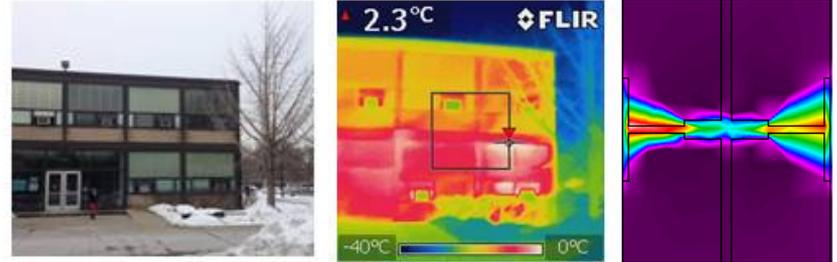


CAE 331/513

Building Science

Fall 2018



October 9, 2018

Psychrometric processes (part 1)

Built
Environment
Research

@ IIT



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Psychrometric equations summary (IP units)

$$pV = nRT$$

$$p = p_{da} + p_w$$

$$pv = \frac{p}{\rho} = RT$$

Humidity ratio:

$$W = 0.622 \frac{p_w}{p - p_w}$$

RH:

$$\phi = \frac{p_w}{p_{ws}} \quad R_i = \frac{R}{MW_i}$$

$$\rho = \frac{m_{da} + m_w}{V} = \frac{1}{v} (1 + W)$$

Air density

Saturation vapor pressure:

$$\ln p_{ws} = \frac{C_8}{T} + C_9 + C_{10}T + C_{11}T^2 + C_{12}T^3 + C_{13} \ln T$$

where

$$C_8 = -1.044\ 039\ 7\ \text{E}+04$$

$$C_9 = -1.129\ 465\ 0\ \text{E}+01$$

$$C_{10} = -2.702\ 235\ 5\ \text{E}-02$$

$$C_{11} = 1.289\ 036\ 0\ \text{E}-05$$

$$C_{12} = -2.478\ 068\ 1\ \text{E}-09$$

$$C_{13} = 6.545\ 967\ 3\ \text{E}+00$$

p_{ws} = saturation pressure, psia

T = absolute temperature, °R = °F + 459.67

Dew point temperature:

Between dew points of 32 to 200°F,

$$t_d = C_{14} + C_{15}\alpha + C_{16}\alpha^2 + C_{17}\alpha^3 + C_{18}(p_w)^{0.1984}$$

Below 32°F,

$$t_d = 90.12 + 26.142\alpha + 0.8927\alpha^2$$

where

t_d = dew-point temperature, °F

$\alpha = \ln p_w$

p_w = water vapor partial pressure, psia

$$C_{14} = 100.45$$

$$C_{15} = 33.193$$

$$C_{16} = 2.319$$

$$C_{17} = 0.17074$$

$$C_{18} = 1.2063$$

Psychrometric equations summary (IP units)

Wet bulb temperature (iterative solver):

$$W = \frac{(1093 - 0.556T_{wb})W_{s@T_{wb}} - 0.240(T - T_{wb})}{1093 + 0.444T - T_{wb}} = \text{actual } W$$

*Where T_{wb} and T are in Fahrenheit

Specific volume:

$$v = \frac{R_{da} T}{P_{da}} = \frac{R_{da} T}{P_{tot} - P_w} = \frac{R_{da} T (1 + 1.6078W)}{P_{tot}}$$

$$v \approx 0.370486(T + 459.67)(1 + 1.6078W) / P_{tot}$$

where

v = specific volume, ft³/lb_{da}
 t = dry-bulb temperature, °F
 W = humidity ratio, lb_w/lb_{da}
 p = total pressure, psia

Specific enthalpy:

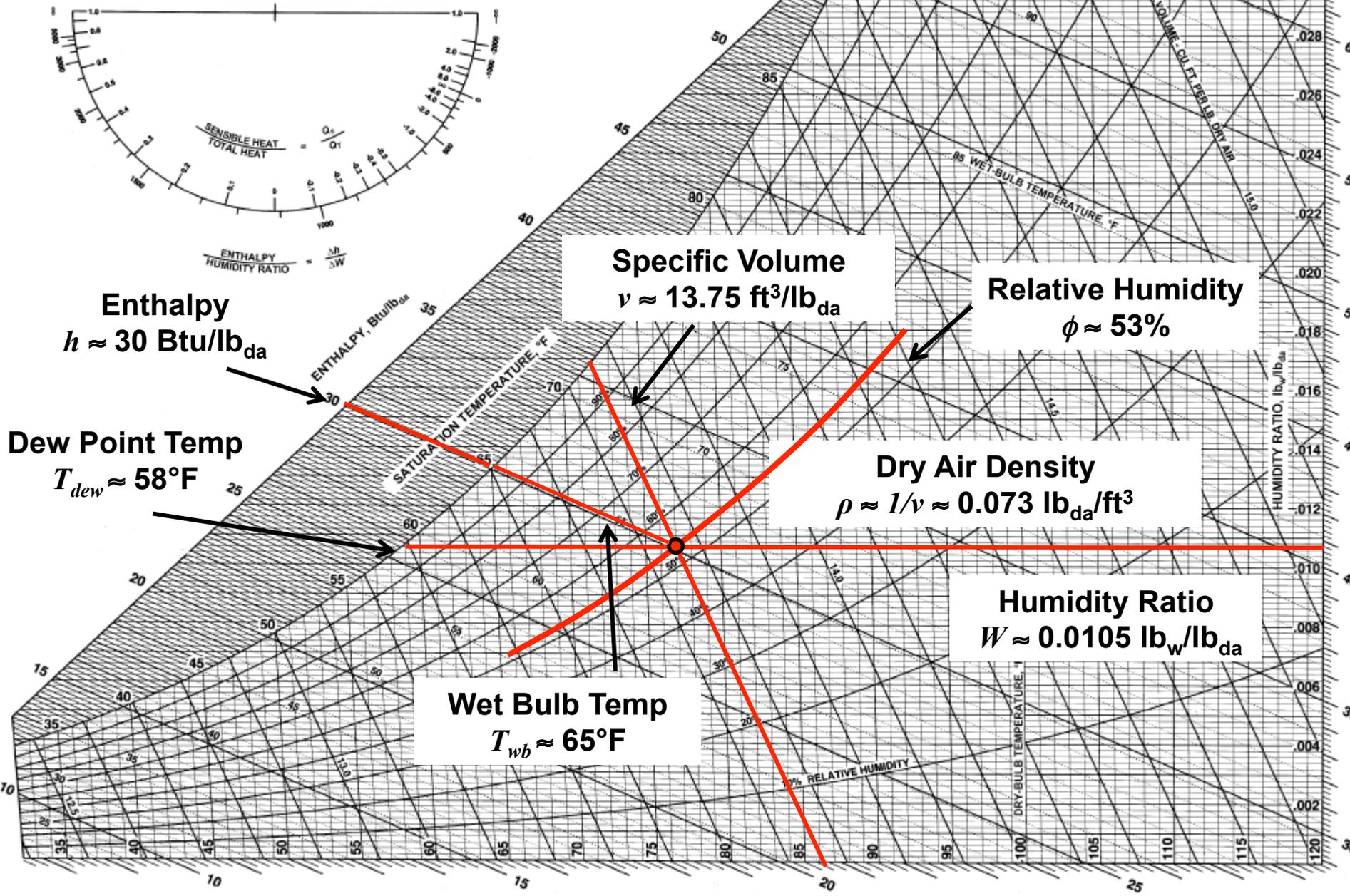
$$h \approx 0.24T + W(1061 + 0.444T)$$

*where T is in °F

Finish state points: Revisit classroom example

- Dry bulb temperature = $25^{\circ}\text{C} = 77^{\circ}\text{F}$
- RH = 53%
- Sea level (14.696 psia)

Find all other relevant parameters using equations



Why is this stuff helpful?

PSYCHROMETRIC PROCESSES

Using the psychrometric chart

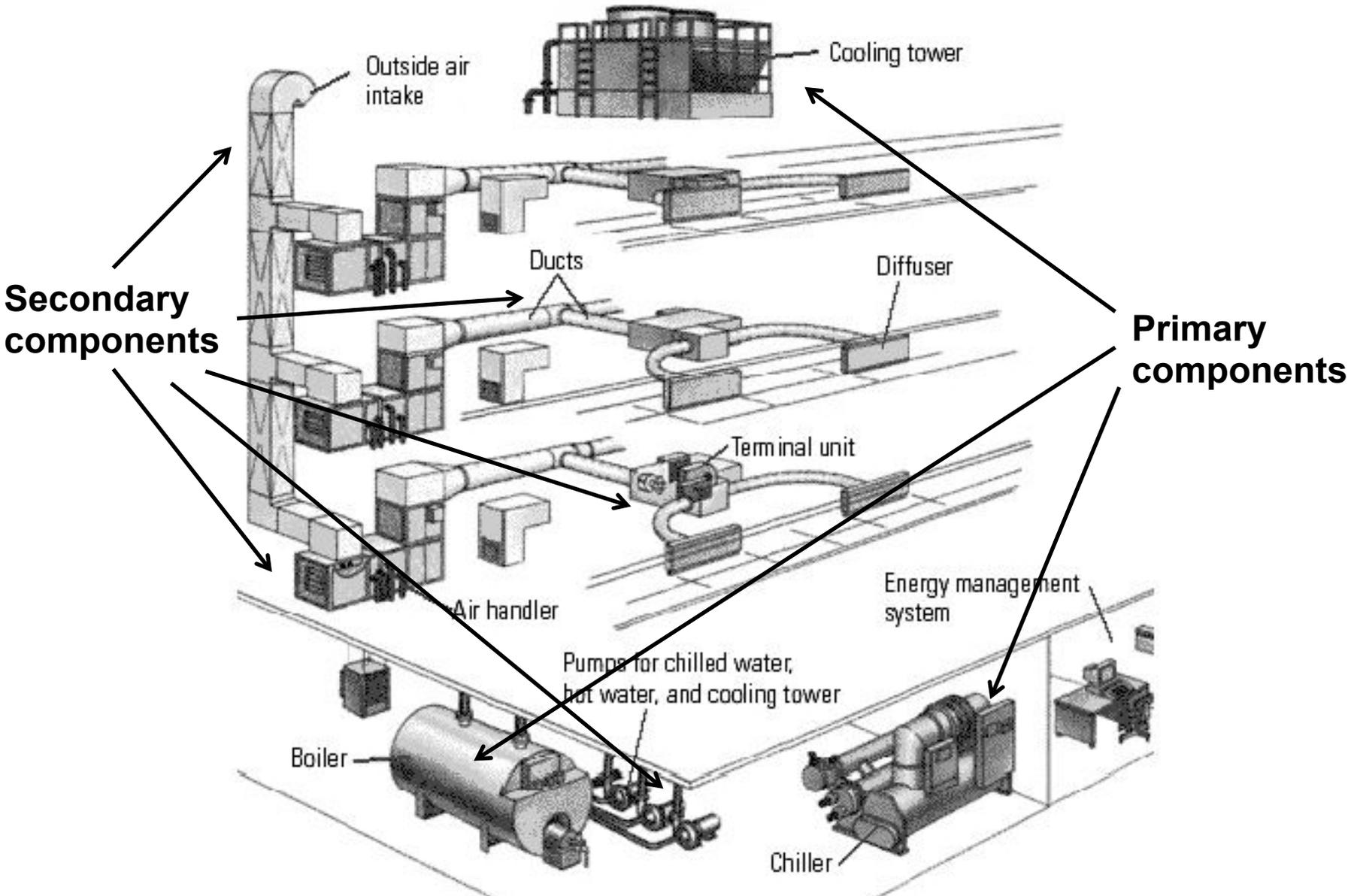
Use of the psychrometric chart for *processes*

We can use the psychrometric chart (and equations) not only to describe states of moist air, but for a number of processes that are important for building science and HVAC applications

Examples:

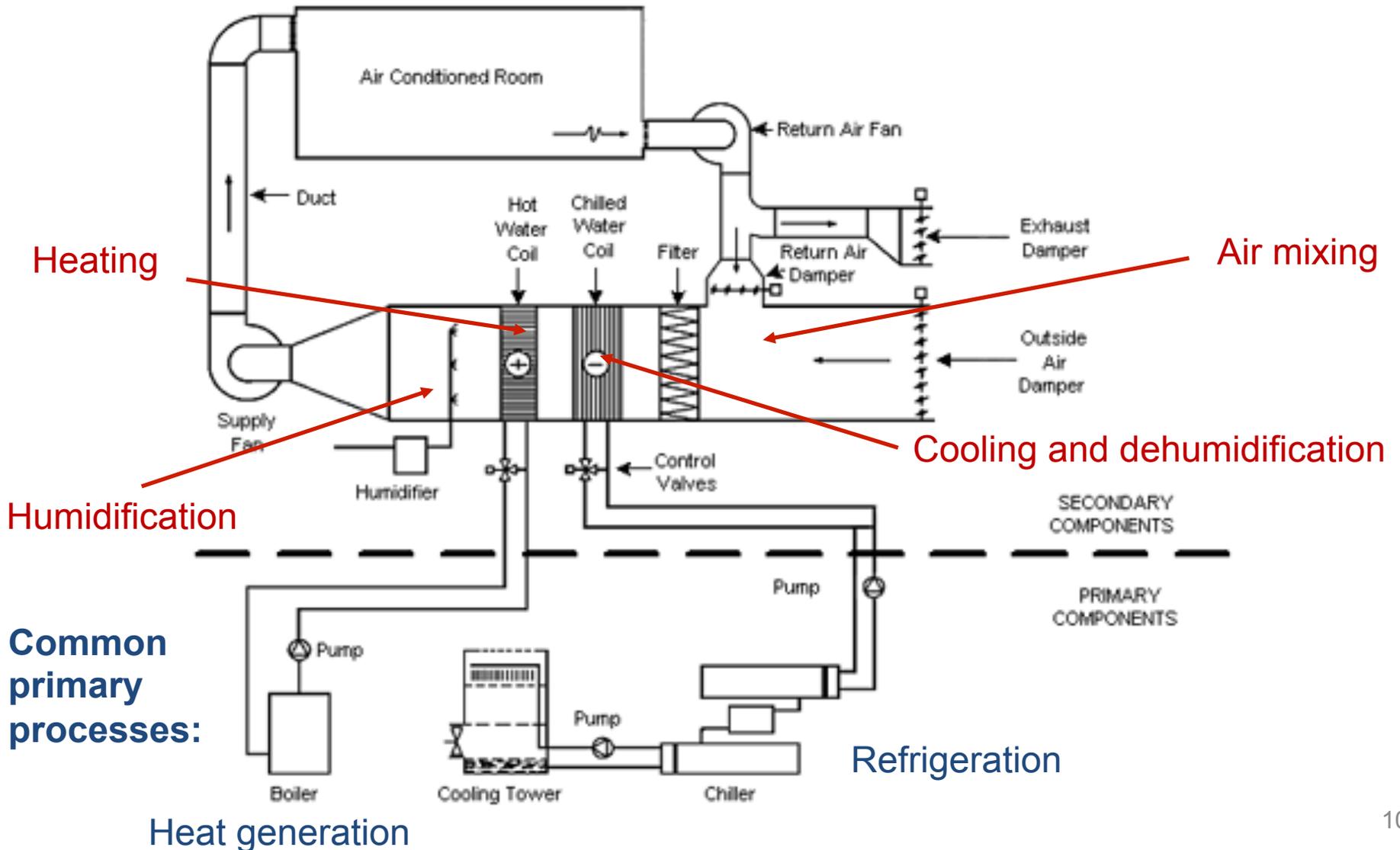
- Sensible cooling or heating
- Warming and humidification of cold, dry air
- Cooling and dehumidification of warm, humid air
 - Sensible + latent cooling
- Evaporative cooling
- Mixing of airstreams

