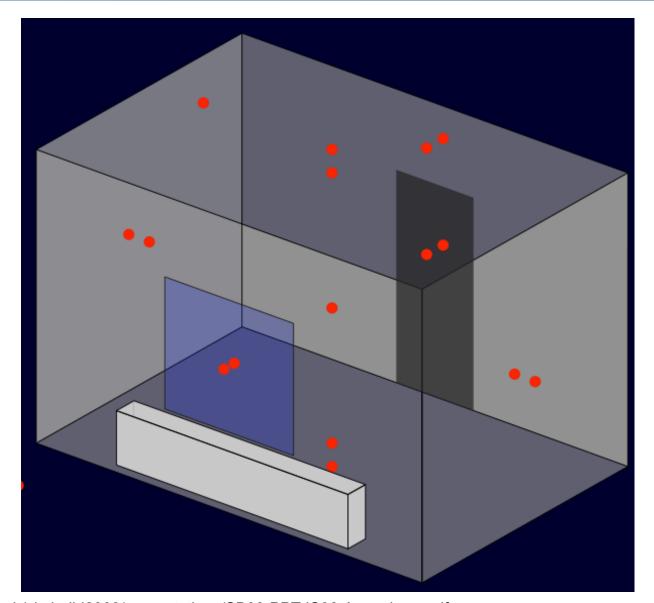
Simplest 'box' model: Long wave radiation elements



Simplest 'box' model: Ventilation/infiltration elements



Simplest 'box' model: Internal mass (e.g., furniture)

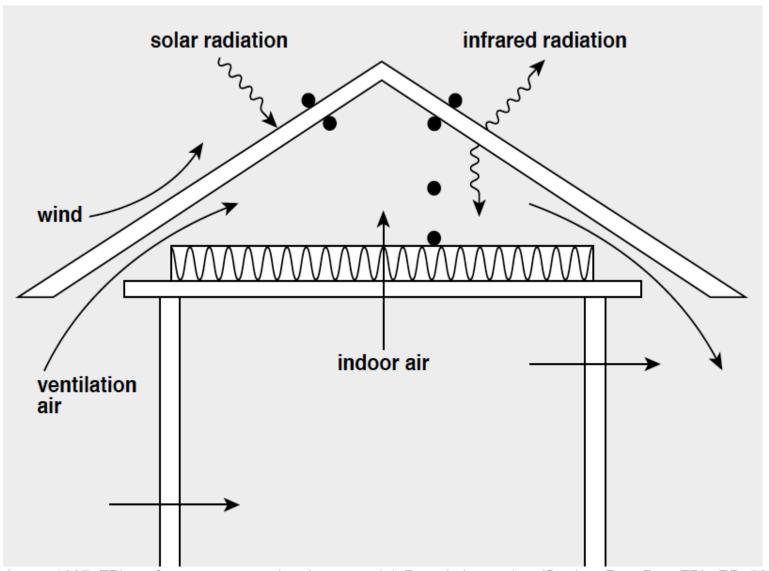


Important input parameters for energy simulation

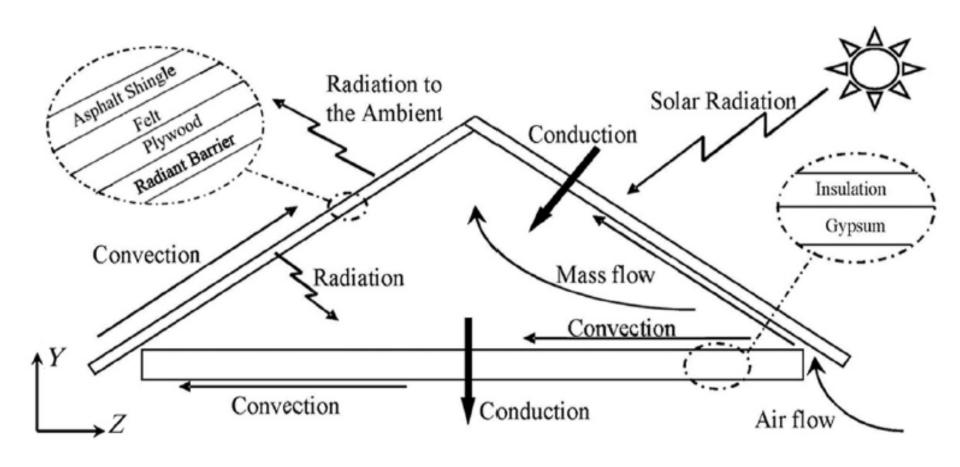
- Conduction (and storage) solution method
 - Finite difference (explicit, implicit)
 - Response functions techniques
- Time steps
 - Too short and calculations take forever
 - Too long and solutions diverge
- Meteorological data (TMY, AMY)
 - Temperature, wind speed, solar radiation, cloud cover
- Radiation and convection models
 - Internal and external
- Windows and shading
- Air infiltration models
- Conduction to the ground
- HVAC system and control models

