

# CAE 463/524

## Building Enclosure Design

Spring 2016

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### Week 4: February 2, 2016

Solar orientation and solar radiation modeling

Built  
Environment  
Research

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# Updates

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- No class last week (ASHRAE conference)
- Campus building enclosure project expectations are on BB
  - Need to select teams (next slides)
- New teaching assistant: Akram Ali
  - PhD candidate, Civil Engineering
  - Graduate research assistant, Built Environment Research Group
  - Email: [aali21@hawk.iit.edu](mailto:aali21@hawk.iit.edu)
  - Location: Alumni 217
- Job opportunities
- Assign HW 1 (due next Tues Feb 9)

# Job opportunities

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- Career fair: Thursday, February 4<sup>th</sup>
  - 12-4 pm Hermann Hall
  - <https://web.iit.edu/career-services/employers/recruit-illinois-tech/career-fairs>
- Building enclosure companies:
  - Wiss, Janney, Elstner Associates (WJE)
    - Contact: Elizabeth (Liz) Pugh
  - Permasteelisa
    - Contact: [pna-recruiting@permasteelisagroup.com](mailto:pna-recruiting@permasteelisagroup.com)

# Campus enclosure assessment projects

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- Need to do thermal assessments by early/mid March
  - There are now 23 students in this class

Course	Name	Email	Major	Level
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CAE524-02	Dipietro, Salvatore D.	sdipietr@hawk.iit.edu	ARCE	GR
CAE524-02	Lee, JiWan	jlee232@hawk.iit.edu	CM	GR

# Campus enclosure assessment projects

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- Need to do thermal assessments by early/mid March
  - I suggest 5 teams of 4 or 5

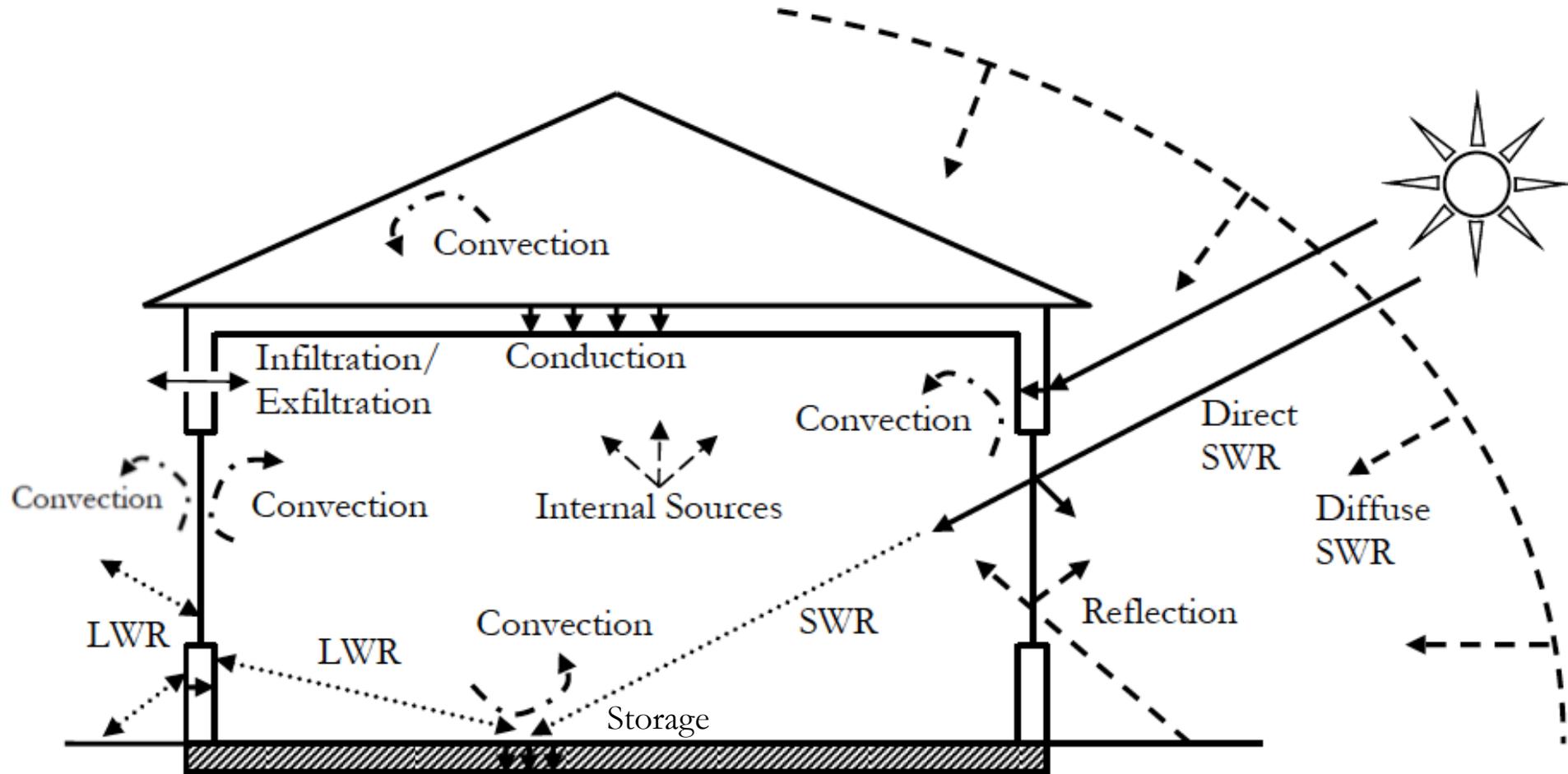
Team #	Members	Building
1	Naveen, Julia, Xu, Luanzhizi	Alumni or Life Sciences
2	Bianca, Al, Taylor, David	SSV
3	Nina, Dina, Lindsey, Salvatore	Vandercook
4	Andrea,	Crown or Alumni

# Review from last time

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- Review of building science principles
  - Psychrometrics
  - Individual modes of heat transfer and fundamental properties
  - Bringing the modes together: surface energy balances

# Building enclosures and heat transfer, visualized



# Heat transfer in building science: **Summary**

## Conduction

$$q = \frac{k}{L} (T_{surf,1} - T_{surf,2})$$

$$\frac{k}{L} = U = \frac{1}{R}$$

$$R_{total} = \frac{1}{U_{total}}$$

$$R_{total} = R_1 + R_2 + R_3 + \dots$$

For thermal bridges and combined elements:

$$U_{total} = \frac{A_1}{A_{total}} U_1 + \frac{A_2}{A_{total}} U_2 + \dots$$

## Convection

$$q_{conv} = h_{conv} (T_{fluid} - T_{surf})$$

$$R_{conv} = \frac{1}{h_{conv}}$$

## Radiation

Long-wave

$$q_{1 \rightarrow 2} = \frac{\sigma (T_{surf,1}^4 - T_{surf,2}^4)}{\frac{1 - \epsilon_1}{\epsilon_1} + \frac{A_1}{A_2} \frac{1 - \epsilon_2}{\epsilon_2} + \frac{1}{F_{12}}}$$

$$q_{rad,1 \rightarrow 2} = h_{rad} (T_{surf,1} - T_{surf,2})$$

$$h_{rad} = \frac{4\sigma T_{avg}^3}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1} \quad R_{rad} = \frac{1}{h_{rad}}$$

Or more simply:  $q_{1 \rightarrow 2} = \epsilon_{surf} \sigma F_{12} (T_{surf,1}^4 - T_{surf,2}^4)$

Solar radiation:  $q_{solar} = \alpha I_{solar}$   
(opaque surface)

Transmitted solar radiation:  $q_{solar} = \tau I_{solar}$   
(transparent surface)