Typical components of an HVAC system



Typical HVAC processes

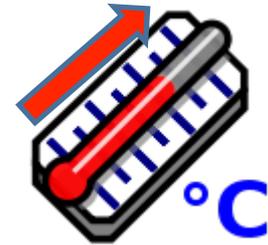
Some common psychrometric processes:



Definitions: Sensible and latent heat

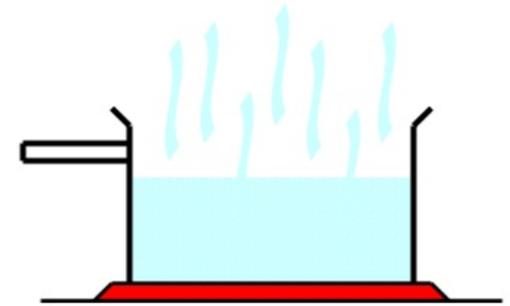
- **Sensible** heat transfer

- Increase or decrease in temperature of a substance *without* undergoing a phase change



- **Latent** heat transfer

- Heat transfer required to change the phase of a substance (e.g., heat required to change liquid to vapor)



$$Q_{total} = Q_{sensible} + Q_{latent}$$

Units of [W], [BTU/hr], or [ton]

Sensible and latent heat transfer equation

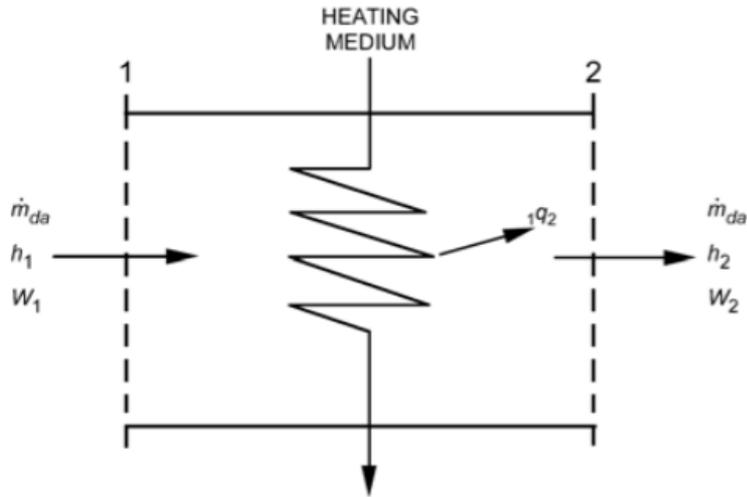


Fig. 2 Schematic of Device for Heating Moist Air

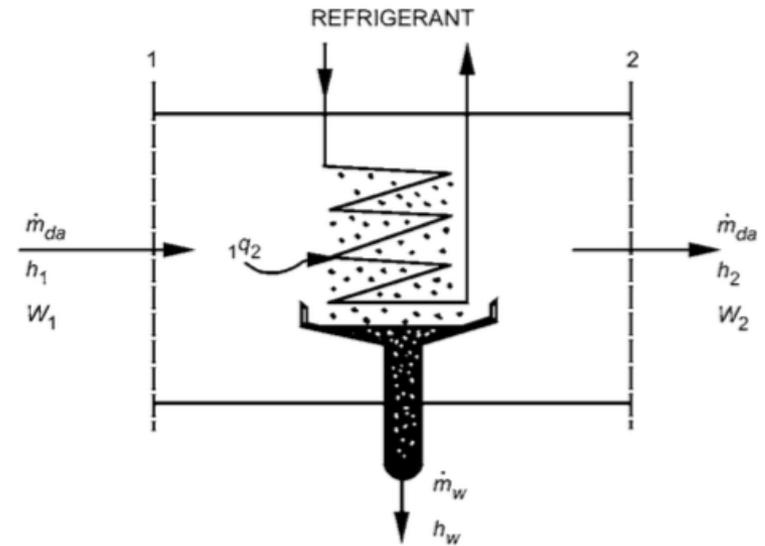


Fig. 3 Schematic of Device for Cooling Moist Air

Generic equations for both heating and cooling processes:

$$Q_{1 \rightarrow 2} = \dot{m}_{da} (h_2 - h_1) \quad Q_{total} = \dot{m}_{da} (h_{exit} - h_{inlet})$$

$Q_{1 \rightarrow 2}$ = total rate of heat transfer from state 1 to state 2 (W or BTU/hr [or ton])

\dot{m}_{da} = mass flow rate of dry air (kg_{da}/s or lb_{da}/hr)

$h_{exit,2}$ = enthalpy at the exit (J/kg_{da} or BTU/lb_{da})

$h_{inlet,1}$ = enthalpy at the inlet (J/kg_{da} or BTU/lb_{da})

Sensible heat transfer equation

$$Q_{sensible} = \dot{m}_{da} C_p (T_{exit} - T_{inlet}) = \rho_{da} \dot{V}_{da} C_p (T_{exit} - T_{inlet})$$

$Q_{sensible}$ = rate of sensible heat transfer (W or BTU/hr [or ton])

C_p = specific heat of air (J/kgK or BTU/lb°F)

ρ_{da} = dry air density (kg_{da}/m³ or lb_{da}/ft³)

T_{inlet} = inlet temperature (K or °F)

T_{exit} = exit temperature (K or °F)

For heating: $Q_{sensible} > 0$

For cooling: $Q_{sensible} < 0$



Latent heat transfer equation

$$Q_{latent} = \dot{m}_{da} h_{fg} (W_{exit} - W_{inlet}) = \rho_{da} \dot{V}_{da} h_{fg} (W_{exit} - W_{inlet})$$

Q_{latent} = rate of latent heat transfer (W or BTU/hr [or ton])

m_w = mass flow rate of water vapor (kg_w/s or lb_w/hr)

h_{fg} = enthalpy, or latent heat, of vaporization (J/kg or BTU/lb)

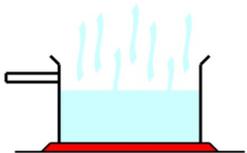
* h_{fg} = 2260 kJ/kg or 970 BTU/lb for water at 212°F (i.e., steam)

W_{inlet} = inlet humidity ratio (kg_w/kg_{da} or lb_w/lb_{da})

W_{exit} = exit humidity ratio (kg_w/kg_{da} or lb_w/lb_{da})

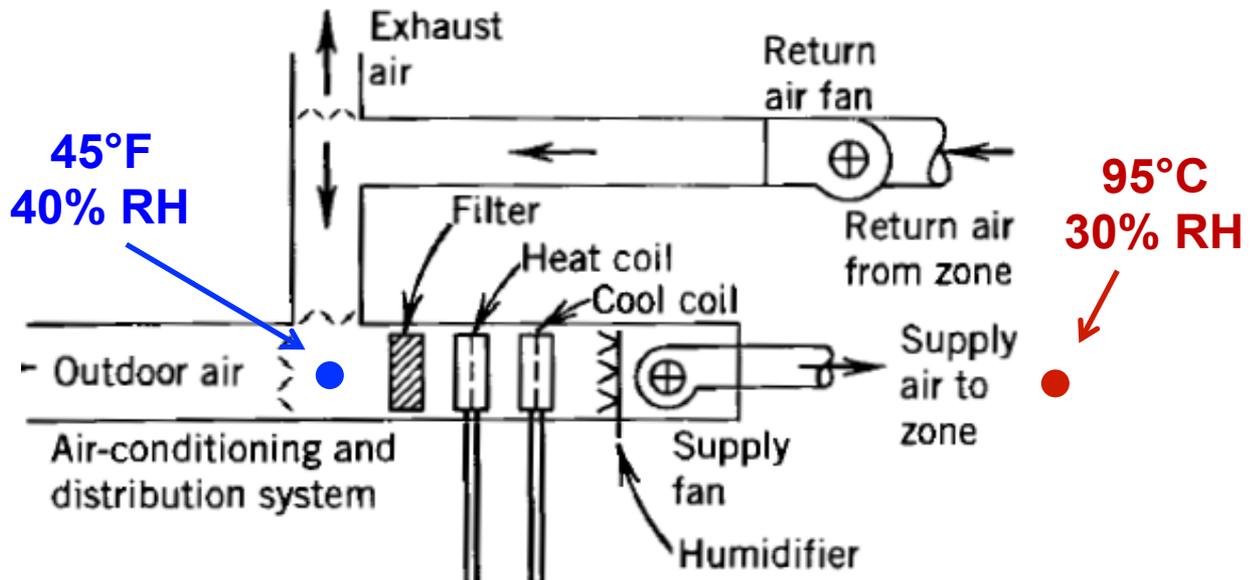
For humidification: $Q_{latent} > 0$

For dehumidification: $Q_{latent} < 0$



Heating and humidification of cold, dry air

- **Example:** Heating and humidification of air
 - Process: Adding moisture and heat (sensible + latent heating)

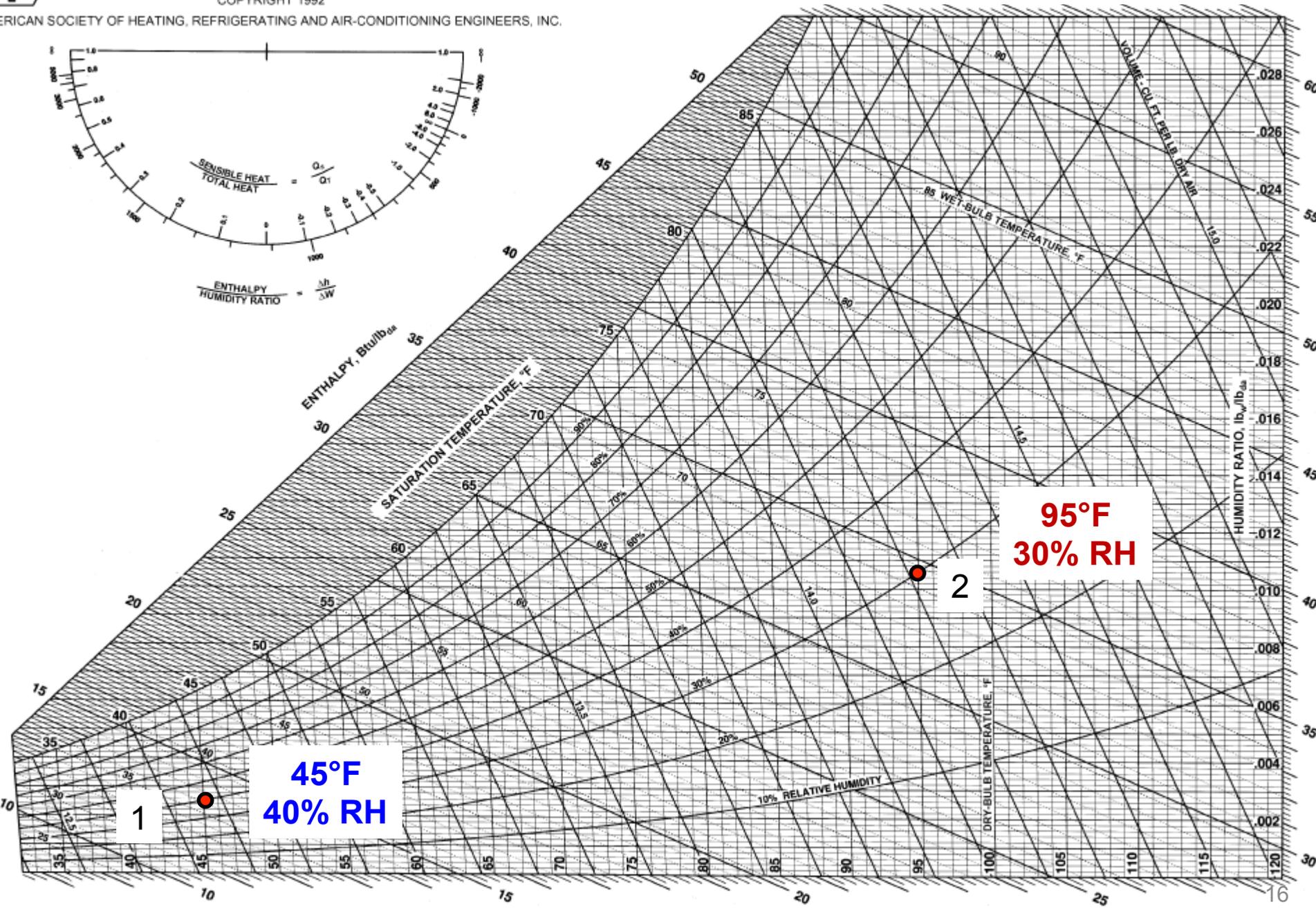


Q1: What is the enthalpy change required?