BUILDING ENERGY SIMULATION EXAMPLE: ATTIC HEAT TRANSFER

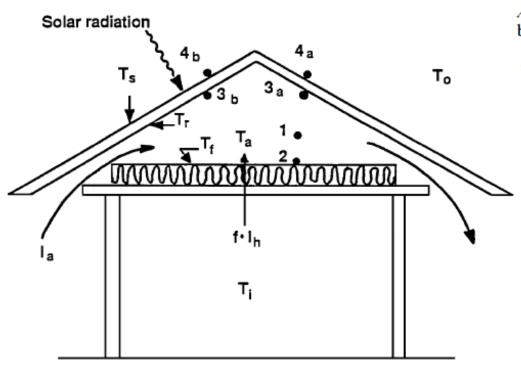
Attic simulation example



TenWolde, Anton. 1997. FPL roof temperature and moisture model: Description and verification. Res. Pap. FPL–RP–561. Madison, WI: U.S. Department of Agriculture, Forest Service, Forest Products Laboratory. 48 p.



Asadi et al., 2012. Performance evaluation of an attic radiant barrier system using three dimensional transient finite element method. *Journal of Building Physics*.



Nodes for heat balance

 T_a , T_i , T_f , Temperatures of attic, indoor air, attic floor T_o , T_r , T_s outside air, underside of roof, surface of roof

f Fraction of air entering attic

Ia, Ih Ventilation rates for attic and house, vol. changes/hour

Attic Air—The heat balance for the attic air (node 1) is given by

$$A_{c}h_{f}(T_{f}-T_{a})+fI_{h}V_{h}\rho C_{p}(T_{i}-T_{a})$$

$$=\frac{A_{r}}{2}h_{r,l}(T_{a}-T_{r,l})+\frac{A_{r}}{2}h_{r,2}(T_{a}-T_{r,2})+\frac{A_{es}}{R_{es}}(T_{a}-T_{o})$$

$$+I_{a}\rho C_{p}V_{a}(T_{a}-T_{o})$$
(2)

where

 $A_{\rm c}, A_{\rm r},$

 A_{es} = surface areas of ceiling, total roof area, and combined area of soffit and end walls (ft²)

 C_p = specific heat of air (Btu/lb·°F)

f = fraction of house exfiltration that transfers

into attic

 h_f , $h_{r,n}$ = convective heat transfer coefficients at attic floor and underside of roof (surface n), respectively (Btu/h·ft²·°F)

= house exfiltration rate (h⁻¹)

 I_a = attic ventilation rate, i.e., outdoor air

entering attic (h⁻¹)

 $R_{e,s}$ = average thermal resistance of end walls and eaves (h·ft²·°F/Btu)

 $T_{\rm a}$ = attic air temperature (°R)

 $T_{\rm f}$ = temperature of attic floor surface (°R)

 T_i = indoor air temperature (°R) T_o = outdoor air temperature (°R)

 $T_{r,1}$ = temperature of roof sheathing underside a (°R)

 $T_{r,2}$ = temperature of roof sheathing underside b (°R)

 V_a = volume of attic space (ft³) V_h = volume of house (ft³)

 ρ = density of air (lb/ft³)

Attic Floor—The heat balance for the attic floor (node 2) is

$$\frac{T_{\rm i} - T_{\rm f}}{R_{\rm c}} = h_{\rm f} (T_{\rm f} - T_{\rm a}) + \frac{F_{\rm l}}{2} (T_{\rm f} - T_{\rm r, l}) + \frac{F_{\rm 2}}{2} (T_{\rm f} - T_{\rm r, 2}) \tag{3}$$

where

 R_c = thermal resistance of attic floor (ceiling) (h·ft²·°F/Btu)

 F_1 , F_2 = radiative heat transfer coefficients between attic floor and undersides of roof (Btu/h·ft²·°F), with the following definition:

$$F_n = \frac{\sigma}{(1/\varepsilon_f) + (1/\varepsilon_r) - 1} (T_f^2 + T_{r,n}^2) (T_f + T_{r,n}) \quad n = 1, 2$$

where

 $\varepsilon_{\rm f}$ = emissivity of attic floor surface (assumed to be 0.9)

 $\varepsilon_{\rm r}$ = emissivity of roof sheathing surface (underside, assumed to be 0.9)

 σ = Stefan–Boltzman constant (Btu/h·ft²·°R⁴)

Sheathing—The heat balance at the underside of sheathing (nodes 3a and 3b) is

$$\frac{T_{r,n} - T_{s,n}}{R_r} = h_r (T_a - T_{r,n})
+ \frac{A_c}{A_r} F_n (T_f - T_{r,n}) + \frac{2}{A_r} L_h W_{r,n} \qquad n = 1,2$$
(5)

where

 L_h = latent heat of vaporization (1,050 Btu/lb)

 $R_{\rm r}$ = thermal resistance of roof (h·ft²·°F/Btu)

 $T_{s,n}$ = temperature of outside roof surface (°R)

 $W_{r,n}$ = rate of moisture adsorption into sheathing (lb/h)