# Surface energy balance: Bringing all the modes together

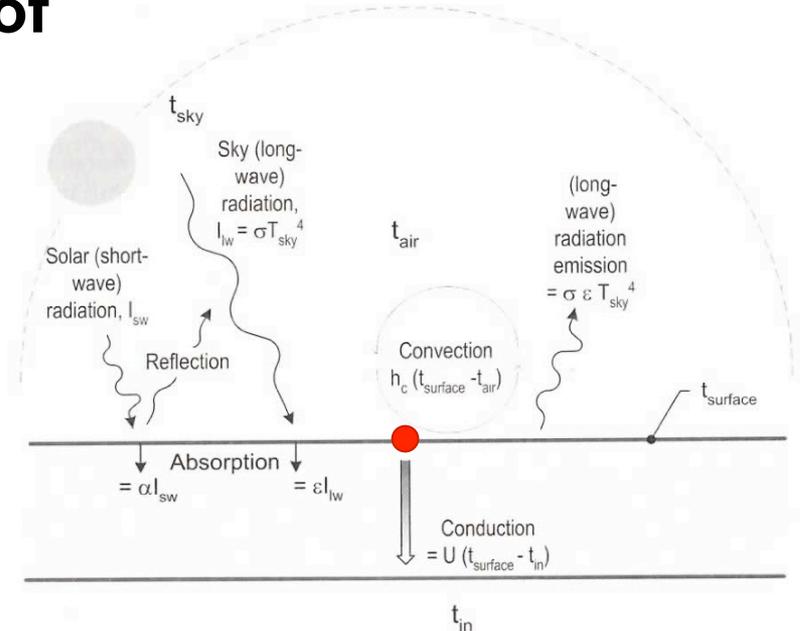
- Exterior surface example: **Roof**

$$\sum q = 0$$

We can use this equation to estimate indoor and outdoor surface temperatures

At steady state, net energy balance is zero

- Because of  $T^4$  term, often requires iteration



Solar gain

$$\alpha I_{solar}$$

$$q_{sw,solar}$$

Surface-sky radiation

$$+\epsilon_{surface} \sigma F_{sky} (T_{sky}^4 - T_{surface}^4)$$

$$+q_{lw,surface-sky}$$

Convection on external wall

$$+h_{conv} (T_{air} - T_{surface})$$

$$+q_{convection}$$

Conduction through wall

$$-U(T_{surface} - T_{surface,interior}) = 0$$

$$-q_{conduction} = 0$$

# Roof surface temperature example

<i>Surface energy balance</i>	<i>Add</i> W/m <sup>2</sup>	<i>Subtract</i> W/m <sup>2</sup>
Solar (short-wave)	900	
Surface-sky long-wave radiation	-338	
Convection on roof	-551	
Conduction through roof		11
<b>SUM</b>	<b>0</b>	

<i>Given</i>	alpha	0.9	bituminous membrane	
<i>Given</i>	I <sub>total</sub> , W/m <sup>2</sup>	1000		
<i>Assume</i>	F <sub>surface-sky</sub>	1		
<i>Assume</i>	e <sub>surface</sub>	0.9		
<i>Given</i>	T <sub>air,out</sub> , K	293.15	20 degC	
<i>Assume</i>	T <sub>air,out,dewpoint</sub> , K	275.06	1.91 degC	<i>psych chart</i>
<i>Calculate</i>	e <sub>sky</sub>	0.79	N = 0	
<i>Calculate</i>	T <sub>sky</sub> , K	276.61	T <sub>sky</sub> equation for clear day	
<b>Guess</b>	<b>T<sub>surface</sub>, K</b>	<b>334.25</b>	<b>61.1 degC</b>	
<i>Given</i>	T <sub>surf,in</sub> , K	295.15	22.0 degC	
<i>Constant</i>	stef-boltz, W/(m <sup>2</sup> K <sup>4</sup> )	5.6704E-08		
<i>Calculate</i>	h <sub>conv</sub> , W/m <sup>2</sup> K	13.4		
<i>Given</i>	R-value IP, h-ft <sup>2</sup> -F/Btu	20		
<i>Given</i>	R-value, SI	3.52		
<i>Given</i>	U-value, W/m <sup>2</sup> K	0.28		

Adjust T<sub>surface</sub> until  
sum of all heat  
transfer modes  
equals zero

# Roof surface temperature example (**low absorptivity**)

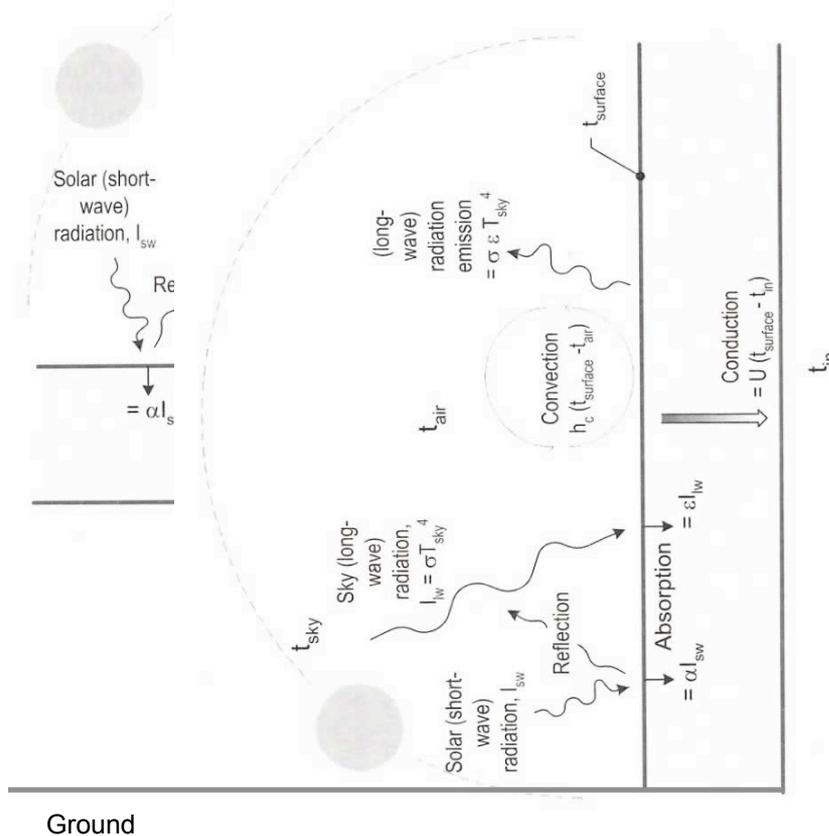
<i>Surface energy balance</i>	<i>Add</i> W/m <sup>2</sup>	<i>Subtract</i> W/m <sup>2</sup>
Solar (short-wave)	300	
Surface-sky long-wave radiation	-141	
Convection on roof	-155	
Conduction through roof		3
<b>SUM</b>	<b>0</b>	

<i>Given</i>	alpha	0.3	bituminous membrane	
<i>Given</i>	I <sub>total</sub> , W/m <sup>2</sup>	1000		
<i>Assume</i>	F <sub>surface-sky</sub>	1		
<i>Assume</i>	e <sub>surface</sub>	0.9		
<i>Given</i>	T <sub>air,out</sub> , K	293.15	20 degC	
<i>Assume</i>	T <sub>air,out,dewpoint</sub> , K	275.06	1.91 degC	<i>psych chart</i>
<i>Calculate</i>	e <sub>sky</sub>	0.79	N = 0	
<i>Calculate</i>	T <sub>sky</sub> , K	276.61	T <sub>sky</sub> equation for clear day	
<b>Guess</b>	<b>T<sub>surface</sub>, K</b>	<b>304.75</b>	<b>31.6 degC</b>	
<i>Given</i>	T <sub>surf,in</sub> , K	295.15	22.0 degC	
<i>Constant</i>	stef-boltz, W/(m <sup>2</sup> K <sup>4</sup> )	5.6704E-08		
<i>Calculate</i>	h <sub>conv</sub> , W/m <sup>2</sup> K	13.4		
<i>Given</i>	R-value IP, h-ft <sup>2</sup> -F/Btu	20		
<i>Given</i>	R-value, SI	3.52		
<i>Given</i>	U-value, W/m <sup>2</sup> K	0.28		

# Bringing all the modes together

- Similarly, for a vertical surface:

$$q_{solar} + q_{lwr} + q_{conv} - q_{cond} = 0$$



$$\alpha I_{solar}$$

$$+\epsilon_{surface} \sigma F_{sky} (T_{sky}^4 - T_{surface}^4)$$

$$+\epsilon_{surface} \sigma F_{ground} (T_{ground}^4 - T_{surface}^4)$$

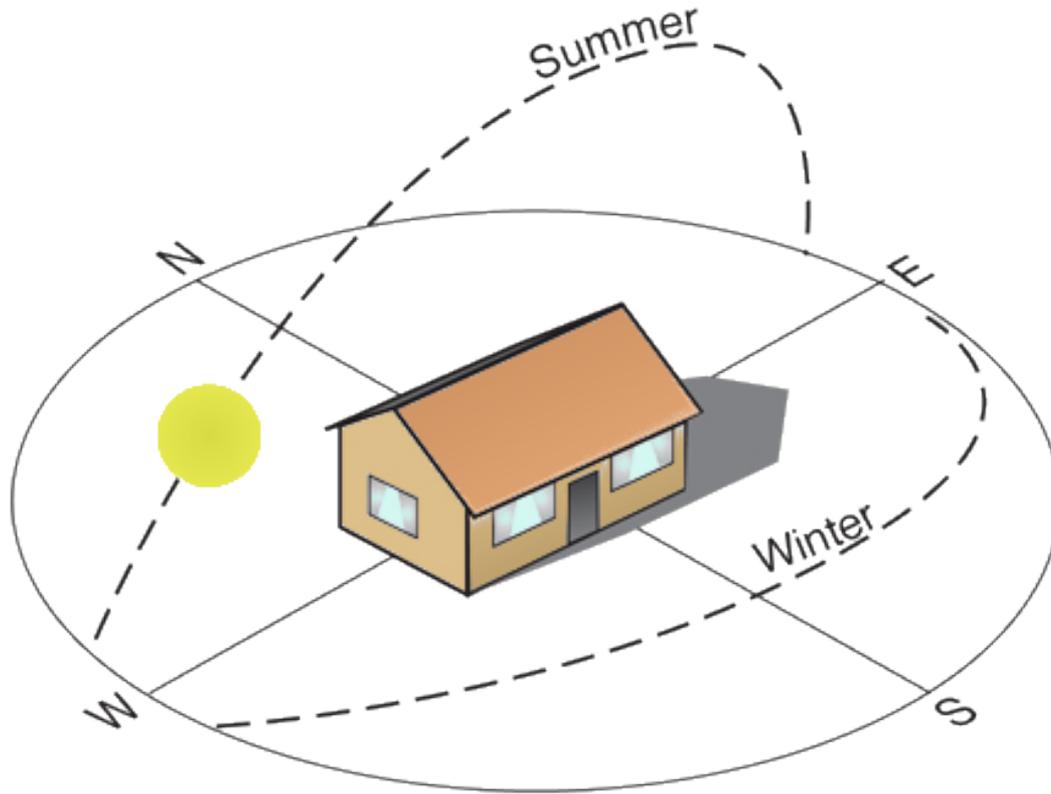
$$+h_{conv} (T_{air} - T_{surface})$$

$$-U (T_{surface} - T_{surface,interior}) = 0$$

# Today's objectives

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- Solar orientation and enclosures
- Assign HW #1



# SOLAR ORIENTATION

# Chicago: Sunrise to sunset

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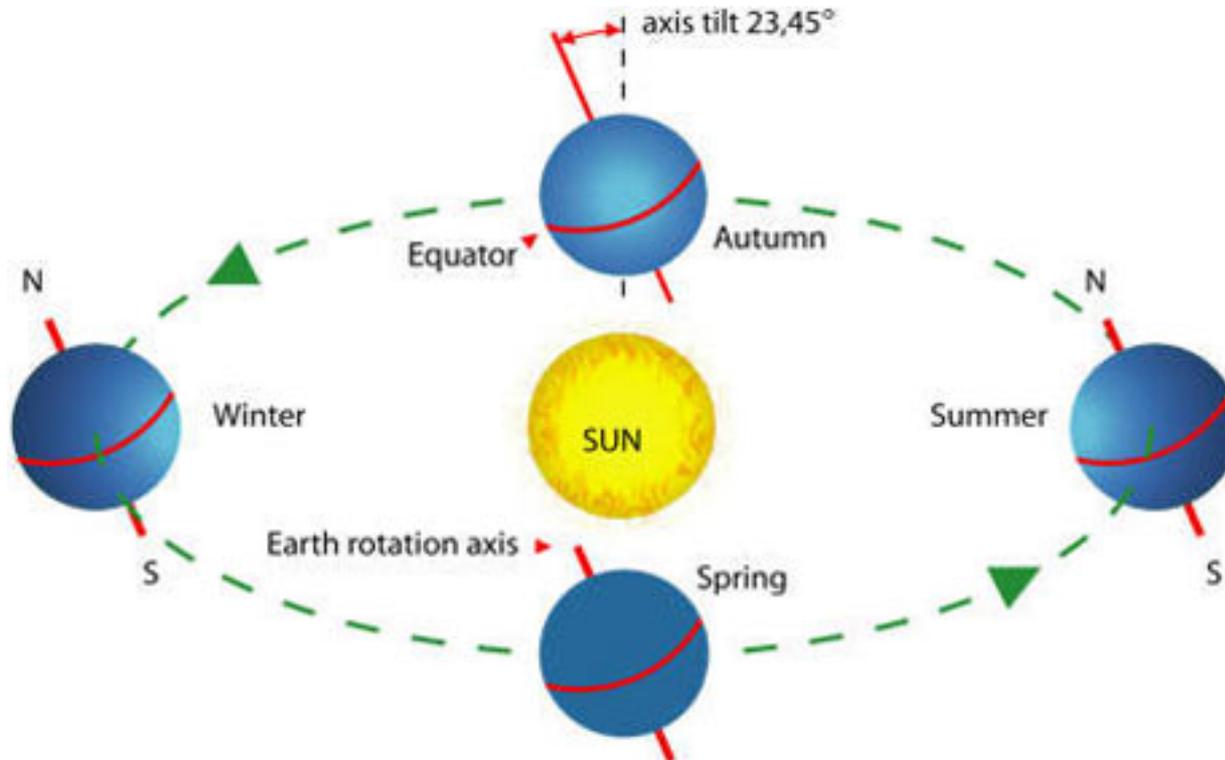
# Solar radiation

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- The sun is the source of most energy on the earth
- We need to have a working knowledge of earth's relationship to the sun
- We should be able to estimate solar radiation intensity
  - To understand thermal effects of solar radiation and how to control or utilize them:
  - We need to estimate solar gains on a building, and
  - We need to predict intensity of solar radiation and the direction at which it strikes building surfaces
    - It starts with relationships between the sun and the earth

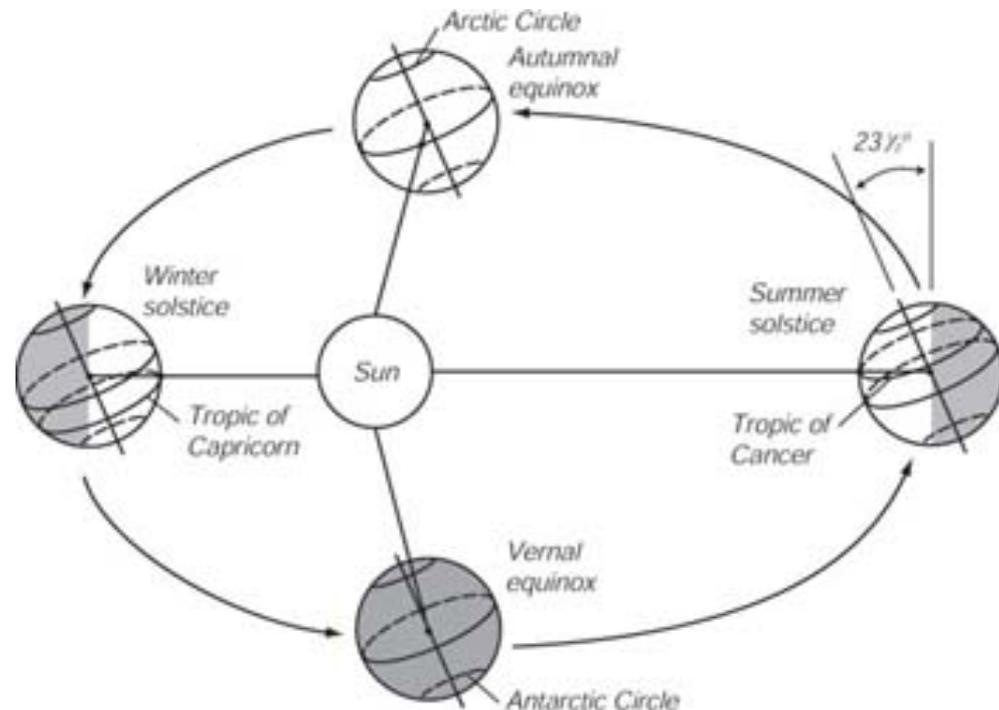
# Solar radiation: earth-sun relationship

- Earth rotates about its axis every 24 hours
- Earth revolves around sun every 365.2425 days
- Earth is tilted at an angle of  $23.45^\circ$



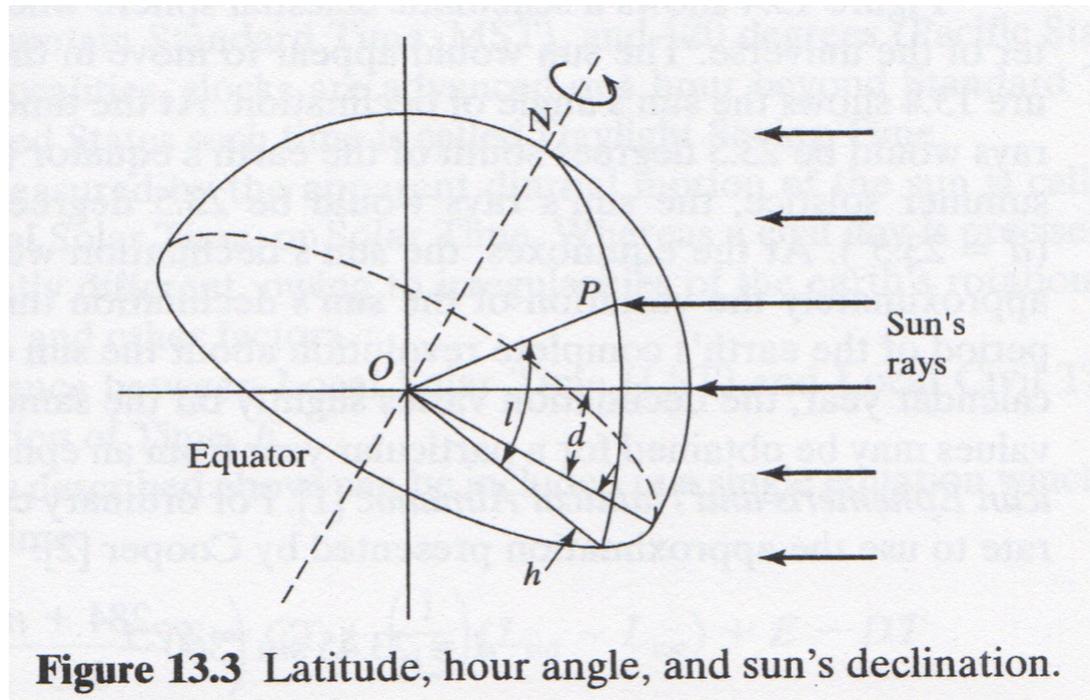
# Solar radiation: earth-sun relationship