Q2: What is the total rate of heat transfer if the airflow rate is 10000 cfm?

Q3: What is the split between sensible and latent transfer?

Heating and humidification of cold, dry air



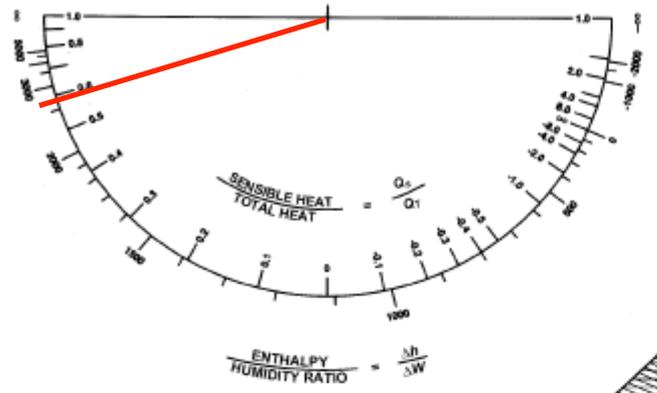
1

45°F
40% RH

2

95°F
30% RH

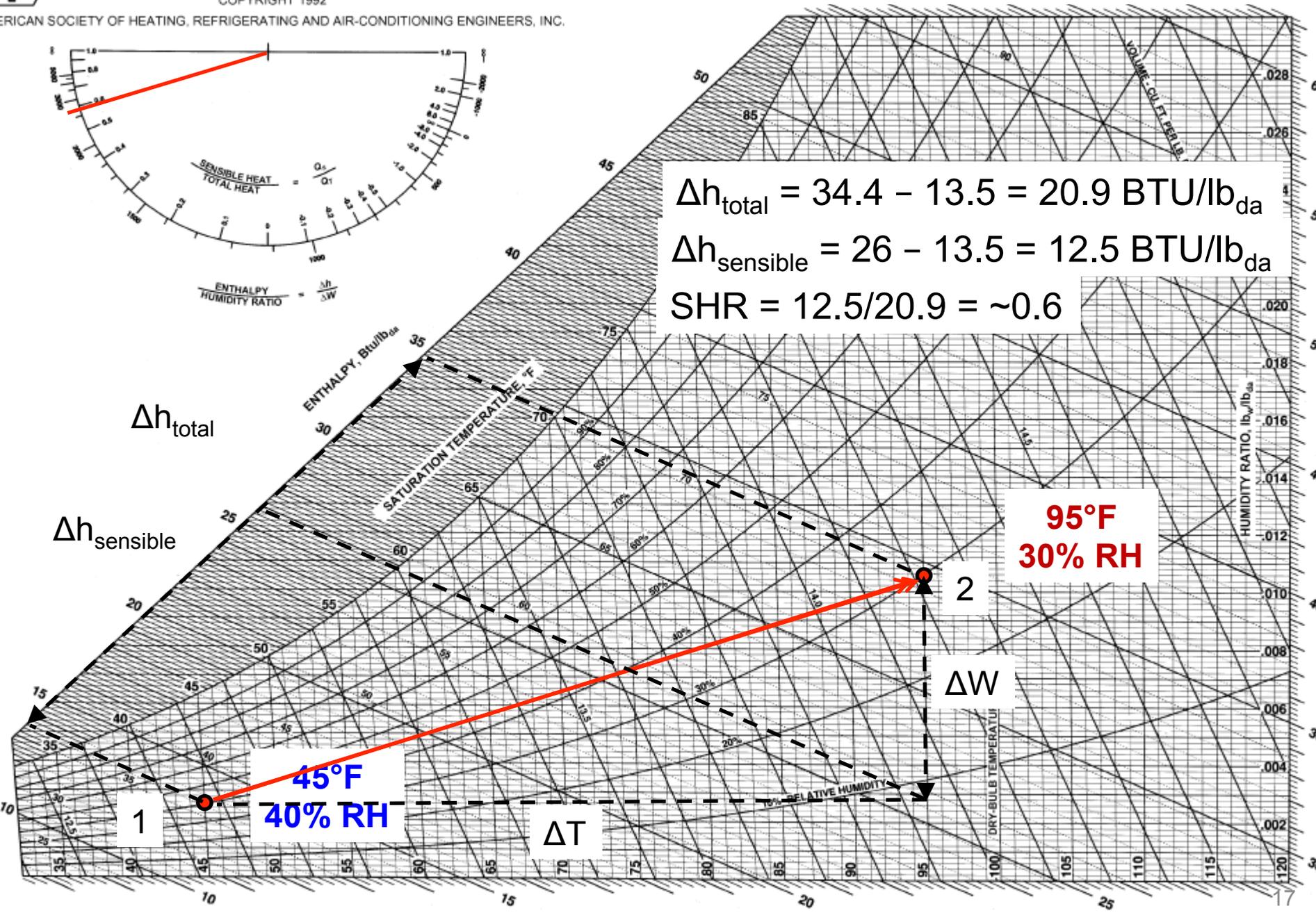
Heating and humidification of cold, dry air



$$\Delta h_{\text{total}} = 34.4 - 13.5 = 20.9 \text{ BTU/lb}_{\text{da}}$$

$$\Delta h_{\text{sensible}} = 26 - 13.5 = 12.5 \text{ BTU/lb}_{\text{da}}$$

$$\text{SHR} = 12.5/20.9 = \sim 0.6$$



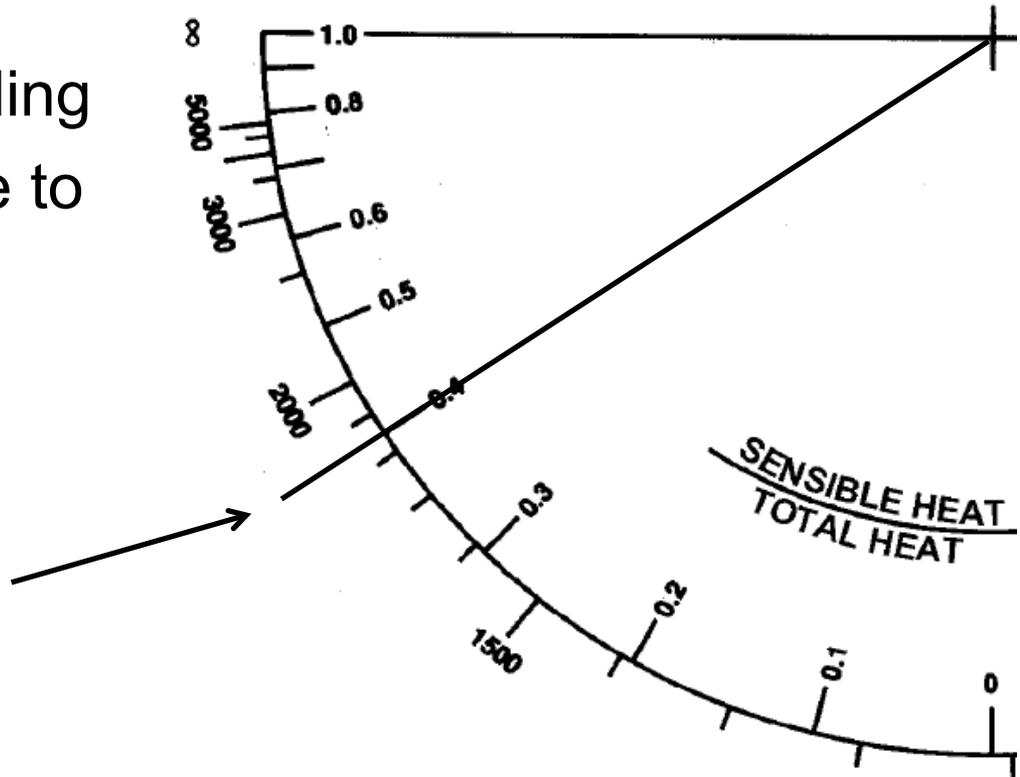
Sensible heat ratio (SHR)

- The sensible heat ratio is defined as:

$$SHR = \frac{\dot{q}_{sens}}{\dot{q}_{total}} = \frac{\dot{q}_{sens}}{\dot{q}_{sens} + \dot{q}_{latent}} = \frac{\Delta h_{sens}}{\Delta h_{total}}$$

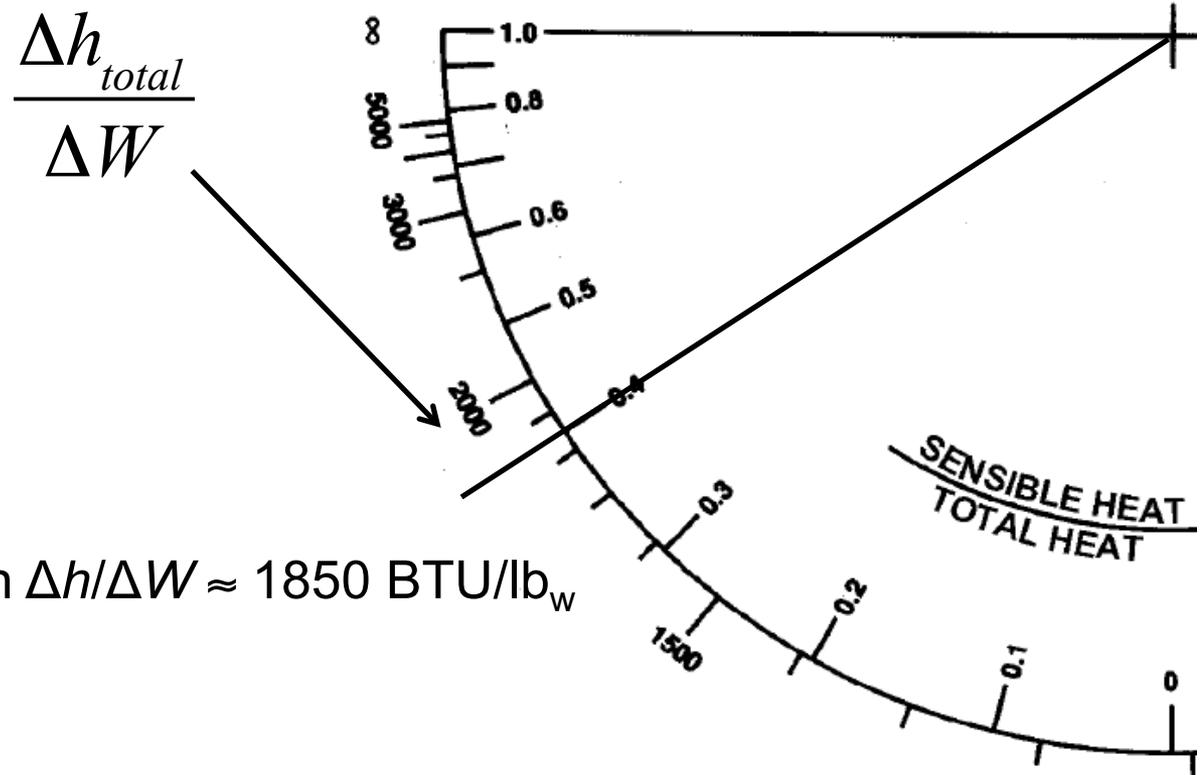
- Allows for understanding sensible load relative to latent load

Here is a process with an SHR ≈ 0.4



Enthalpy protractor ($\Delta h/\Delta W$)

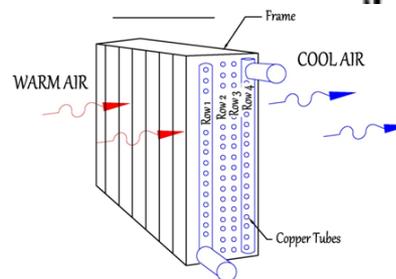
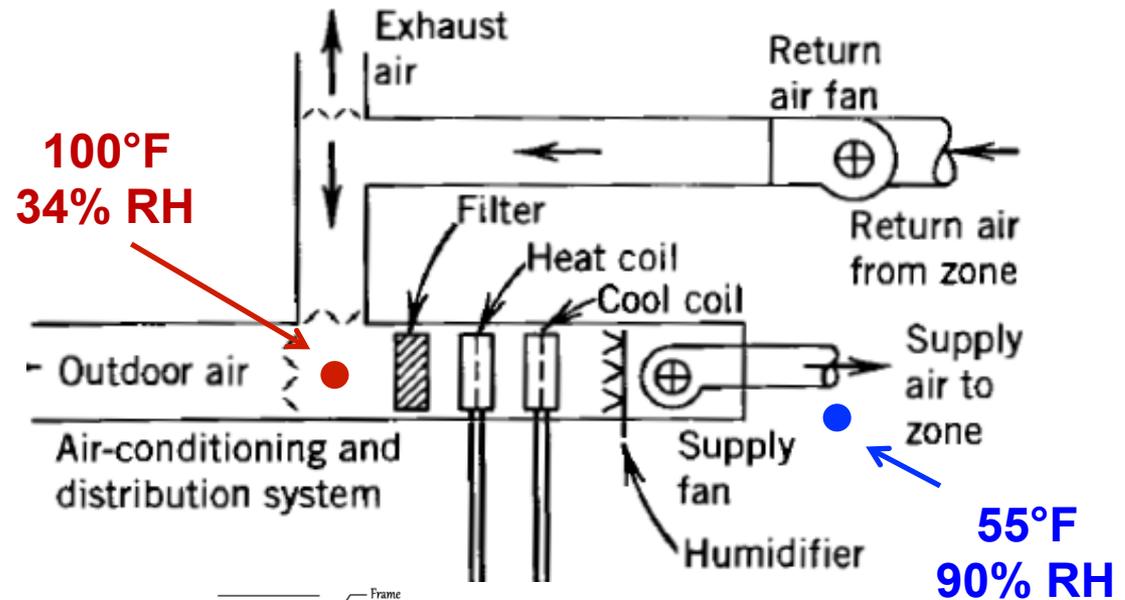
- The other side of the enthalpy protractor tells us:
 - What is the enthalpy change relative to the change in humidity ratio