The heat balance at the top surface of sheathing (nodes 4a and 4b) is

$$\frac{T_{s,n} - T_{r,n}}{R_r} = \alpha I_n + (h_{o,n} + h_{IR})(T_o - T_{s,n}) - L_{IR} \qquad n = 1,2$$
 (6)

where

```
h_{IR}, L_{IR} = adjustments for infrared radiation exchange with sky (see Eqs. (7), (8), and (9))
```

 $h_{o,n}$ = convective heat transfer coefficient at exterior roof surface n (Btu/h·ft²·°F)

I_n = total solar radiation incident on roof surface (Btu/h·ft²)

 α = solar absorptance

$$h_{\rm IR} = 4\varepsilon_{\rm s}\sigma T_{\rm o}^3 \tag{7}$$

$$L_{\rm IR} = \varepsilon_{\rm s} \sigma T_{\rm o}^4 (1 - \varepsilon_{\rm IR}) \tag{8}$$

where

 $\varepsilon_{\rm s}$ = emissivity of roof shingles (assumed to be 0.9)

 ε_{IR} = sky emissivity with clouds

The sky emissivity is calculated with equations from Martin and Berdahl (1984). The emissivity for a clear sky is

$$\epsilon_0 = 0.711 + 0.56 \frac{T_d}{100} + 0.73 \left(\frac{T_d}{100}\right)^2 + 0.013 \cos\left(\frac{2\pi t}{24}\right)$$
(9)

where

 ε_0 = emissivity of clear sky

 $T_{\rm d}$ = outdoor dew point temperature (°C)

t = time(h)

and the emissivity of the sky with clouds is

$$\varepsilon_{\rm IR} = \varepsilon_0 + 0.784C(1 - \varepsilon_0) \tag{10}$$

where C = total cloud cover as recorded by National Climatic Center (Asheville, NC). Values of C range from 0 to 10.

Sheathing surface temperature: Measured vs. modeled

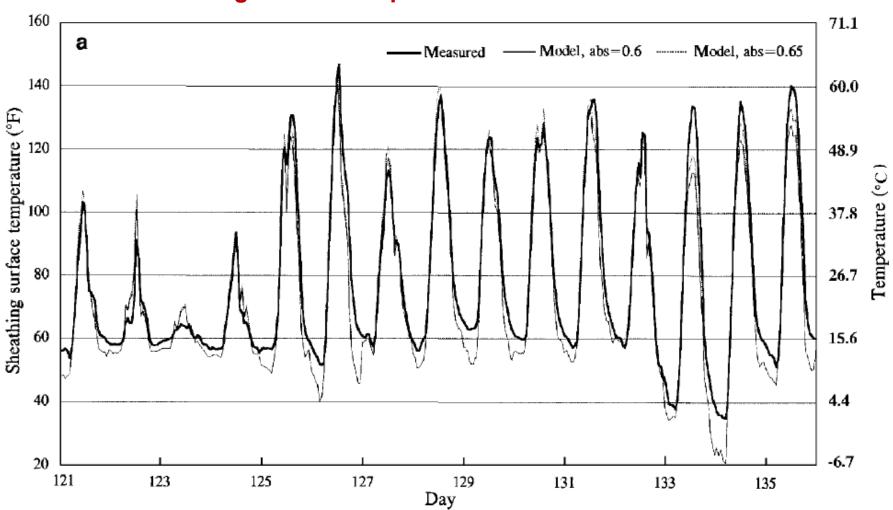


Figure 4—Exterior sheathing surface temperature, bay 2, May 1–15, 1993.

Attic air temperature: Measured vs. modeled

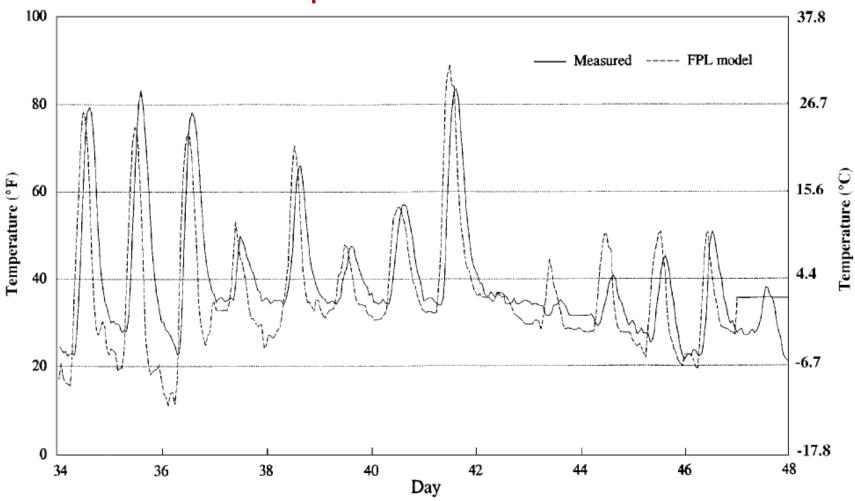


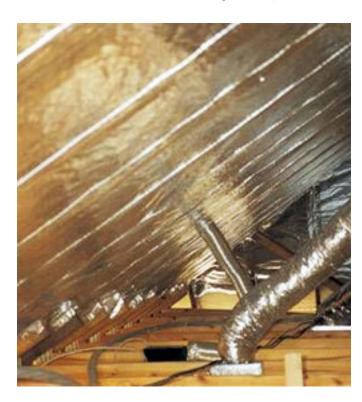
Figure 5—Attic air temperature, bay 2, February 3–16, 1993; absorptance = 0.65.