- Therefore, different locations on earth receive different levels of solar radiation during different times of the year (and different times of the day)
  - The greatest amount of solar radiation is delivered to northern hemisphere on **June 21**
  - Least amount of solar energy delivered on **December 21**
- There are methods of determining the amount of flux of solar radiation to surfaces on the earth



# Earth-sun relationships

- The position of a point  $P$  on the earth's surface with respect to the sun's rays can be calculated if we know:
  - Latitude of point on earth,  $l$  (degrees)
  - Hour angle of the point on earth,  $h$  (degrees)
  - Sun's declination,  $d$  (degrees)



# Earth-sun relationships

- Sun's declination,  $d$ , can be estimated by:

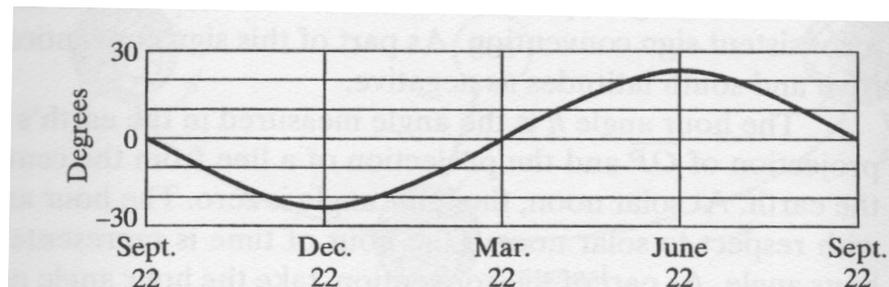
$$d = 23.45 \sin\left(360 \frac{284 + n}{365}\right)$$

Where  $n$  is the day of the year, which you can determine by counting on your hands, looking up online, or using this table:

**TABLE 13.1** Variation in  $n$  throughout the Year for Eq. (13.1)

Month	$n$ for the Day of the Month, $D$	Month	$n$ for the Day of the Month, $D$
January	$D$	July	$181 + D$
February	$31 + D$	August	$212 + D$
March	$59 + D$	September	$243 + D$
April	$90 + D$	October	$273 + D$
May	$120 + D$	November	$304 + D$
June	$151 + D$	December	$334 + D$

Where  $D$  is the day of the month



**Figure 13.5** Variation of sun's declination.

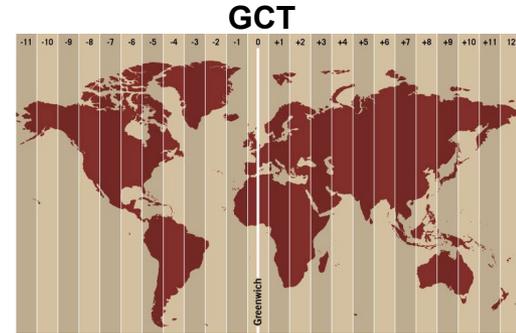
$d$  is **positive** when sun's rays are **north** of the equator

# Earth-sun relationships

- Now we have latitude ( $l$ ) and sun's declination ( $d$ )
  - Need hour angle ( $h$ )

It's all about **time**:

- Greenwich Civil Time = time at line of zero longitude
- Local Civil Time (CT) is governed by your longitude
  - $1/15^{\text{th}}$  of an hour (4 mins) of time for each degree difference in longitude
    - Central Standard Time is 90 degrees from 0
    - 4 min per degree \* 90 degrees = 360 minutes = 6 hours
- Time is also measured by apparent diurnal motion of the sun
  - Apparent Solar Time (AST), Local Solar Time (LST), or Solar Time (ST)
    - Interchangeable terms
  - Slightly different than a civil day because of irregularities of the earth's rotation and shape of earth's orbit
  - The difference between solar time (LST) and civil time (CT) is called the **Equation of Time ( $E$ )**



# Calculating solar time (LST)

- Local **solar** time (LST):

$$\text{LST} = \text{CT} + \left(\frac{1}{15}\right)(L_{\text{std}} - L_{\text{loc}}) + E - \text{DT}$$

Where:

LST = local solar time (hour)

CT = clock time (hour)

$L_{\text{std}}$  = standard meridian longitude for local time zone (degrees west)

$L_{\text{loc}}$  = longitude of actual location (degrees west)

$E$  = Equation of Time (hour)

$\text{DT}$  = Daylight savings time correction (hour)

\* $\text{DT} = 1$  if on DST; otherwise 0

\*\*Note that all times should be converted to decimal format from 0 to 24. For example, 3:45 PM = 15.75 hours

- Equation of Time:  $E = 0.165 \sin 2B - 0.126 \cos B - 0.025 \sin B$

where  $B = \frac{360(n - 81)}{364}$  and  $n$  is the day of the year.

$B$  is in degrees

# Calculating solar time (LST)

- Finally, the solar hour angle,  $h$ , can be calculated:

$$h = 15(\text{LST} - 12) \text{ degrees}$$

$h$  is **positive after** solar noon and **negative before**

LST is in 24 hour format

- Again, you can either calculate these values, use a website\*, or look them up in a table like this:

TABLE 13.2 The Sun's Declination and Equation of Time, Calculated

Month	Day							
	7		14		21		28	
	Declination, Degrees	Eq. of Time, Hours						
January	-22.4	-0.10	-21.4	-0.15	-20.1	-0.19	-18.5	-0.22
February	-15.8	-0.24	-13.6	-0.24	-11.2	-0.24	-8.7	-0.22
March	-6.0	-0.20	-3.2	-0.17	-0.4	-0.13	2.4	-0.09
April	6.4	-0.04	9.0	-0.01	11.6	0.02	13.9	0.04
May	16.7	0.06	18.5	0.06	20.1	0.06	21.4	0.05
June	22.7	0.02	23.3	0.00	23.45	-0.03	23.3	-0.05
July	22.6	-0.08	21.7	-0.09	20.4	-0.10	18.9	-0.10
August	16.3	-0.09	14.1	-0.07	11.8	-0.04	9.2	-0.01
September	5.4	0.05	2.6	0.09	-0.2	0.13	-3.0	0.17
October	-6.6	0.22	-9.2	0.25	-11.8	0.27	-14.1	0.27
November	-17.1	0.27	-18.9	0.25	-20.4	0.22	-21.7	0.18
December	-22.8	0.12	-23.3	0.07	-23.45	0.02	-23.3	-0.04

\*NOAA has website for this: <http://www.esrl.noaa.gov/gmd/grad/solcalc/>

# Calculating solar time (LST) and hour angle ( $h$ )

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- Example problem:
- Determine the local solar time and sun's hour angle in Minneapolis, MN ( $44.9^\circ$  N,  $93.3^\circ$  W) at 2:25 PM Central Daylight Savings Time on July 21

# Earth-sun relationships

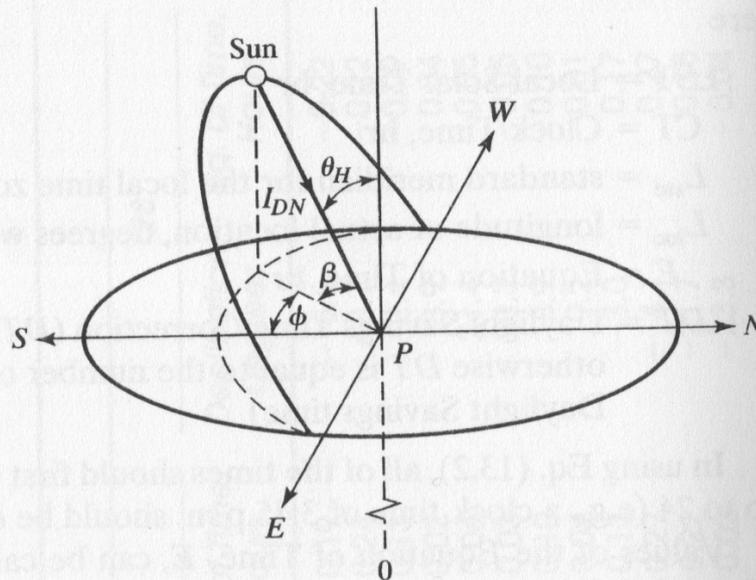
- Once we have our local latitude  $l$ , the sun's declination angle  $d$ , and the hour angle  $h$ , we can move on to other important relationships:

## Three important angles (°)

$\theta_H$  = **sun's zenith angle**  
angle between the sun's rays and the local vertical

$\beta$  = **altitude angle**  
angle in a vertical plane between the sun's rays and the projection of the earth's horizontal plane

$\phi$  = **solar azimuth angle**  
angle in the horizontal plane measured from south to the horizontal projection of the sun's rays



**Figure 13.6** Definition of sun's zenith, altitude, and azimuth angles.

\*Note that  $I_{DN}$  represents the sun's rays



# Determining solar angles

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- After a lot of complex geometry/trigonometry...

$$\cos \theta_H = \cos l \cos h \cos d + \sin l \sin d$$

$$\sin \beta = \cos l \cos h \cos d + \sin l \sin d$$

$$\cos \phi = (\cos d \sin l \cos h - \sin d \cos l) / \cos \beta$$

**A note on sign conventions for all of these relationships:**

North latitudes ( $l$ ) are positive, south latitudes are negative

Declination ( $d$ ) is positive when sun's rays are north of equator

Hour angle ( $h$ ) is negative before solar noon, positive after

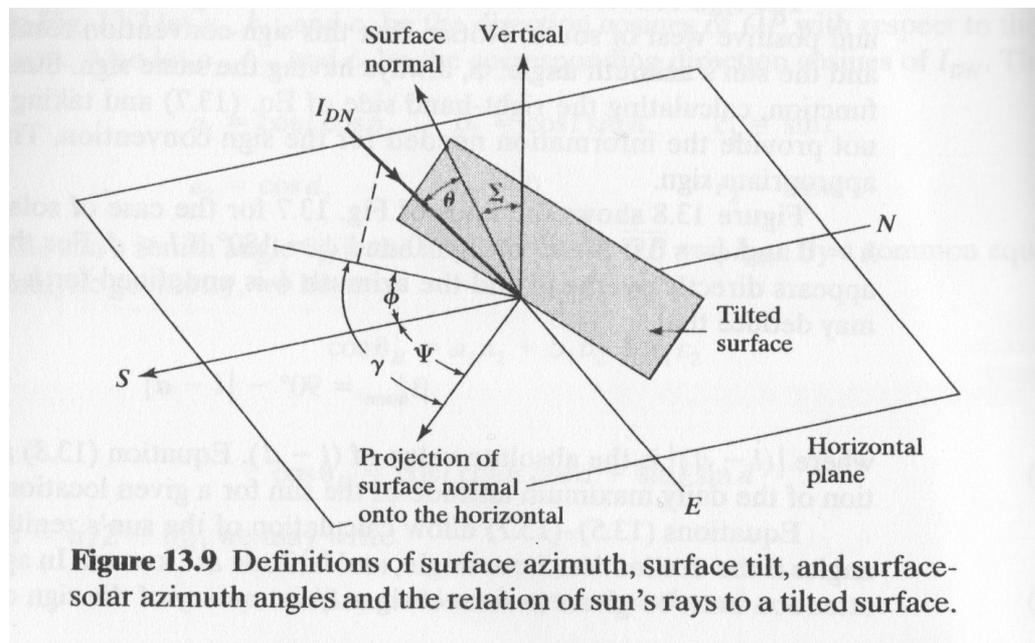
Azimuth angle ( $\phi$ ) is negative before solar noon, positive after (same as  $h$ )

Note that  $\beta$  for solar noon = 90 degrees -  $|l - d|$

Also note that  $\beta + \theta_H = 90$  degrees

# Earth-sun relationships

- Last but not least...
- The previous relationships identify a point on the earth's surface in relation to the sun
  - All valid for horizontal surfaces
  - Buildings are not horizontal surfaces!
- Need to describe **surface-sun** relationships:



# Surface-sun relationships

## More important angles (°)

### $\theta$ = incidence angle

angle between the solar rays and the surface normal

### $\Sigma$ = surface tilt angle

angle between surface normal and the vertical

Vertical surface:  $\Sigma = 90^\circ$

Horizontal surface:  $\Sigma = 0^\circ$

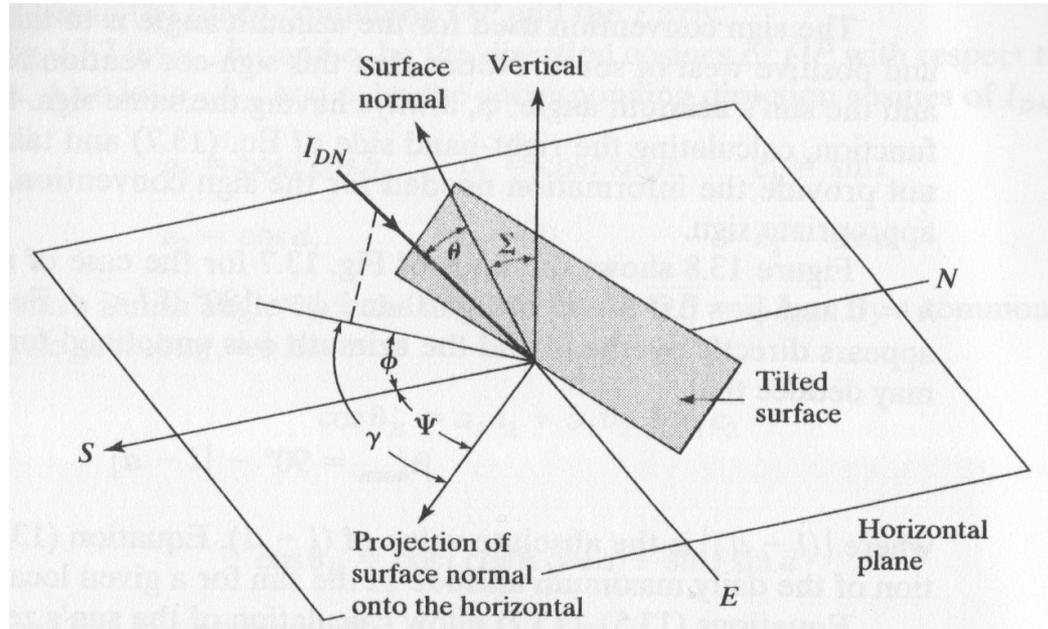
### $\Psi$ = surface azimuth angle

angle between south and the horizontal projection of the surface normal

### $\gamma$ = surface-solar azimuth angle

angle between horizontal projection of solar rays and the horizontal projection of the surface normal

$$\gamma = |\phi - \Psi|$$



**Figure 13.9** Definitions of surface azimuth, surface tilt, and surface-solar azimuth angles and the relation of sun's rays to a tilted surface.

\*Sign convention:  $\Psi$  is negative for a surface that faces east of south and positive for a surface that faces west of south

### Tilted surface:

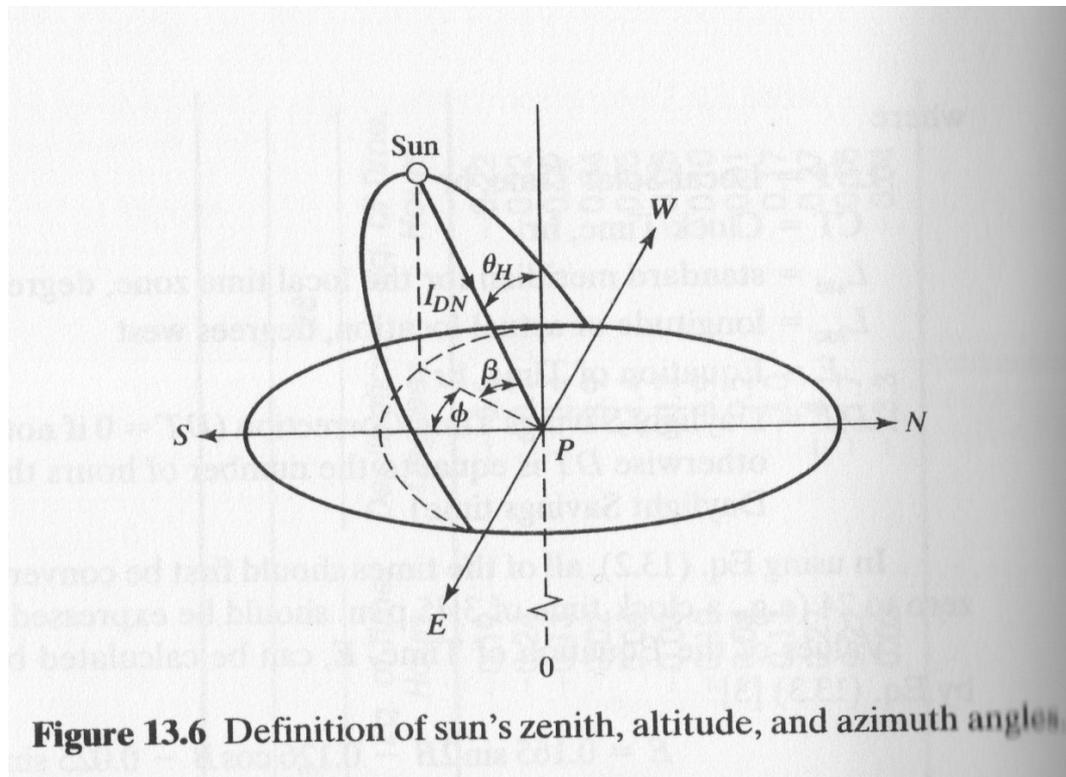
$$\cos \theta = \cos \beta \cos \gamma \sin \Sigma + \sin \beta \cos \Sigma$$