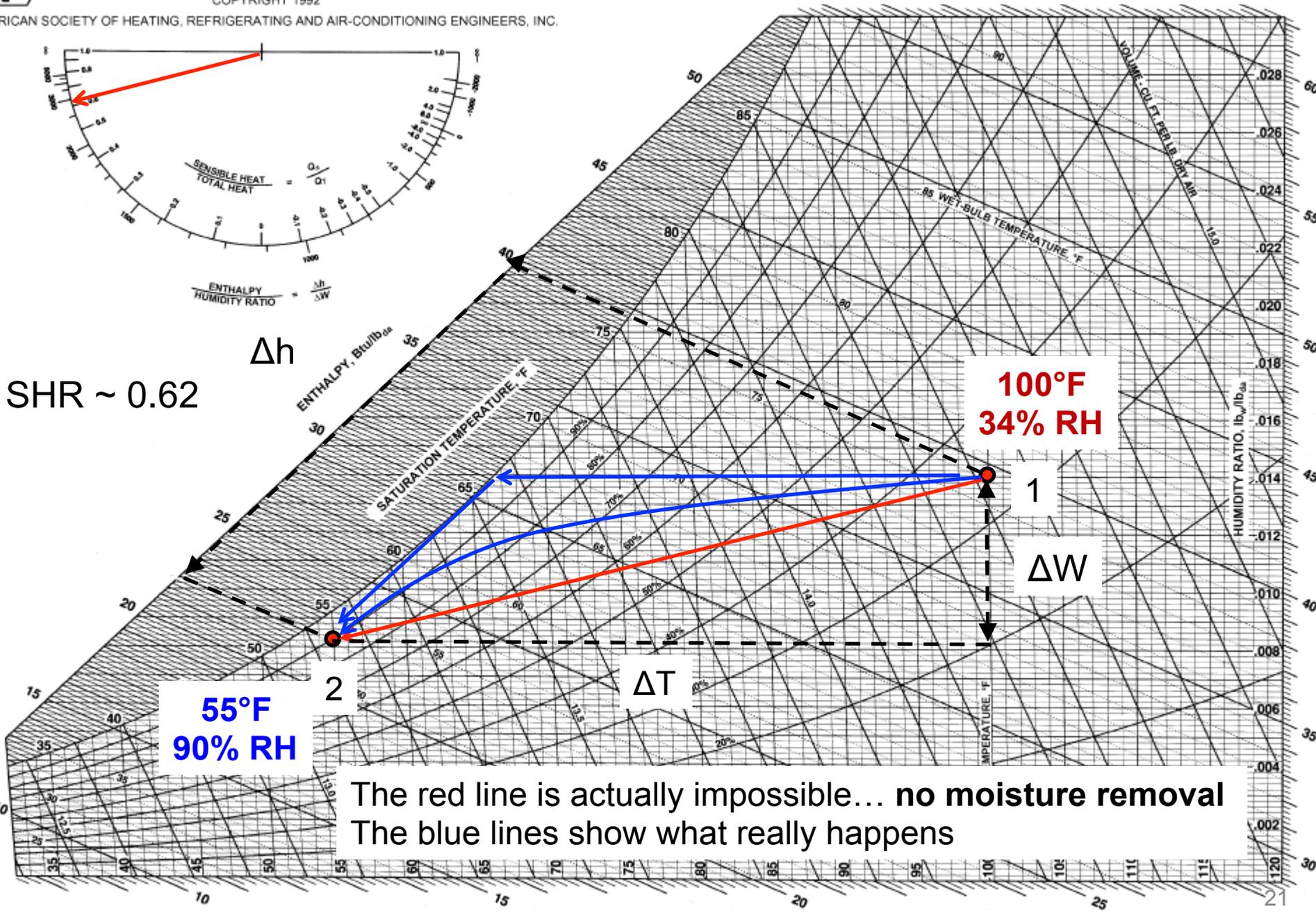
Here is a process with $\Delta h/\Delta W \approx 1850$ BTU/lb_w
SI units: kJ/kg_w

Cooling and dehumidification of **warm**, humid air

- **Example:** Air flowing over a cooling coil
- Removing both moisture and heat
 - Sensible + latent **cooling**



Cooling and dehumidification of warm, humid air



The red line is actually impossible... no moisture removal
The blue lines show what really happens

Example: *Sensible* cooling

- Moist air is cooled from 40°C and 30% RH to 30°C without condensation
 - What is the RH at W at the process end point?



ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

SEA LEVEL

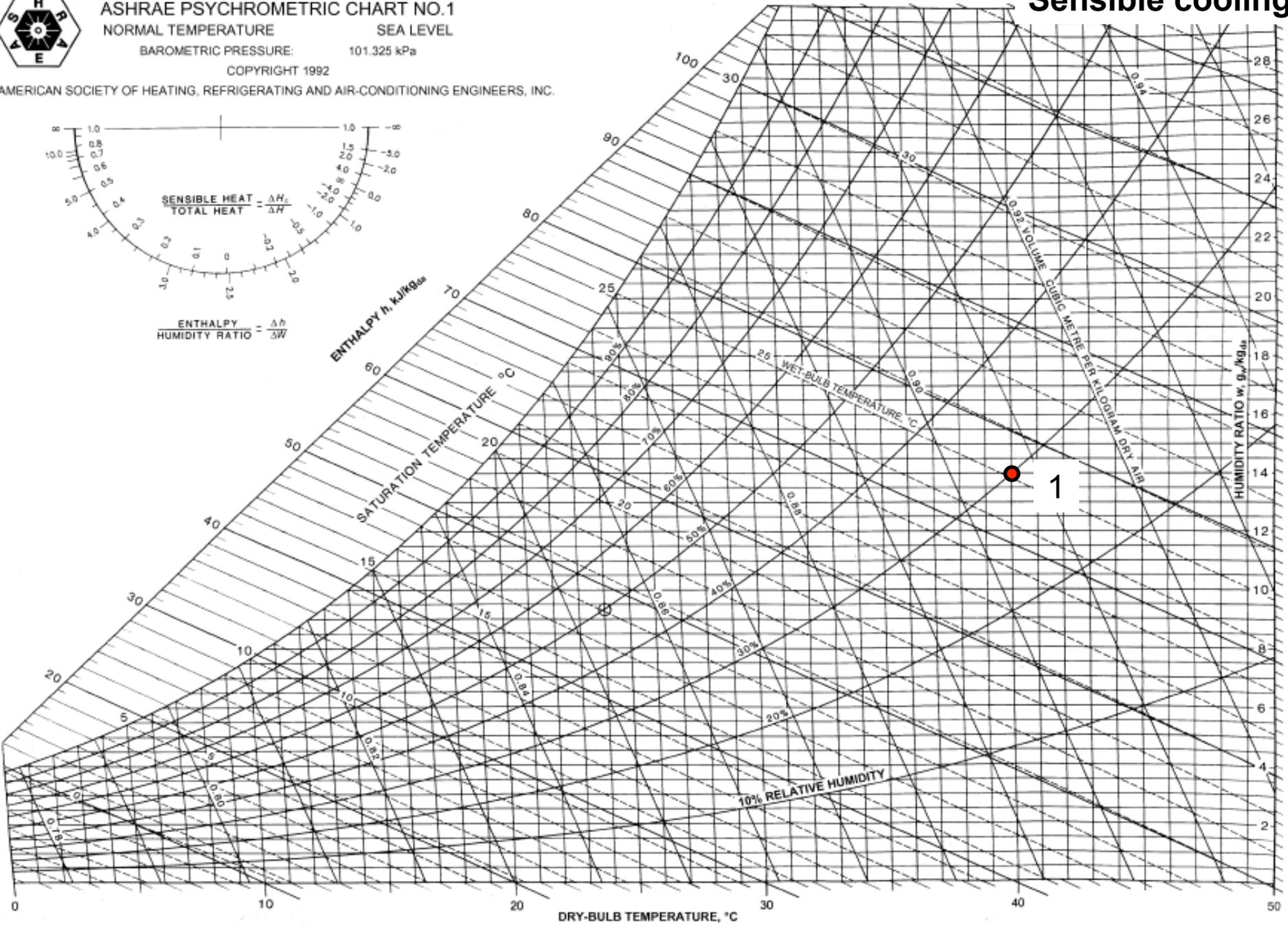
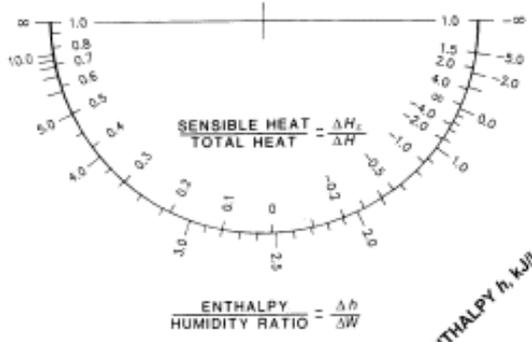
BAROMETRIC PRESSURE:

101.325 kPa

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Sensible cooling

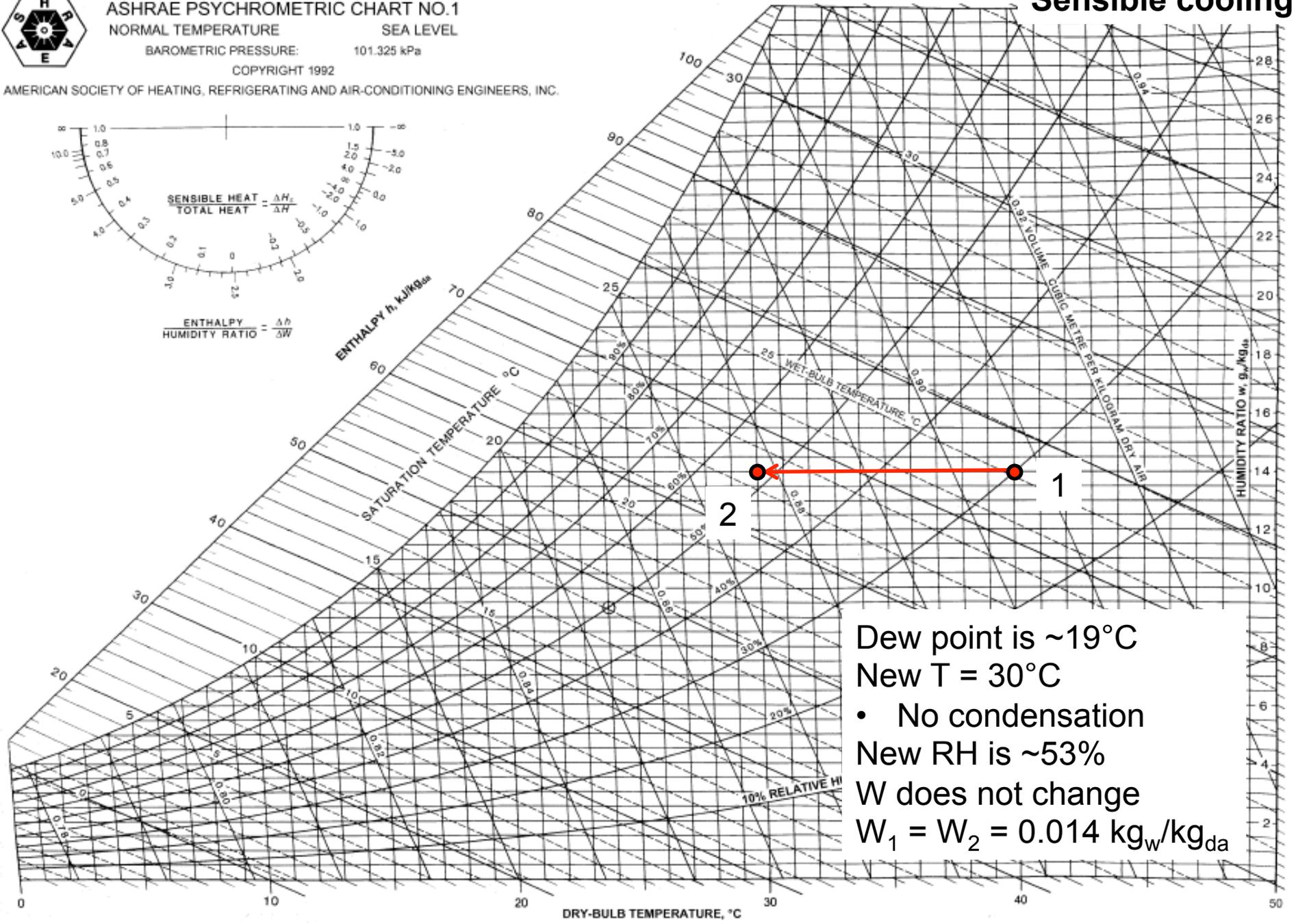
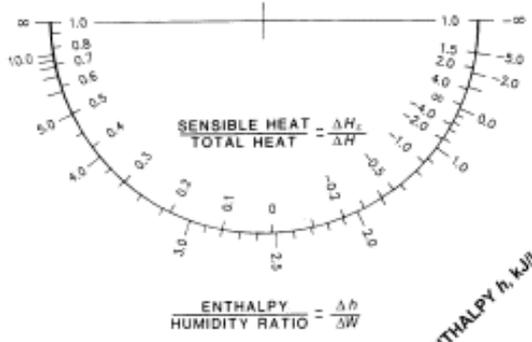




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 NORMAL TEMPERATURE SEA LEVEL
 BAROMETRIC PRESSURE: 101.325 kPa
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Sensible cooling

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Dew point is ~19°C
 New T = 30°C