Attic heat transfer summary

- Attic temperature is important
 - HVAC equipment is often located in attics
 - Impacts conduction across ceiling into interior space
- Ways to reduce attic temperatures?
 - Increase convective heat transfer
 - Attic ventilation
 - Reduce exterior roof surface temperature
 - 'Cool roof' low absorptivity materials on the exterior
 - Reduce attic floor surface and underside sheathing temperatures
 - Low-emissivity materials inside attic
 - Attic floor or underside of sheathing
 - Radiant barriers

Radiant barriers

- Radiant barriers typically have LW emissivity less than ~0.1
 - Approximately 90% of materials have emissivity of 0.9
- Inhibits heat flow through radiation only
 - Doesn't directly impact convection or conduction





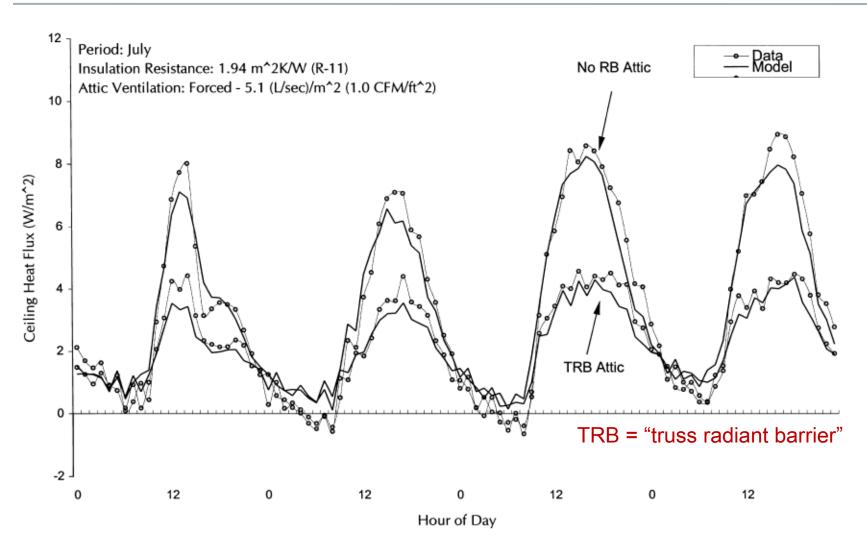


Fig. 6. Ceiling heat fluxes (TRB case, insulation resistance: 1.94 m² K/W, R-11; with attic airflow rate: 5.1 l/s/m², 1.0 CFM/ft²).

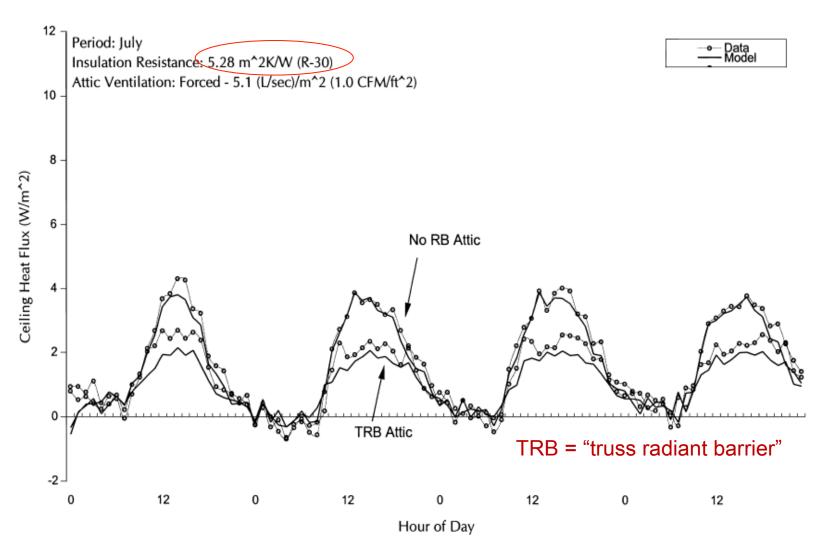
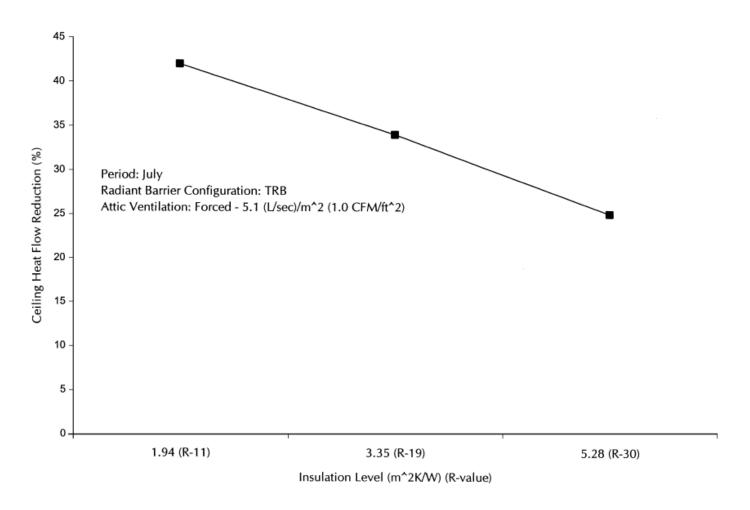
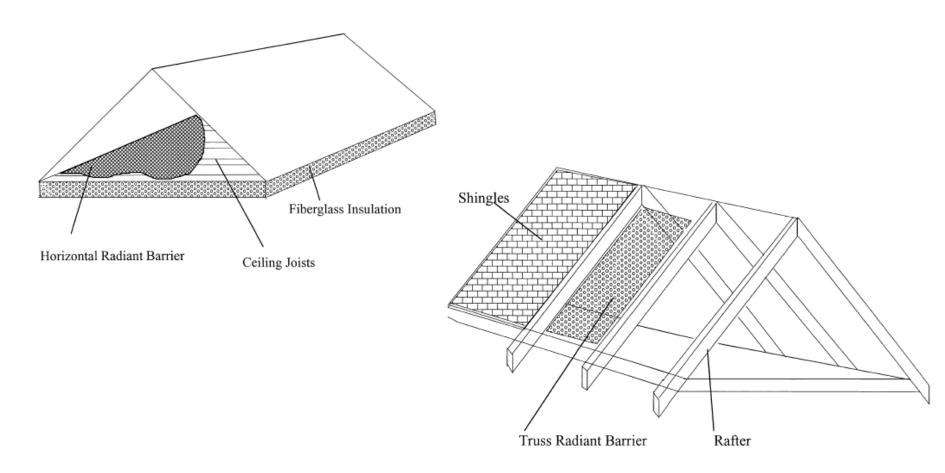