### Vertical surface ( $\Sigma = 90^\circ$ ):

$$\cos \theta = \cos \beta \cos \gamma$$

# Surface-sun relationships: Example problem

- Calculate the sun's altitude ( $\beta$ ) and azimuth ( $\phi$ ) angles at 7:30 am local solar time (LST) on August 7 for a location at 40 degrees north latitude



# Surface-sun relationships: Example problem

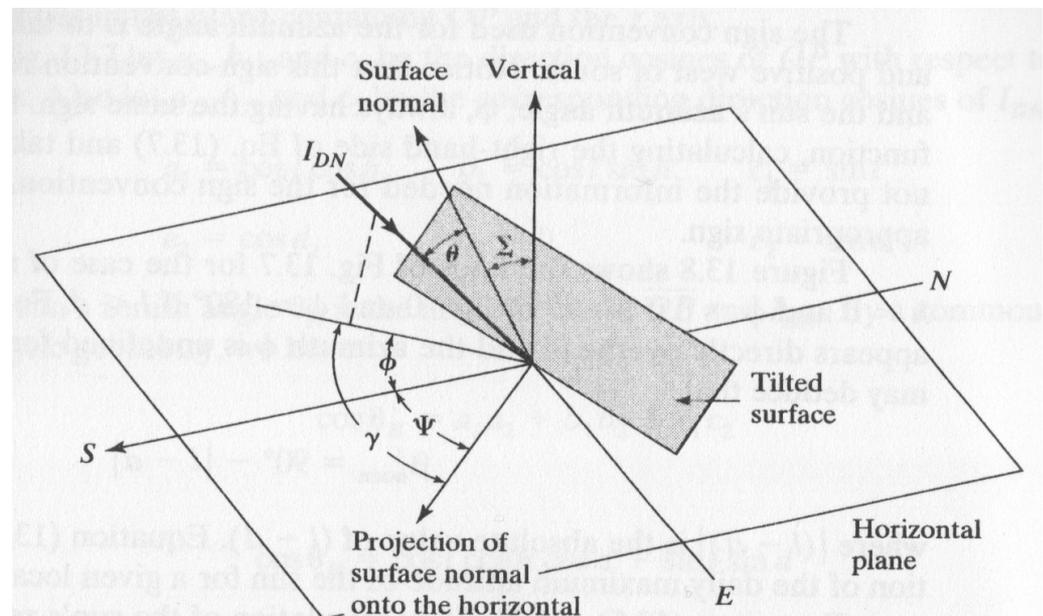
- Calculate sun's incidence angle for a vertical surface that faces 25 degrees east of south and has a tilt angle of 60 degrees at 3:00 pm local solar time on June 7 for a location at 36 degrees north latitude

## Translation:

Find  $\theta$

Given:

$\Psi, \Sigma, l, h, \beta, \phi$



**Figure 13.9** Definitions of surface azimuth, surface tilt, and surface-solar azimuth angles and the relation of sun's rays to a tilted surface.

# What is this all about? ... Solar flux

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- Once we know earth-surface-sun relationships, we can eventually get to the effects of those relationships on actual solar radiation intensity
- Solar radiation intensity is roughly constant at the outer layer of the atmosphere
  - 1367 W/m<sup>2</sup> – varying a few percent depending on time of year
- The earth's atmosphere depletes some direct solar radiation
  - Intercepted by other air molecules, water molecules, dust particles
  - Remaining reaches earth's surface unchanged in wavelength
    - Direct radiation
  - The deflected radiation turns aside from the direct beam
    - Diffuse radiation

# Estimating solar flux

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- Estimating intensity of direct normal solar radiation:
  - There are many, *many* ways to estimate this
  - ASHRAE uses a model for “average clear days” that works well for most of our purposes

$$I_{DN} = Ae^{-B/\sin\beta}$$

Where:

$I_{DN}$  = direct normal irradiance, or amount of solar radiation per unit area on a surface that is always held perpendicular to the sun's rays ( $\text{W}/\text{m}^2$ )

$A$  = apparent direct normal solar flux at outer edge of earth's atmosphere ( $\text{W}/\text{m}^2$ )

$B$  = empirically determined atmospheric extinction coefficient (dimensionless)

$\beta$  = altitude angle

- Estimating intensity of diffuse horizontal radiation:  $I_{dH} = CI_{DN}$

Where:

$I_{dH}$  = diffuse horizontal irradiance, or that which is scattered ( $\text{W}/\text{m}^2$ )

$C$  = empirically determined coefficient for typical “clear days” (dimensionless)

# Typical clear day values for solar radiation

**TABLE 13.3** Coefficients for Average Clear Day Solar Radiation Calculations for the Twenty-First Day of Each Month, Base Year 1964

	A		B	C	Declination, deg	Equation of Time, hr
	$\frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2}$	$\frac{\text{W}}{\text{m}^2}$	Dimensionless Ratios			
January	390	1230	0.142	0.058	-20.0	-0.19
February	385	1215	0.144	0.060	-10.8	-0.23
March	376	1186	0.156	0.071	0.0	-0.13
April	360	1136	0.180	0.097	11.6	0.02
May	350	1104	0.196	0.121	20.0	0.06
June	345	1088	0.205	0.134	23.45	-0.02
July	344	1085	0.207	0.136	20.6	-0.10
August	351	1107	0.201	0.122	12.3	-0.04
September	365	1151	0.177	0.092	0	0.13
October	378	1192	0.160	0.073	-10.5	0.26
November	387	1221	0.149	0.063	-19.8	0.23
December	391	1233	0.142	0.057	-23.45	0.03

SOURCE: Adapted by permission from *ASHRAE Handbook, Fundamentals Edition, 1993*.

$$I_{DN} = Ae^{-\frac{B}{\sin \beta}}$$

# Solar flux to building surfaces (**finally!**)

---

- Solar radiation striking a surface:  $I_{solar} = I_D + I_d + I_R$ 
  - Direct + diffuse + reflected

- Direct ( $I_D$ ):  $I_D = I_{DN} \cos \theta$

Where:

$\theta$  = incidence angle, or the angle between the solar rays and the surface normal

$I_{DN}$  = direct normal irradiance (W/m<sup>2</sup>)

- Diffuse ( $I_d$ ):  $I_d = I_{dH} \frac{1 + \cos \Sigma}{2}$

Where:

$\Sigma$  = surface tilt angle, or the angle between surface normal and surface vertical

$I_{dH}$  = diffuse horizontal solar radiation (W/m<sup>2</sup>)

# Solar flux to building surfaces (**finally!**)

---

- Reflected ( $I_R$ )
  - Radiation striking a surface after reflecting off surrounding surfaces
  - Similar to diffuse
  - Usually concerned with reflection from the ground

$$I_R = \frac{\rho_g I_H (1 - \cos \Sigma)}{2}$$

Where:

$\rho_g$  = solar reflectance of the ground (depends on surface, usually 0.1-0.4)

$I_H$  = total solar flux striking the horizontal ground ( $\text{W/m}^2$ )

$$I_H = I_{DN} \cos \theta_H + I_{dH}$$

# Solar flux to building surfaces

- Reflected ( $I_R$ )
  - Values of reflectance ( $\rho_g$ ) for common ground surfaces