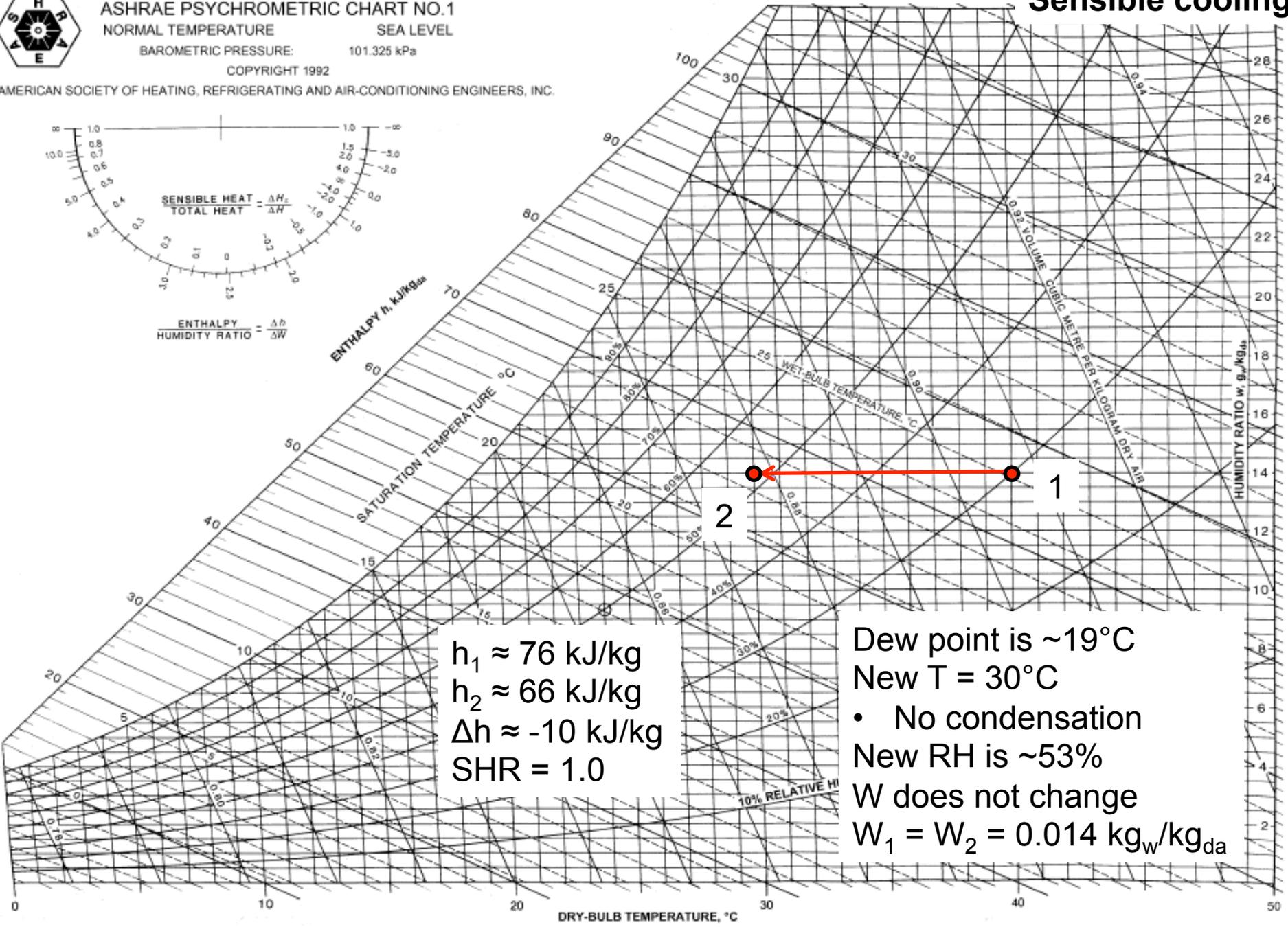
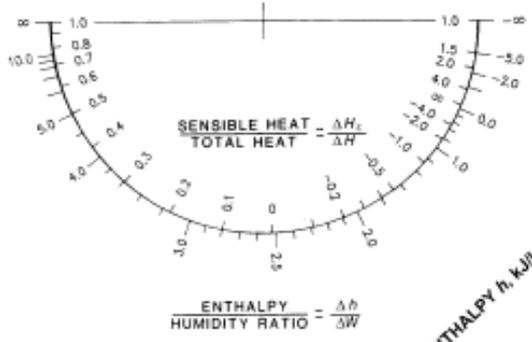
- No condensation
- New RH is ~53%
- W does not change
- $W_1 = W_2 = 0.014 \text{ kg}_w/\text{kg}_{da}$



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 NORMAL TEMPERATURE
 SEA LEVEL
 BAROMETRIC PRESSURE: 101.325 kPa
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Sensible cooling

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$h_1 \approx 76 \text{ kJ/kg}$
 $h_2 \approx 66 \text{ kJ/kg}$
 $\Delta h \approx -10 \text{ kJ/kg}$
 $\text{SHR} = 1.0$

Dew point is $\sim 19^\circ\text{C}$
 New $T = 30^\circ\text{C}$
 • No condensation
 New RH is $\sim 53\%$
 W does not change
 $W_1 = W_2 = 0.014 \text{ kg}_w/\text{kg}_{da}$

Example: *Sensible + latent cooling*

- Moist air is cooled from 40°C and 30% RH to 15°C
 - Q1: Does the water vapor condense?
 - Q2: What is RH at W at the process end point?



ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

SEA LEVEL

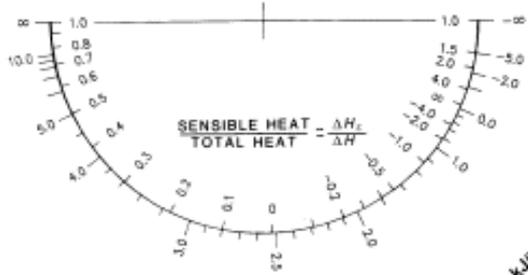
BAROMETRIC PRESSURE:

101.325 kPa

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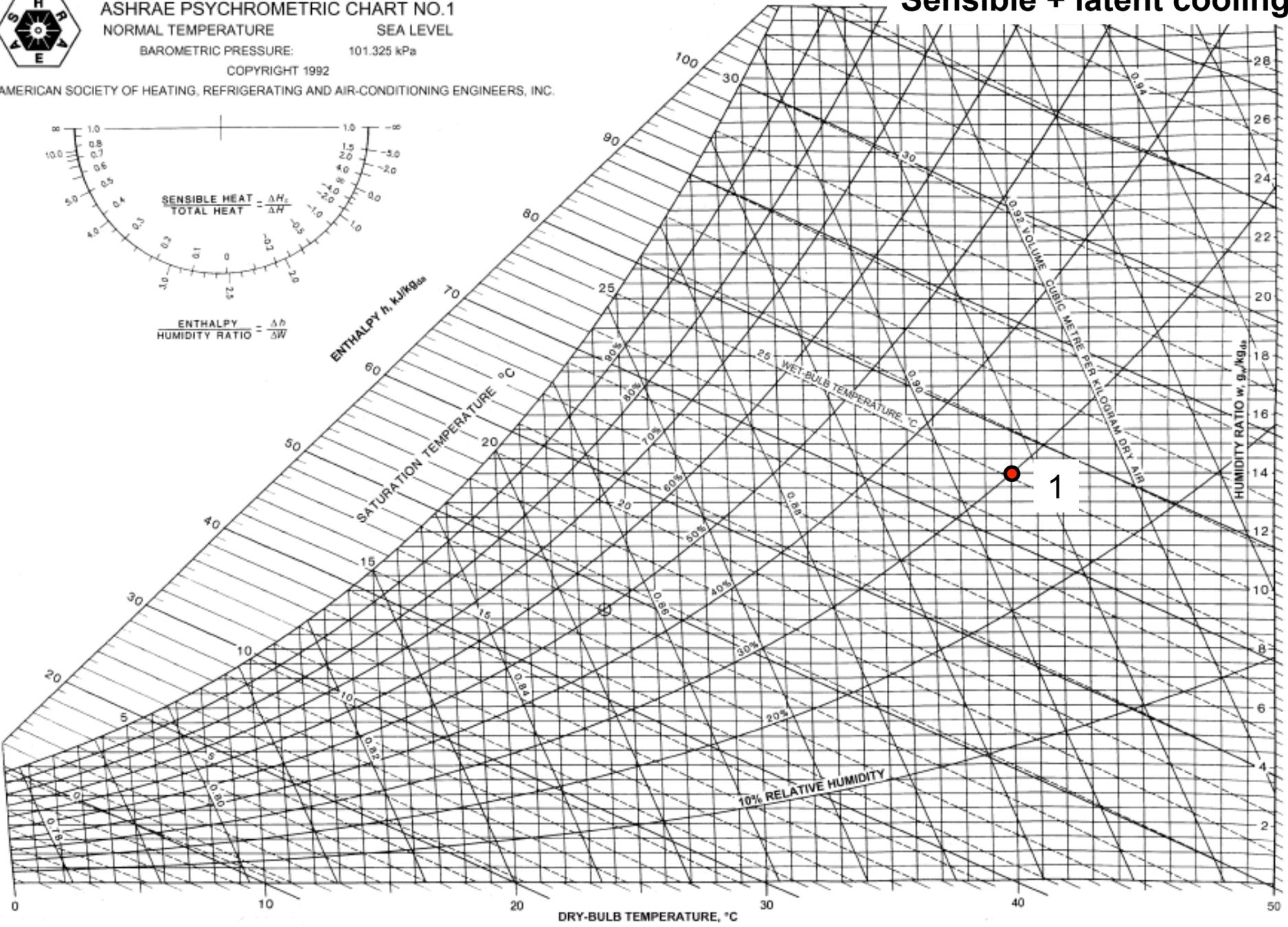
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Sensible + latent cooling



$$\frac{\text{SENSIBLE HEAT}}{\text{TOTAL HEAT}} = \frac{\Delta H_s}{\Delta H}$$

$$\frac{\text{ENTHALPY}}{\text{HUMIDITY RATIO}} = \frac{\Delta h}{\Delta W}$$

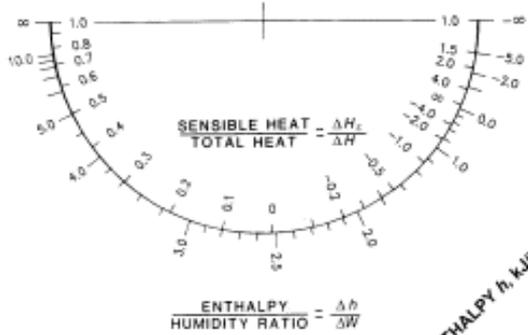




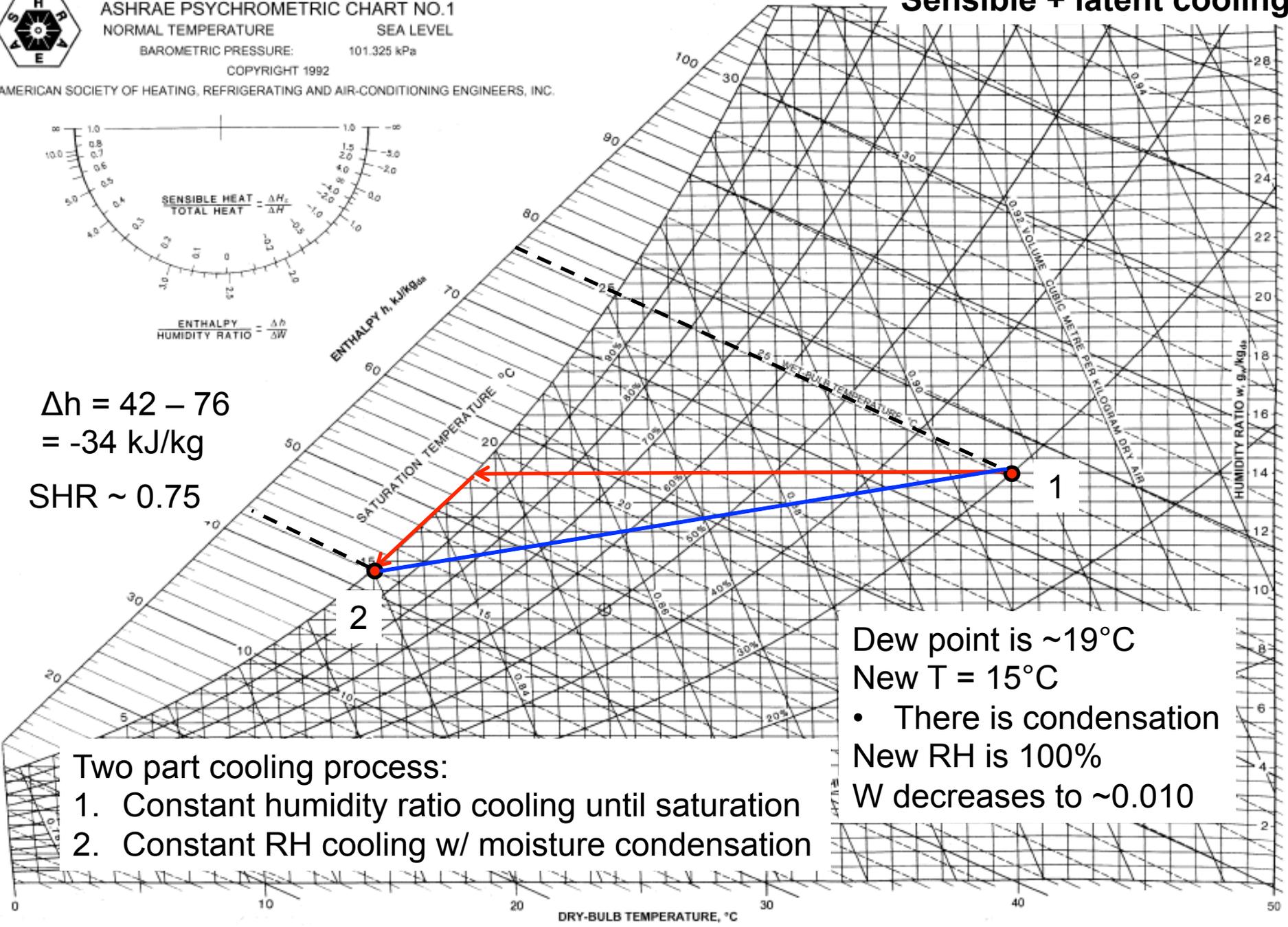
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 SEA LEVEL
 BAROMETRIC PRESSURE: 101.325 kPa
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Sensible + latent cooling

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$\Delta h = 42 - 76$
 $= -34 \text{ kJ/kg}$
 SHR ~ 0.75