Fig. 7. Ceiling heat fluxes (TRB case, insulation resistance: 5.28 m² K/W, R-30; with attic airflow rate: 5.1 l/s/m², 1.0 CFM/ft²).

Radiant barriers have less of an impact on well-insulated roofs



 Should we install radiant barriers on attic floors or underside of roof sheathing?



 Should we install radiant barriers on attic floors or underside of roof sheathing?

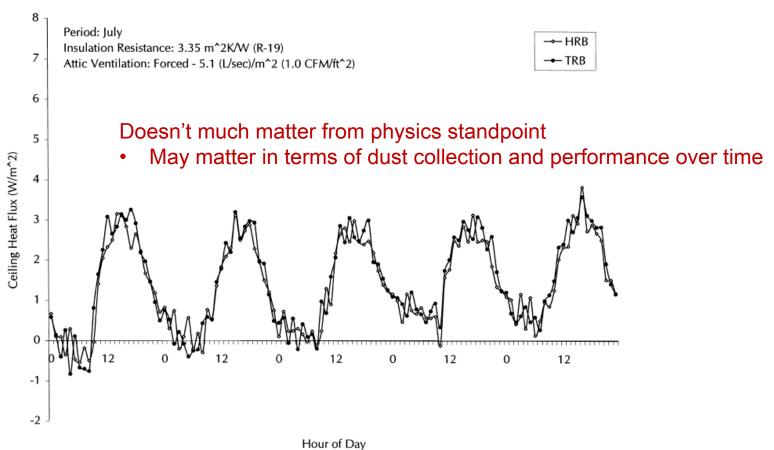


Fig. 9. Comparison between HRB and TRB configurations — experimental (insulation resistance: 3.35 m² K/W, R-19; with airflow rate: 5.1 l/s/m², 1.0 CFM/ft²).

Roof and attic heat transfer summary

- Roof surfaces can be extremely hot
 - Several energy and material longevity impacts
 - We can alter materials in design to reduce roof temperatures
- Attic air can also be very warm
 - Also has energy and comfort impacts
 - We now know what governs attic air temperatures
 - We know radiant barriers can help
 - Particularly if you have a poorly insulated roof
 - Better off just insulating roof if you can
- For both of these, we can use our modeling approaches in the design phase

WHOLE BUILDING ENERGY SIMULATION (BES) PROGRAMS

Energy simulation (BES) programs

- A wide variety of programs exists
 - http://apps1.eere.energy.gov/buildings/tools_directory/subjects_sub.cfm
 - Different levels of functions, user interfaces, and pricing
 - Some have very good GUIs with less functionality
 - Some have the exact opposite
- Most commonly used BES programs:
 - eQUEST (DOE2 engine; free; easy GUI)
 - ESPr (free; difficult to use; research grade)
 - TRNSYS (modular; requires extensive inputs; expensive)
 - TRACE 700 (from Trane; HVAC focus; expensive)
 - EnergyGauge USA (residential only; user-friendly; cheap)
 - EnergyPlus (free; excellent capabilities; modular; difficult to use)
 - Ease of use is improving with DesignBuilder USA, OpenStudio (free), and Simergy (free)
 - IES-VE (expensive; free educational; many capabilities; easy to use)⁶²