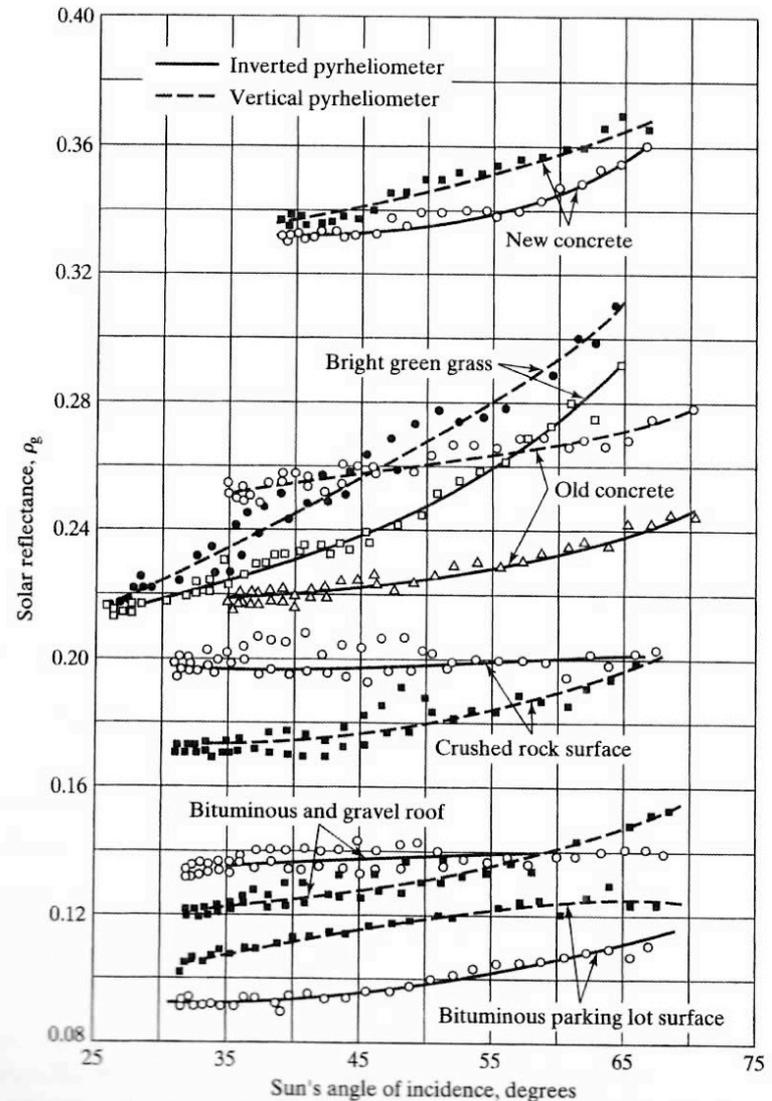


Figure 13.21 Solar reflectance for various ground surfaces. [Reprinted by permission from *ASHRAE Trans.*, 69 (1963), 31.]

# Solar flux to building surfaces: Example problem

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- Find the solar flux incident on the tilted surface used in the previous problem
  - Assume a ground reflectance of 0.15

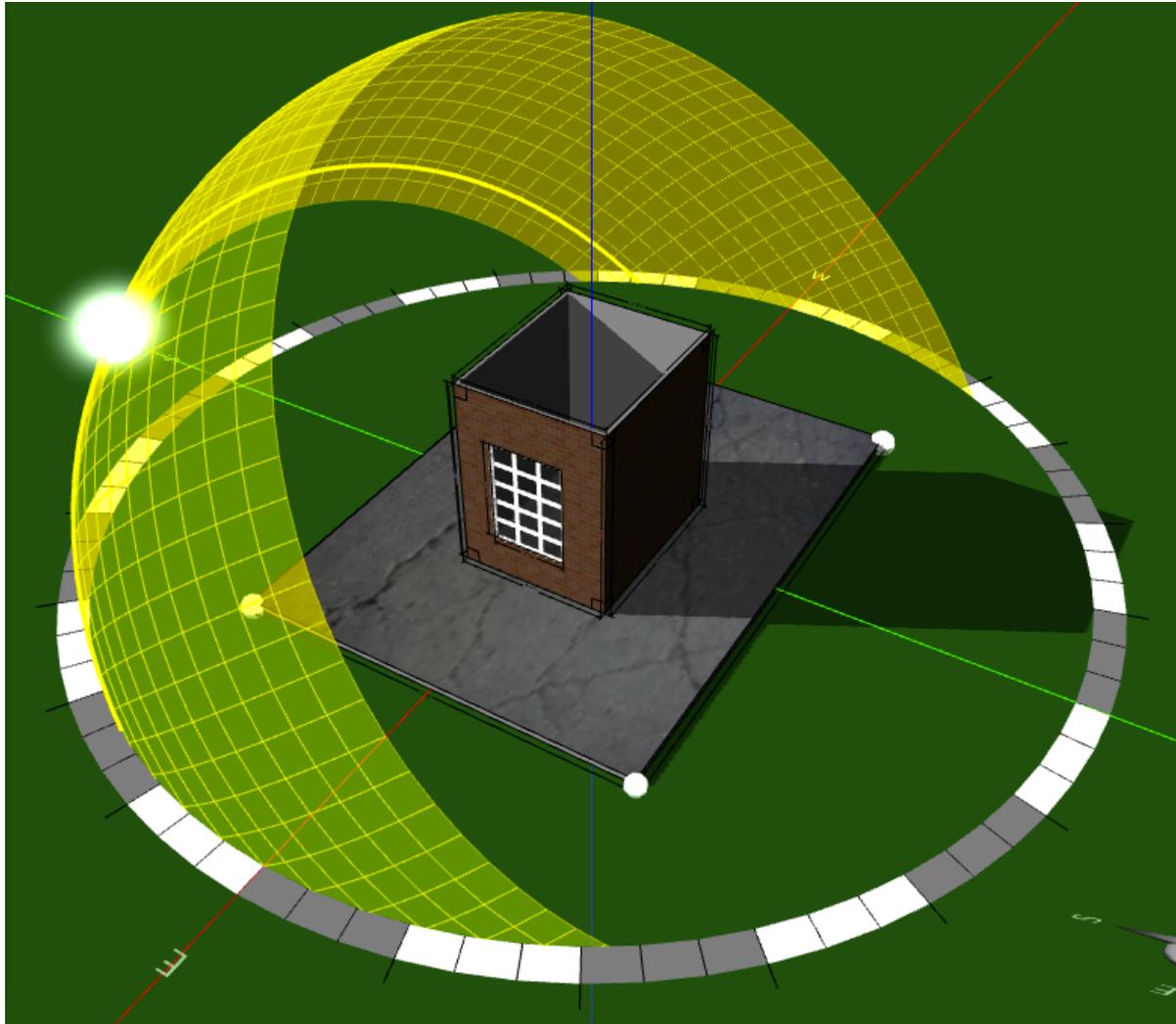
# Solar orientation videos/software

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- [http://built-envi.com/wp-content/uploads/2013/07/solar\\_position\\_ies.zip](http://built-envi.com/wp-content/uploads/2013/07/solar_position_ies.zip)
  - 56 mb zip file of several videos
- January, April, July, November 1<sup>st</sup>
  - Just one day (24 hours)
- 6 am, 9 am, 12 pm, and 4pm for an entire year

# Solar orientation videos/software

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# Refined solar data

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- Now, you could make all of these calculations by hand for every hour of the day, or...

# Downloading solar data

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- For hourly sun positions, you can build a calculator or use one from the internet
  - <http://www.susdesign.com/sunposition/index.php>
  - <http://www.esrl.noaa.gov/gmd/grad/solcalc/azel.html>
- For solar position and intensity (from time and place)
  - <http://www.nrel.gov/midc/solpos/solpos.html>
  - Output of interest = “global irradiance on a tilted surface”
- For *actual* hourly solar data (direct + diffuse in W/m<sup>2</sup>)
  - [http://rredc.nrel.gov/solar/old\\_data/nsrdb/](http://rredc.nrel.gov/solar/old_data/nsrdb/)
  - Output of interest = “direct normal radiation” → adjust using  $\cos\theta$ 
    - Note: “typical meteorological years”