Dew point is $\sim 19^\circ\text{C}$
 New $T = 15^\circ\text{C}$
 • There is condensation
 New RH is 100%
 W decreases to ~ 0.010

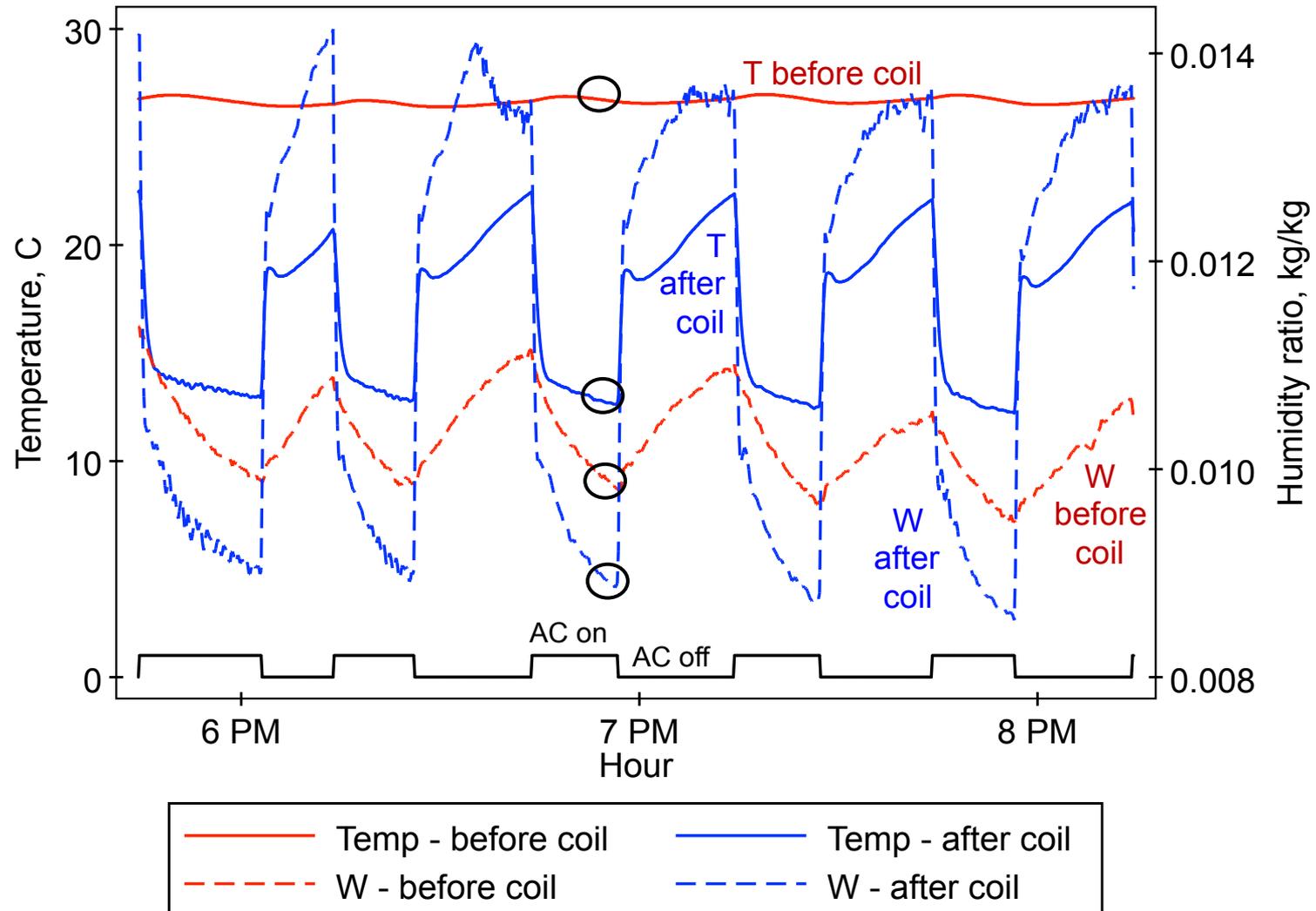
- Two part cooling process:
1. Constant humidity ratio cooling until saturation
 2. Constant RH cooling w/ moisture condensation

DRY-BULB TEMPERATURE, °C

Real data: ASHRAE RP-1299

Energy implications of filters

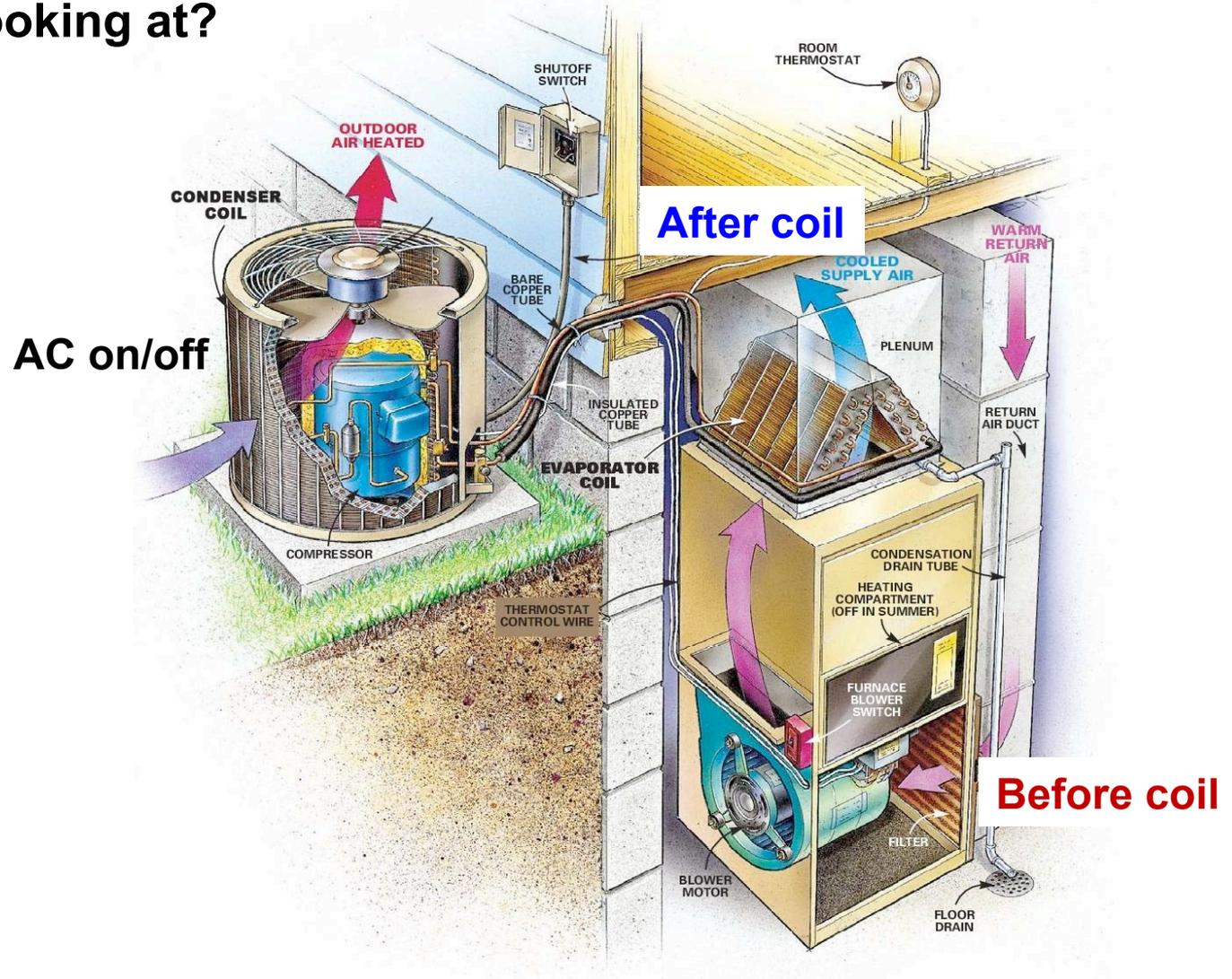
Temperature and humidity ratio differences across AC coils in homes



Real data: ASHRAE RP-1299

Energy implications of filters

What are we looking at?

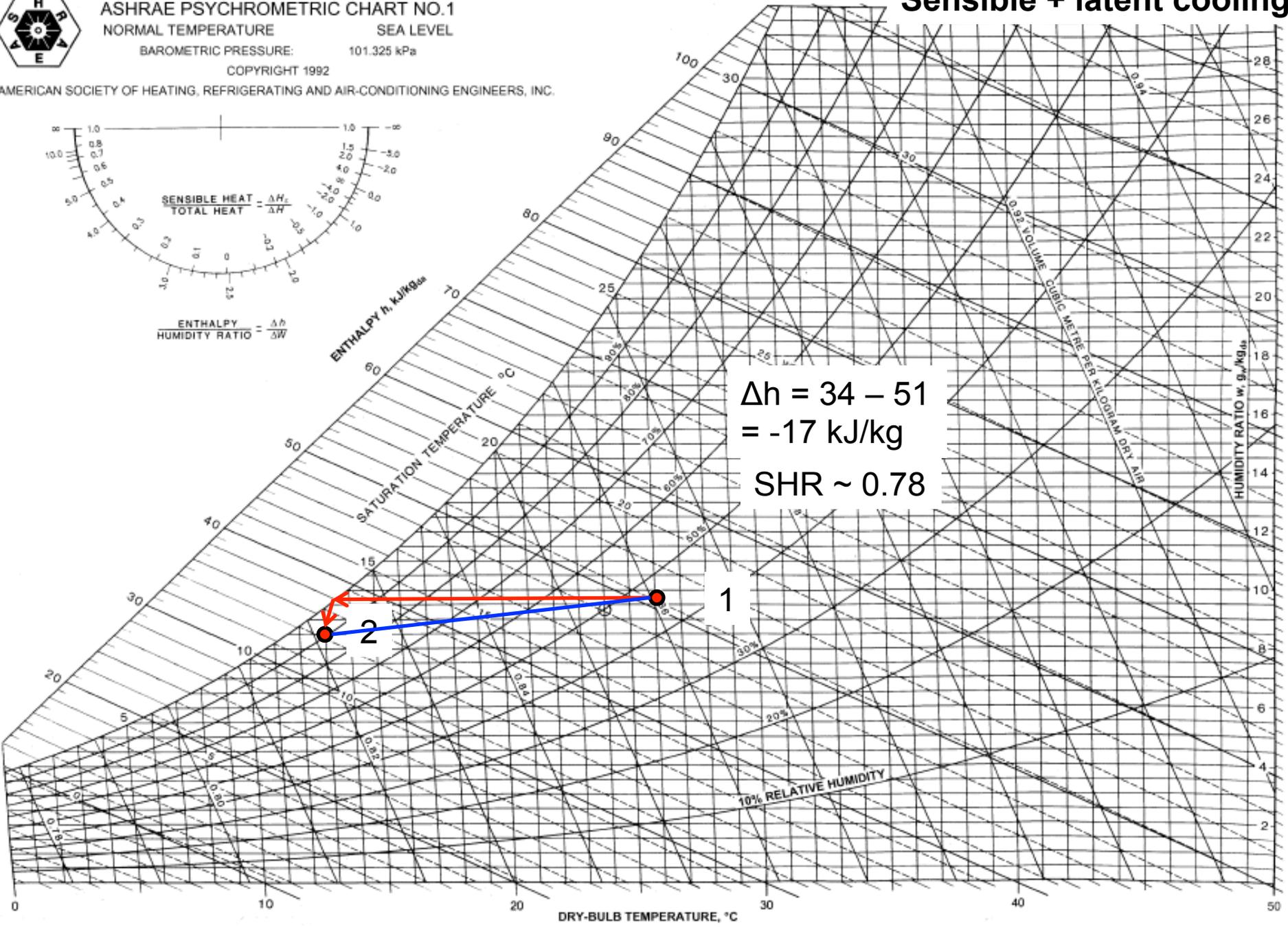
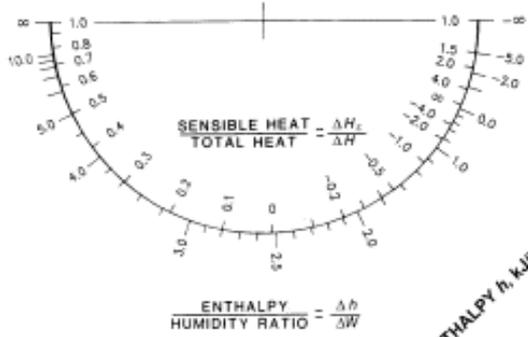




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Sensible + latent cooling

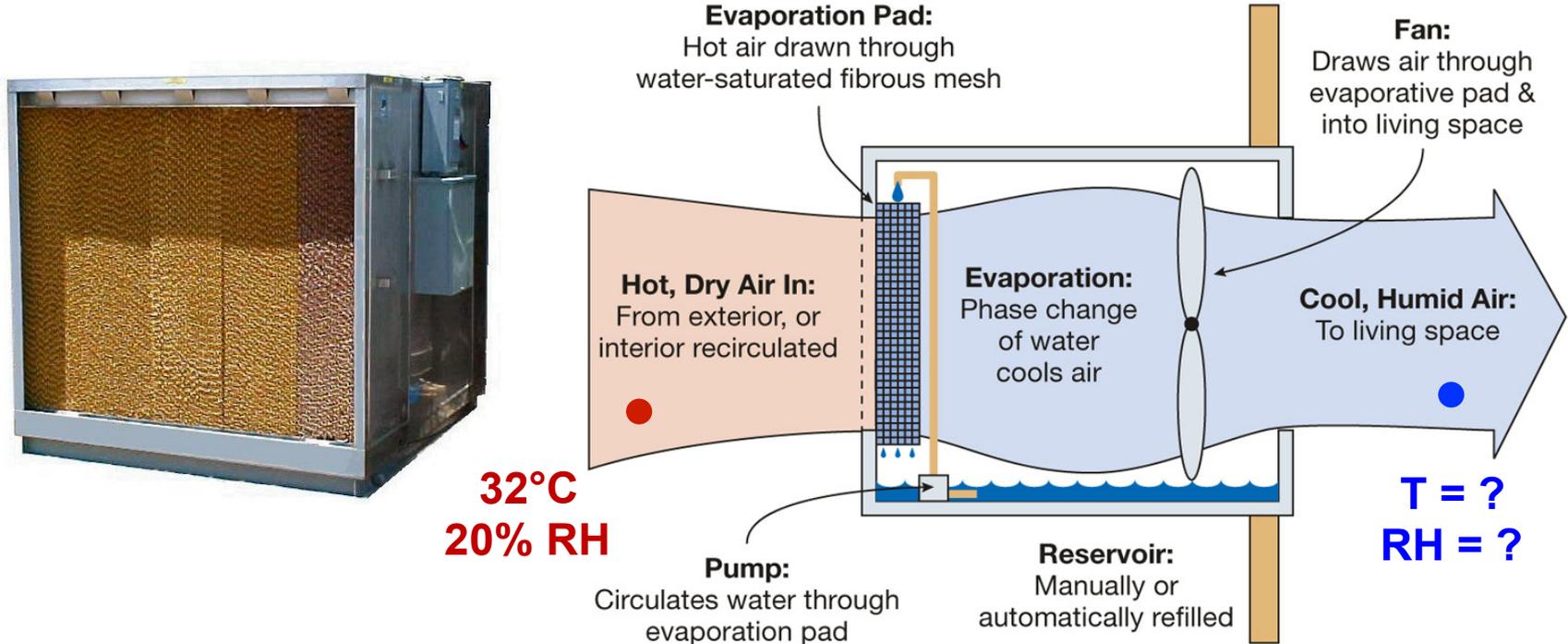
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$\Delta h = 34 - 51$
 $= -17 \text{ kJ/kg}$
 SHR ~ 0.78

Evaporative cooling example

- Hot, dry outdoor air is cooled with an evaporative cooler, or “swamp cooler”
 - Q1: What is the T, RH, and W of the supply air?
 - Q2: Why would we choose this system?