These programs rely on the same equations we've been using

$$C_{z}\frac{dT_{z}}{dt} = \sum_{i=1}^{N_{sl}} \dot{Q}_{i} + \sum_{i=1}^{N_{surfaces}} h_{i}A_{i}\left(T_{si} - T_{z}\right) + \sum_{i=1}^{N_{zones}} \dot{m}_{i}C_{p}\left(T_{zi} - T_{z}\right) + \dot{m}_{inf}C_{p}\left(T_{\infty} - T_{z}\right) + \dot{Q}_{sys}$$

where:

$$\sum_{i=1}^{N_{sl}} \dot{Q}_i = \text{sum of the convective internal loads}$$

$$\sum_{i=1}^{N_{\it surfaces}} h_i A_i \left(T_{\it si} - T_z \right)$$
 = convective heat transfer from the zone surfaces

$$\dot{m}_{\rm inf} C_p \left(T_{\infty} - T_z \right)$$
 = heat transfer due to infiltration of outside air

$$\sum_{i=1}^{N_{zones}} \dot{m_i} C_p \left(T_{zi} - T_z \right) = \text{heat transfer due to interzone air mixing}$$

$$\dot{Q}_{sys}$$
 = air systems output

$$C_z \frac{dT_z}{dt}$$
 = energy stored in zone air

$$C_z = \rho_{air}C_pC_T$$

 ρ_{air} = zone air density

C_p = zone air specific heat

Rearrange to solve for instantaneous HVAC system capacity:

$$-\dot{Q}_{sys} = \sum_{i=1}^{N_{sl}} \dot{Q}_{i} + \sum_{i=1}^{N_{surfaces}} h_{i} A_{i} \left(T_{si} - T_{z} \right) + \sum_{i=1}^{N_{zones}} \dot{m}_{i} C_{p} \left(T_{zi} - T_{z} \right) + \dot{m}_{inf} C_{p} \left(T_{\infty} - T_{z} \right)$$

Instantaneous HVAC sensible capacity also equals:

$$\dot{Q}_{sys} = \dot{m}_{sys} C_p \left(T_{sup} - T_z \right)$$

• Once you have Q_{sys} at each time step, you can calculate the energy required to deliver that rate of bulk heat transfer by knowing the efficiency/COP of your equipment

$$COP = \frac{Q_{sys}}{P_{sys}} \longrightarrow P_{sys} = \frac{Q_{sys}}{COP}$$

• Discretizing for time t versus time $t - \delta t$:

$$C_{z} \frac{T_{z}^{t} - T_{z}^{t-\delta t}}{dt} + T_{z}^{t} \left(\sum_{i=1}^{N_{surfaces}} h_{i} A_{i} + \sum_{i=1}^{N_{zones}} \dot{m}_{i} C_{p} + \dot{m}_{inf} C_{p} + \dot{m}_{sys} C_{p} \right) =$$

$$\sum_{i=1}^{N_{sl}} \dot{Q}_{i}^{t} + \dot{m}_{sys} C_{p} T_{supply}^{t} + \left(\sum_{i=1}^{N_{surfaces}} h_{i} A_{i} T_{si} + \sum_{i=1}^{N_{zones}} \dot{m}_{i} C_{p} T_{zi} + \dot{m}_{inf} C_{p} T_{\infty} \right)^{t-\delta t}$$

If there is any thermal mass at any element, link to surface T:

$$C_{p}\rho\Delta\mathbf{x}\frac{T_{i}^{j+1}-T_{i}^{j}}{\Delta t}=\frac{1}{2}\begin{bmatrix} \left(k_{w}\frac{\left(T_{i+1}^{j+1}-T_{i}^{j+1}\right)}{\Delta\mathbf{x}}+k_{E}\frac{\left(T_{i-1}^{j+1}-T_{i}^{j+1}\right)}{\Delta\mathbf{x}}\right)\\ +\left(k_{w}\frac{\left(T_{i+1}^{j}-T_{i}^{j}\right)}{\Delta\mathbf{x}}+k_{E}\frac{\left(T_{i-1}^{j}-T_{i}^{j}\right)}{\Delta\mathbf{x}}\right) \end{bmatrix}$$

Discretized conduction

Or use a lumped capacitance model (more detail next lecture):

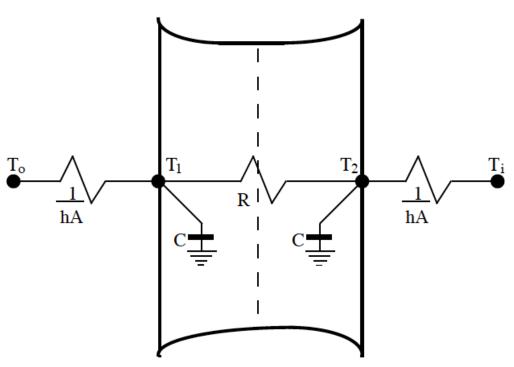


Figure 9. Two Node State Space Example.