# Typical meteorological year (TMY)

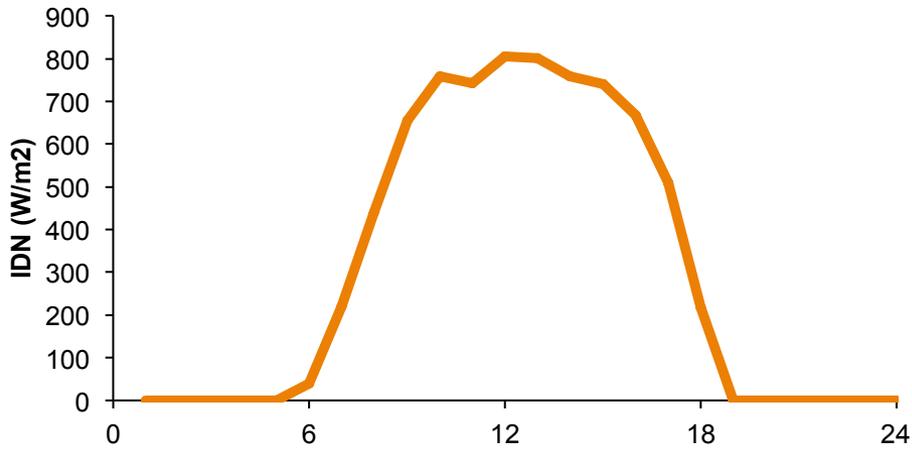
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- For heating and cooling load calculations and for hourly building energy simulations, we often rely on a collection of weather data for a specific location
- We generate this data to be representative of more than just the previous year
  - Represents a wide range of weather phenomena for our location
  - TMY3: Data for 1020 locations from 1960 to 2005
    - Composed of 12 typical meteorological months
    - Each month is pulled from a random year in the range
    - Actual time-series climate data
    - Mixture of measured and modeled solar values
    - [http://rredc.nrel.gov/solar/old\\_data/nsrdb/1991-2005/tmy3/](http://rredc.nrel.gov/solar/old_data/nsrdb/1991-2005/tmy3/)
  - Variables include: outdoor temperature, direct normal radiation, wind speed, wind direction, outdoor RH, cloud cover, and more

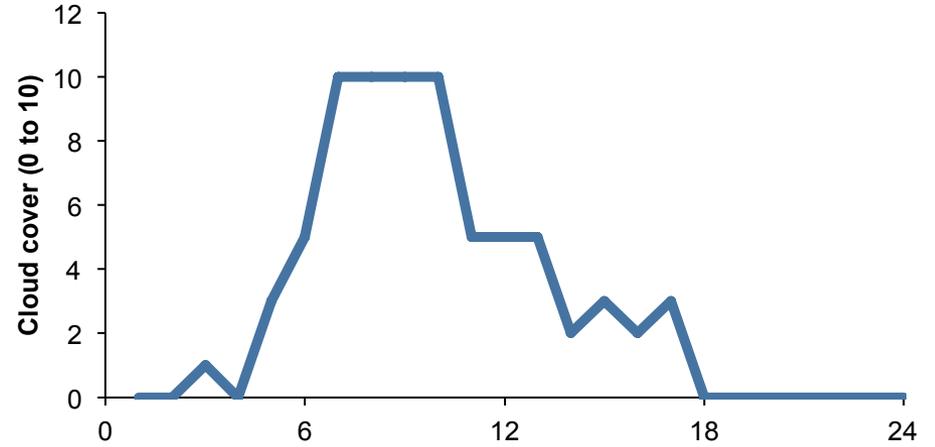
# Typical meteorological year (TMY): Solar data

Data for typical September 10<sup>th</sup> at Midway, Chicago, IL

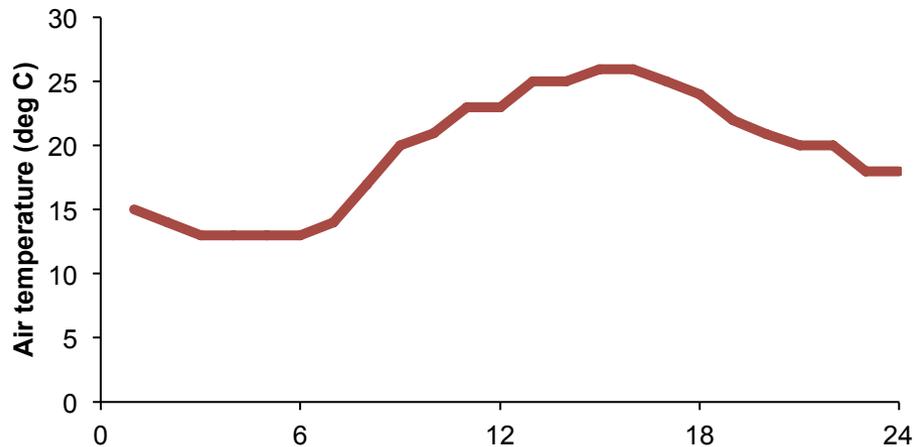
## Direct Normal Irradiance



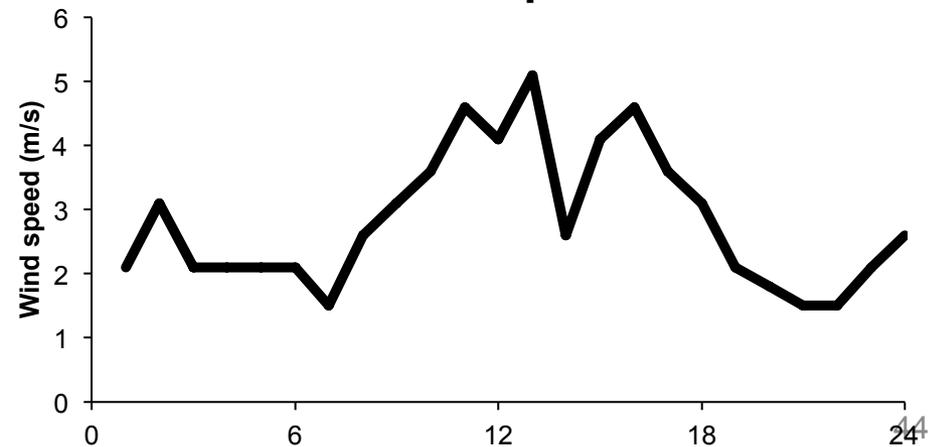
## Cloud Cover



## Air temperature

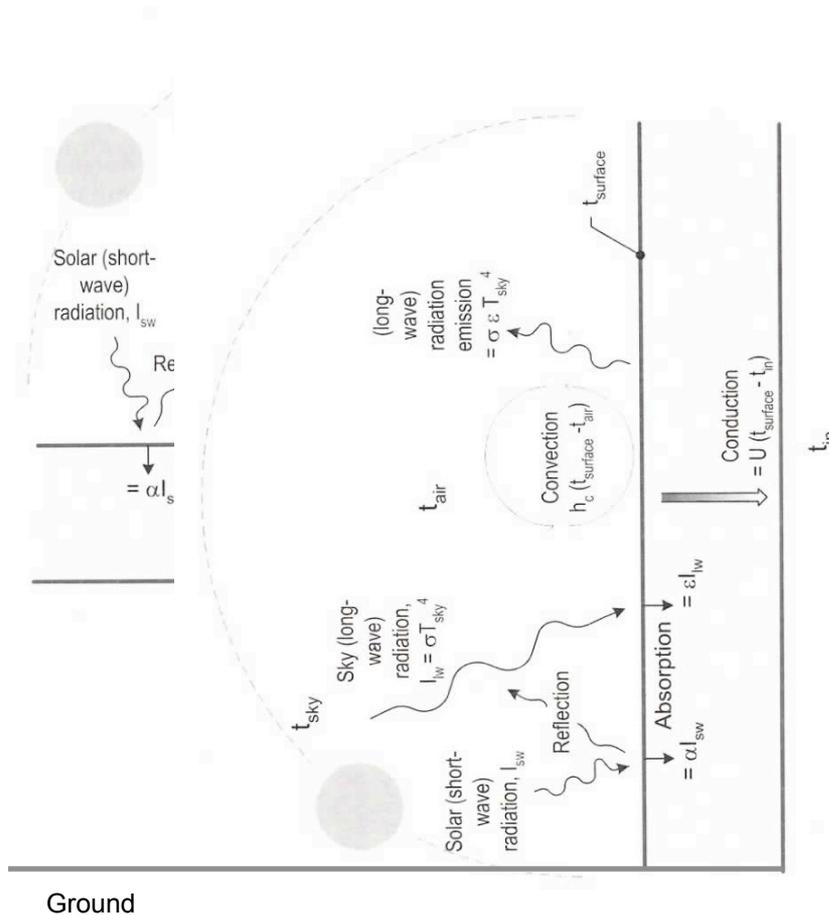


## Wind speed



# Bringing all the modes together (again)

- Back to our energy balance for a vertical surface:



$$q_{solar} + q_{lwr} + q_{conv} - q_{cond} = 0$$

$$\begin{aligned} & \alpha I_{solar} \\ & + \epsilon_{surface} \sigma F_{sky} (T_{sky}^4 - T_{surf}^4) \\ & + \epsilon_{surface} \sigma F_{air} (T_{air}^4 - T_{surface}^4) \\ & + \epsilon_{surface} \sigma F_{ground} (T_{air}^4 - T_{ground}^4) \\ & + h_{conv} (T_{air} - T_{surface}) \\ & - U (T_{surface} - T_{surface,interior}) = 0 \end{aligned}$$

We need to understand conduction through enclosures that are more complex than just single materials

# Next lectures

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- The next 2 lectures are on more complex conduction than we've previously dealt with
  - Realistic layers and assemblies
  - 2D and 3D conduction
  - Thermal bridges
- Tuesday Feb 9 will be a short class (only 1 hour)
  - NAS meeting travel