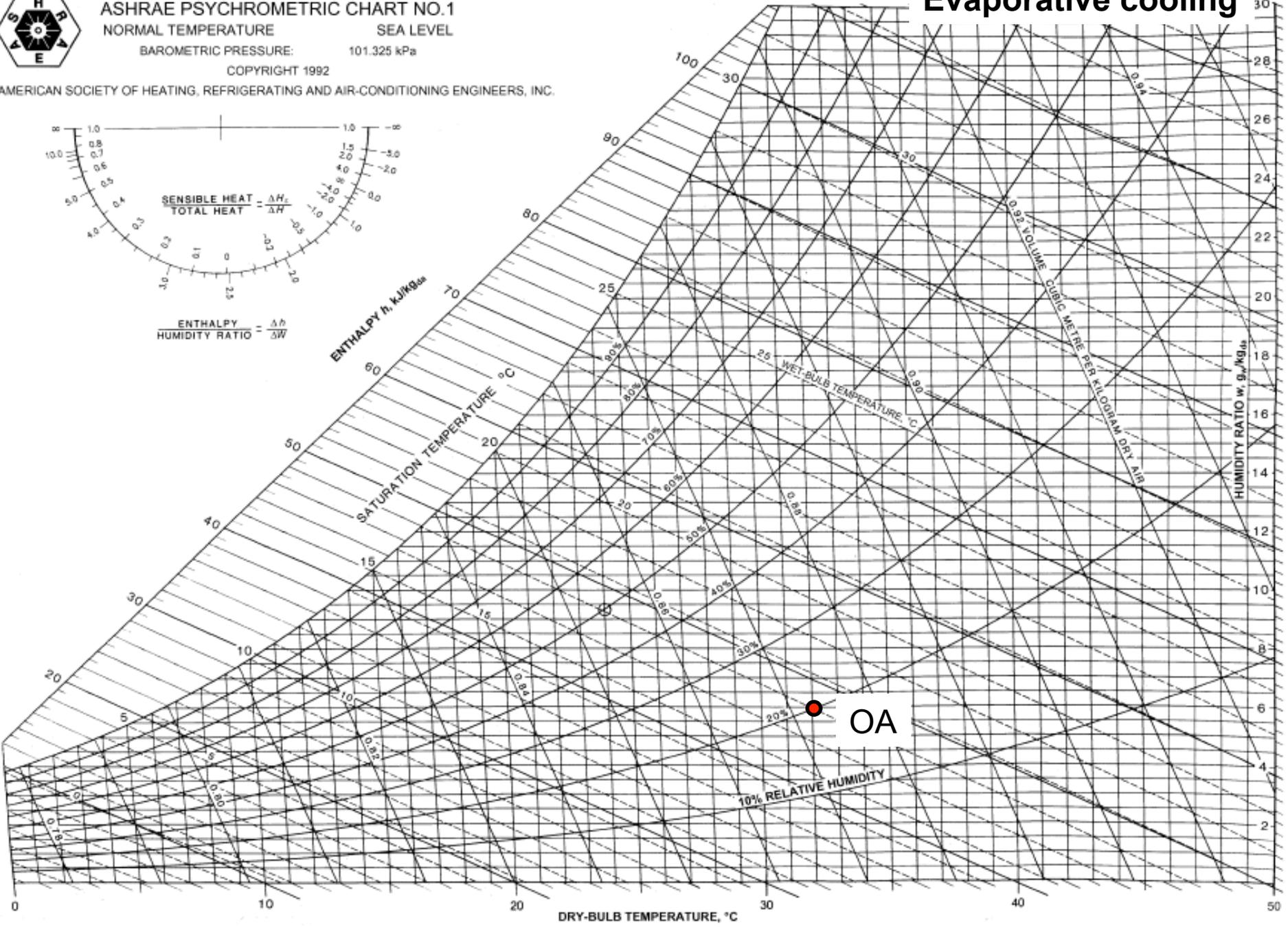
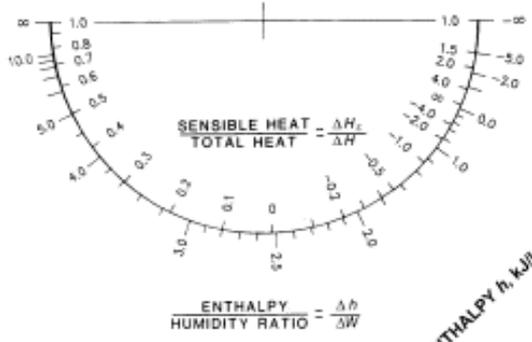




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Evaporative cooling

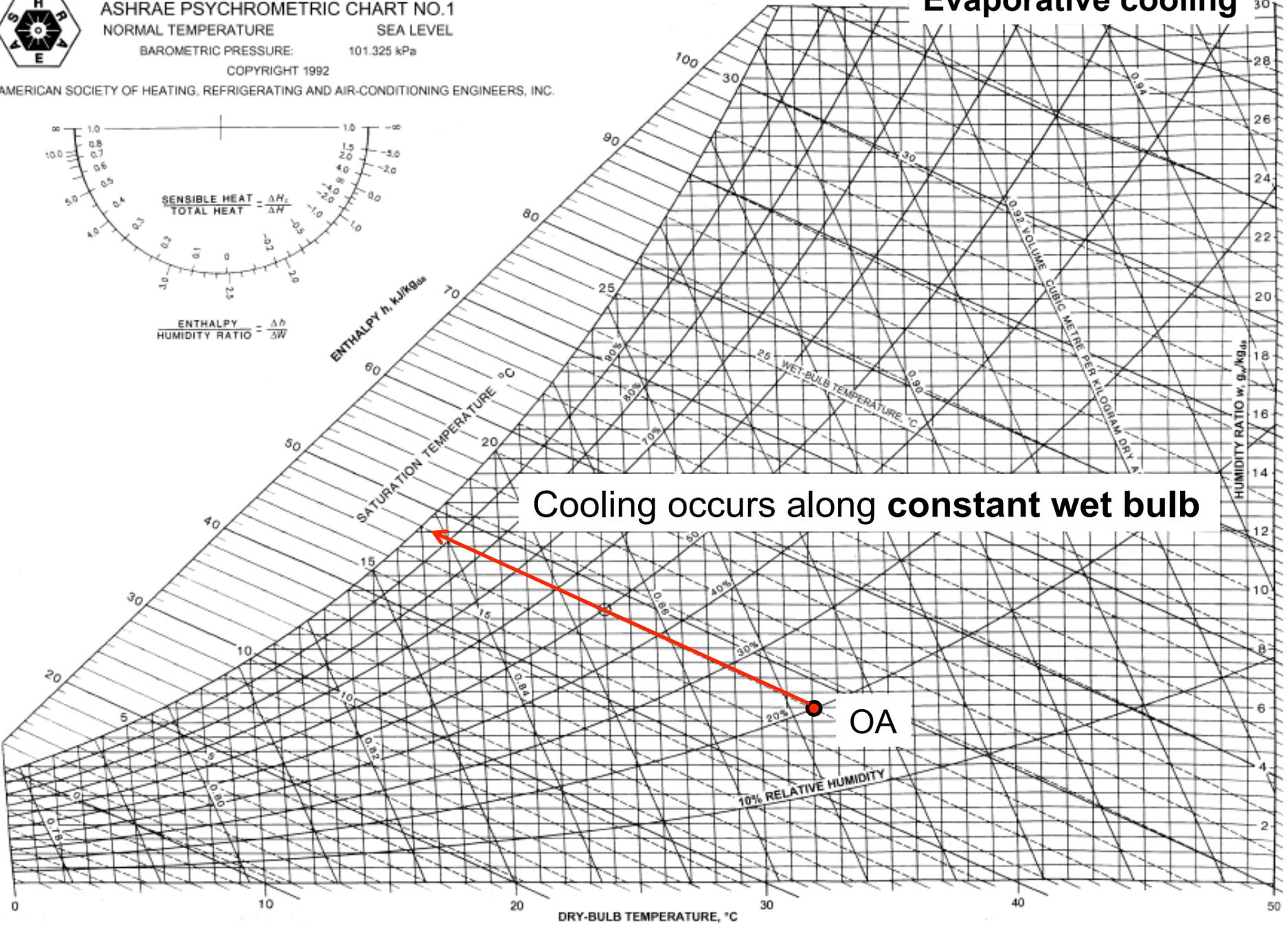
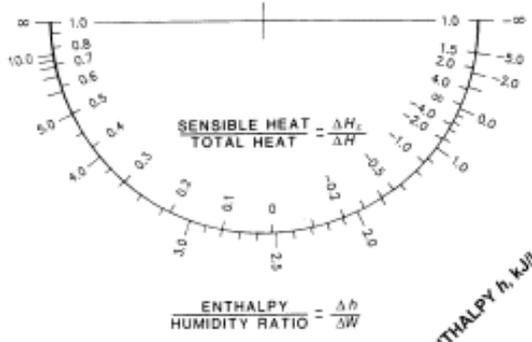




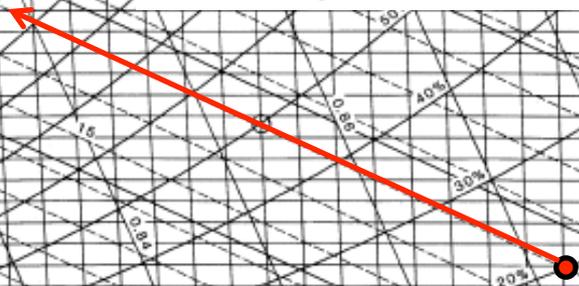
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NORMAL TEMPERATURE SEA LEVEL
BAROMETRIC PRESSURE: 101.325 kPa
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Evaporative cooling

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Cooling occurs along **constant wet bulb**

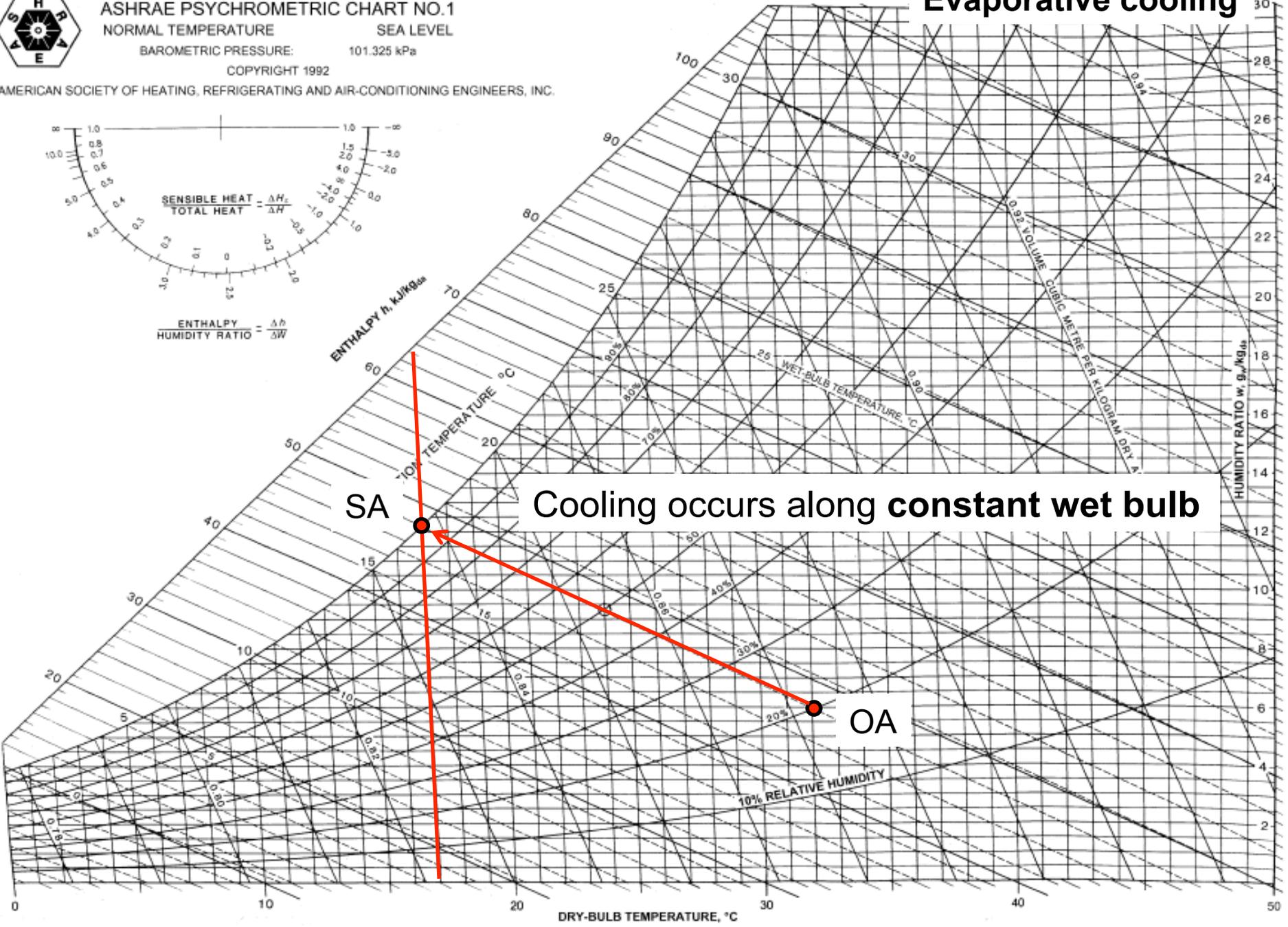
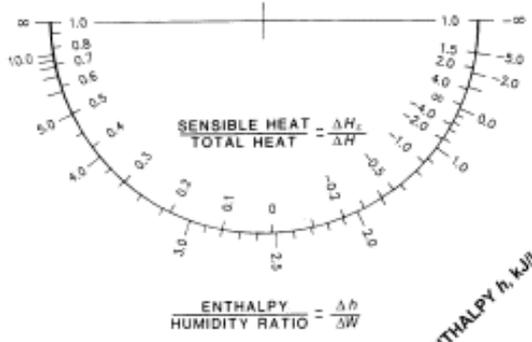