$$C\frac{dT_1}{dt} = hA(T_o - T_1) + \frac{T_2 - T_1}{R}$$

$$C\frac{dT_2}{dt} = hA(T_i - T_2) + \frac{T_1 - T_2}{R}$$

where:

$$R = \frac{\ell}{kA}$$
,

$$C = \frac{\rho c_p \ell A}{2}$$

Lumped capacitance model for conduction

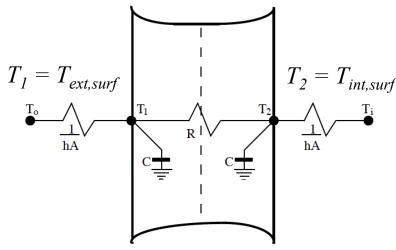


Figure 9. Two Node State Space Example.

Steady state surface energy balance...

$$\alpha I_{solar} + \varepsilon_1 \sigma F_{sky} (T_{sky}^4 - T_1^4) + \varepsilon_1 \sigma F_{air} (T_{air}^4 - T_1^4) + \varepsilon_1 \sigma F_{ground} (T_{ground}^4 - T_1^4) + h_{conv} (T_{air} - T_1) - U(T_1 - T_2) = 0$$

...becomes a time-varying surface energy balance:

$$\alpha I_{solar} + \varepsilon_{1} \sigma F_{sky} (T_{sky}^{4} - T_{1}^{4}) + \varepsilon_{1} \sigma F_{air} (T_{air}^{4} - T_{1}^{4}) + \varepsilon_{1} \sigma F_{ground} (T_{ground}^{4} - T_{1}^{4}) + h_{conv} (T_{air} - T_{1}) - U(T_{1} - T_{2}) = \frac{\rho C_{p}}{\Delta t} \frac{L}{2} (T_{1}^{n} - T_{1}^{n-1})$$

Outside Surface Heat Balance

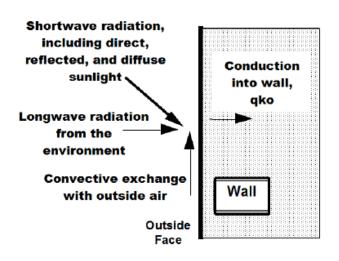


Figure 17. Outside Heat Balance Control Volume Diagram

The heat balance on the outside face is:

 $q''_{asol} + q''_{lwR} + q''_{conv} - q''_{ko} = 0$

 We know how to model all of these elements now

 Programs differ in how they select inputs, particularly heat transfer coefficients...

(64)

where.

 q''_{goal} = Absorbed direct and diffuse solar (short wavelength) radiation heat flux.

 q''_{LWR} = Net long wavelength (thermal) radiation flux exchange with the air and surroundings.

 q''_{conv} = Convective flux exchange with outside air.

 q_{ko}'' = Conduction heat flux (q/A) into the wall.

Simple Combined

The simple algorithm uses surface roughness and local surface windspeed to calculate the exterior heat transfer coefficient (key:SimpleCombined). The basic equation used is:

$$h = D + EV_z + FV_z^2 \tag{82}$$

where

h = heat transfer coefficient

 V_z = local wind speed calculated at the height above ground of the surface centroid

D, E, F = material roughness coefficients

The roughness correlation is taken from Figure 1, Page 22.4, ASHRAE Handbook of Fundamentals (ASHRAE 1989). The roughness coefficients are shown in the following table:

Table 6. Roughness Coefficients D, E, and F.

Roughness Index	D	E	F	Example Material
1 (Very Rough)	11.58	5.894	0.0	Stucco
2 (Rough)	12.49	4.065	0.028	Brick
3 (Medium Rough)	10.79	4.192	0.0	Concrete
4 (Medium Smooth)	8.23	4.0	-0.057	Clear pine
5 (Smooth)	10.22	3.1	0.0	Smooth Plaster
6 (Very Smooth)	8.23	3.33	-0.036	Glass

Inside Heat Balance

The heart of the heat balance method is the internal heat balance involving the inside faces of the zone surfaces. This heat balance is generally modeled with four coupled heat transfer components: 1) conduction through the building element, 2) convection to the air, 3) short wave radiation absorption and reflectance and 4) longwave radiant interchange. The incident short wave radiation is from the solar radiation entering the zone through windows and emittance from internal sources such as lights. The longwave radiation interchange includes the absorption and emittance of low temperature radiation sources, such as all other zone surfaces, equipment, and people.

The heat balance on the inside face can be written as follows:

$$q_{LWX}'' + q_{SW}'' + q_{LWS}'' + q_{ki}'' + q_{sol}'' + q_{conv}'' = 0 (92)$$

where:

 $q_{\scriptscriptstyle LWX}^{\prime\prime}$ = Net longwave radiant exchange flux between zone surfaces.

 q_{sw}'' = Net short wave radiation flux to surface from lights.

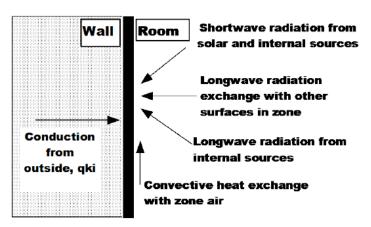
 q''_{LWS} = Longwave radiation flux from equipment in zone.

 q_{ki}'' = Conduction flux through the wall.

 q_{sol}'' = Transmitted solar radiation flux absorbed at surface.

 q''_{conv} = Convective heat flux to zone air.

Each of these heat balance components is introduced briefly below.



- Choice of interior convection coefficients is complicated
 - Still a topic of ongoing research
 - Remember: Forced vs. laminar? Orientation? Cold or hot surface?
- Different equations for different surfaces
 - Simple buoyancy
 - Vertical walls, tilted surfaces, windows, etc.
 - In-floor heating or in-ceiling cooling
 - Vertical walls, heated floors, chilled ceilings, windows
 - Forced flow near diffusers
 - Ceiling diffusers, floor diffusers, near heated or cooled windows
 - Central mechanical fan circulation
 - Walls, horizontal flow
- EnergyPlus documentation has a great review of all of these

Cost analysis during design

- Were any of those enclosure design changes worth it financially?
- For any energy efficiency improvement, you expect lower energy bills
 - But that improvement also had an upfront (capital) cost
- Payback periods
 - How long will it take for energy savings to cover the initial cost?
 - Several methods to calculate
 - Simple payback
 - Cash flow analysis
 - Net present value
 - Internal rate of return
 - Return on investment

Cost analysis during design

Simple payback

- Say you are considering a \$5,000 improvement
- Your energy simulations predict \$350 per year in savings on energy bills
 - Assuming rates stay constant
- The simple payback period is: $Payback = \frac{\$5000}{\$350 / year} = 14.3 years$
- After ~14 years, you will have covered your upfront costs

Rate of return on investment

Inverse of payback period

$$ROI = \frac{1}{14.3 \ years} = 7\%$$

Cost analysis during design

- Cash flow analysis and net present value methods
 - If you take out a loan to pay for efficiency improvements, you need to factor in the interest rate on that loan/mortgage
 - Will likely extend the payback period to cover principal + interest
- Other considerations:
 - Inflation
 - Somewhat predictable
 - Changes in energy costs
 - More variable
 - Most assume energy costs will rise at a constant rate
 - Not always the case (e.g., natural gas prices today)
 - If energy costs rise above predicted, payback period shortens
 - Vice versa for falling energy costs
- Overall: who pays capital costs and who pays for energy costs?

Life cycle cost in design

- New methods of energy simulation are taking advantage of optimization algorithms to find least cost, most effective solutions for energy efficiency
- EnergyPlus and DOE2 engines both now integrate with BEopt

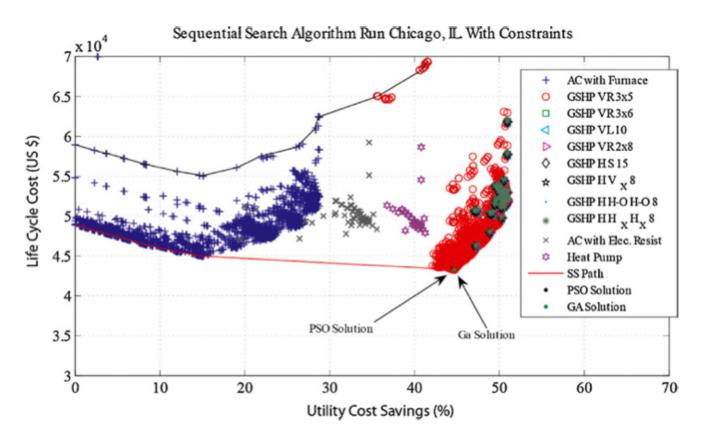
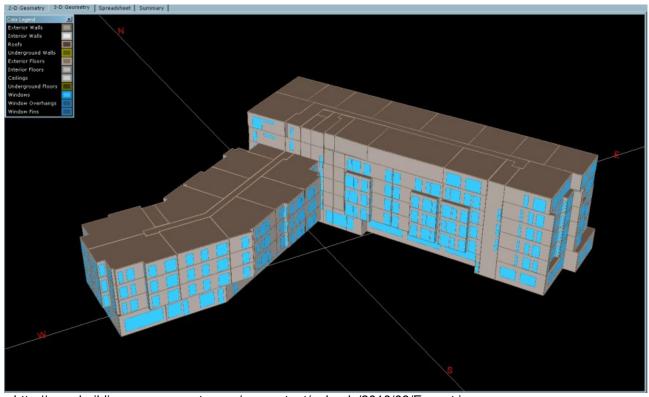


Fig. 6. LCC as a function of utility cost reduction for Chicago, IL.

Demonstration of eQUEST

- eQUEST demonstration
 - Launch program



http://www.buildingenergyexperts.com/wp-content/uploads/2010/08/Equest.jpg

HW #4

 HW #4 will involve modeling a commercial building in eQUEST

http://www.doe2.com/equest/

Current version: 3.65 (released March 2014)