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NORMAL TEMPERATURE SEA LEVEL
BAROMETRIC PRESSURE: 101.325 kPa
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SA Cooling occurs along **constant wet bulb**

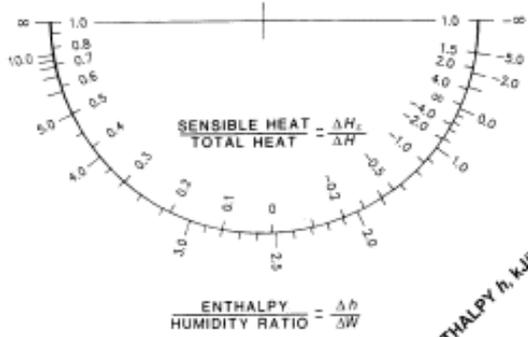
OA

DRY-BULB TEMPERATURE, °C

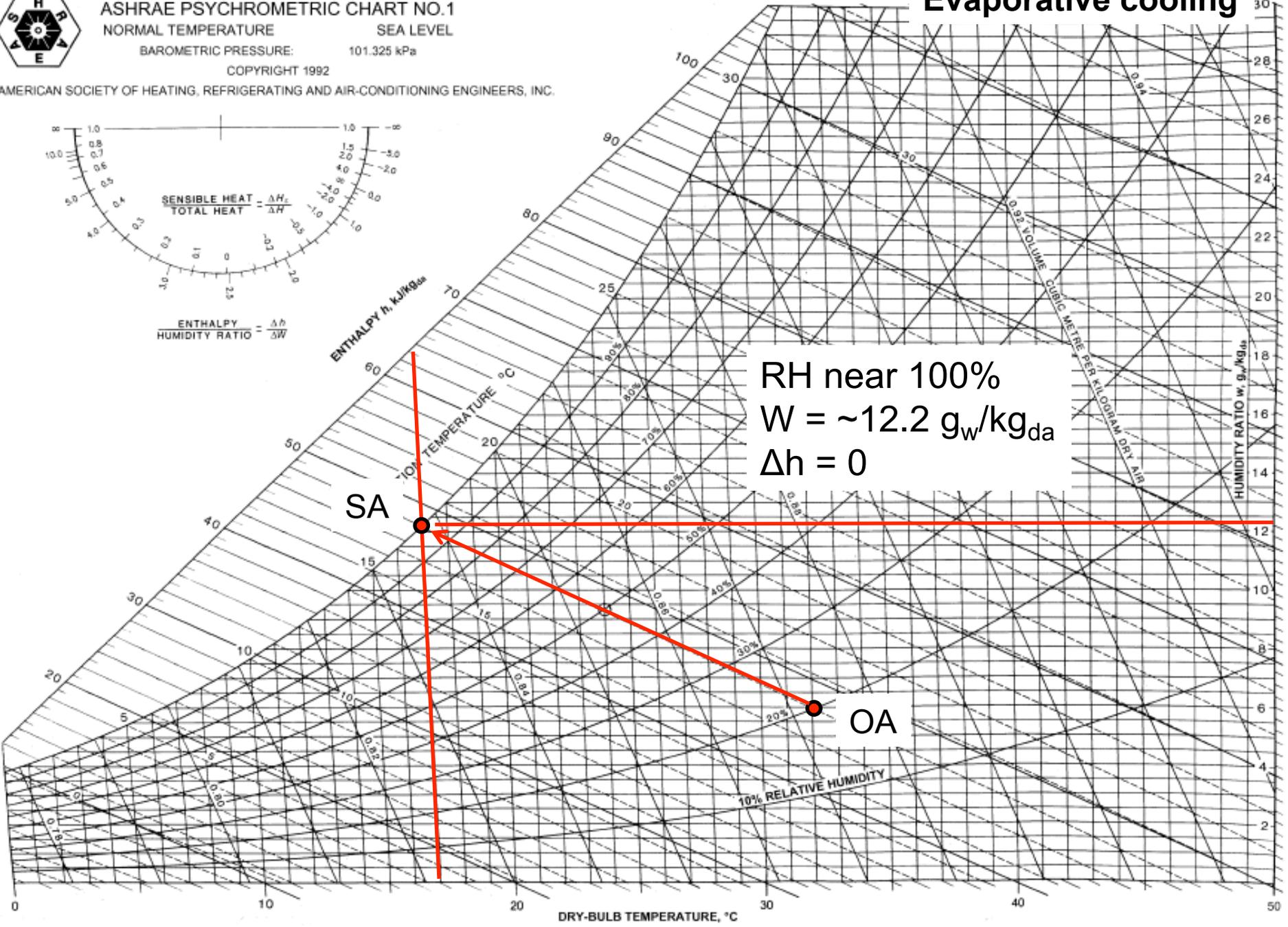


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NORMAL TEMPERATURE SEA LEVEL
BAROMETRIC PRESSURE: 101.325 kPa
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Evaporative cooling



RH near 100%
 $W = \sim 12.2 \text{ g}_w/\text{kg}_{da}$
 $\Delta h = 0$

SA

OA

10% RELATIVE HUMIDITY

DRY-BULB TEMPERATURE, °C

HUMIDITY RATIO w , g_w/kg_{da}

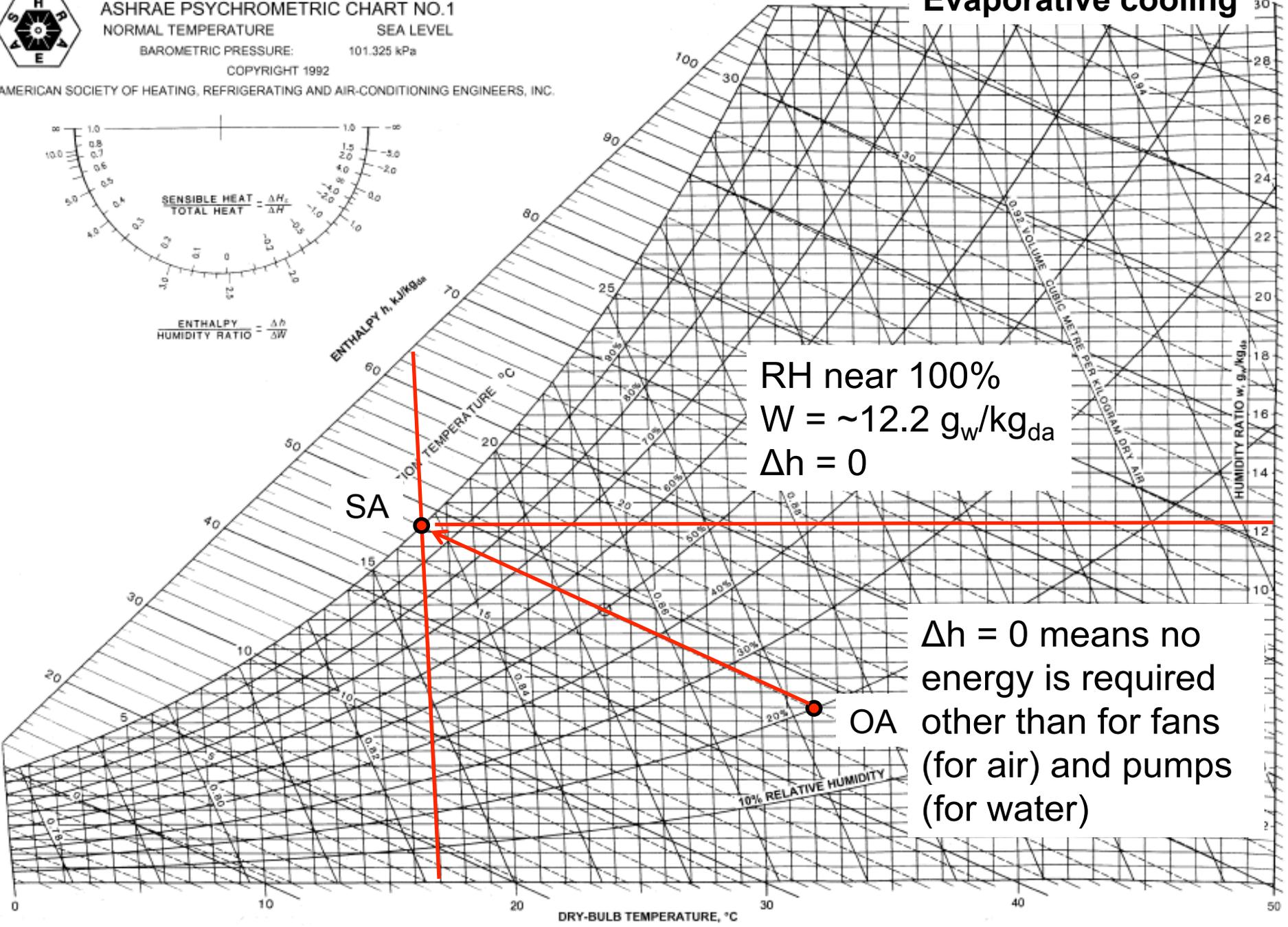
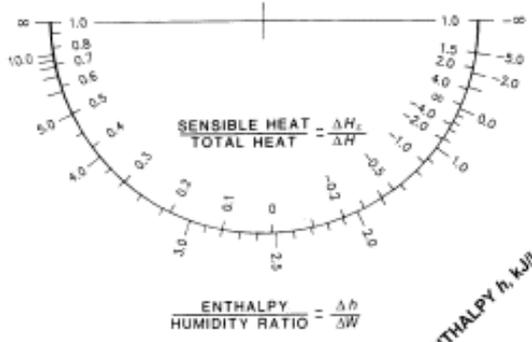
0.92 VOLUME CUBIC METRE PER KILOGRAM DRY AIR



ASHRAE PSYCHROMETRIC CHART NO.1
 NORMAL TEMPERATURE SEA LEVEL
 BAROMETRIC PRESSURE: 101.325 kPa
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Evaporative cooling

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SA

RH near 100%
 $W = \sim 12.2 \text{ g}_w/\text{kg}_{da}$
 $\Delta h = 0$

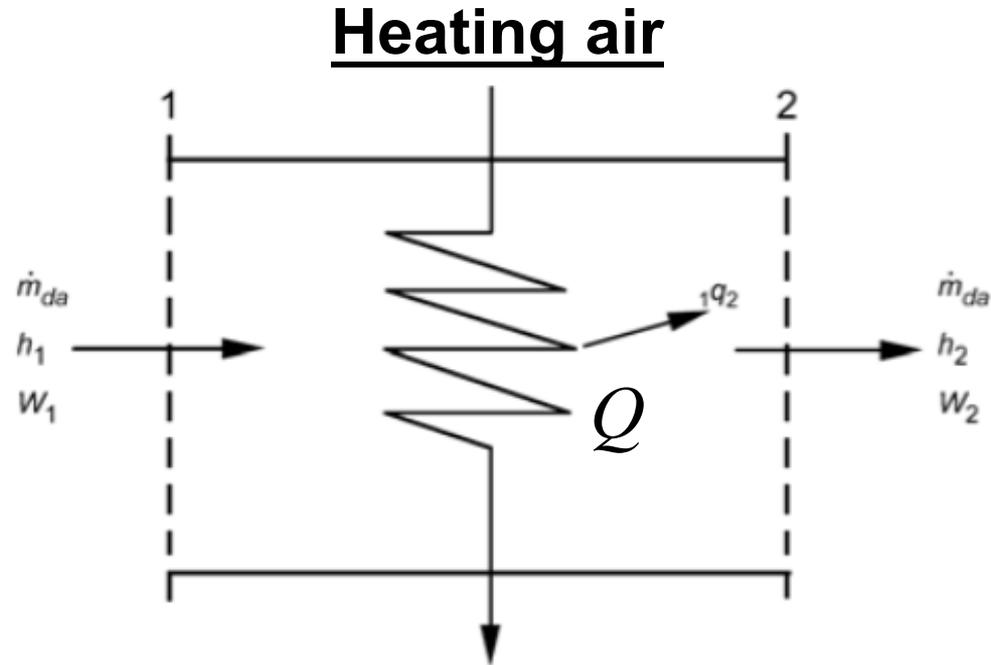
OA

$\Delta h = 0$ means no energy is required other than for fans (for air) and pumps (for water)

PSYCHROMETRIC PROCESSES

Using energy and mass balance equations

Energy/mass balances for psychrometric processes



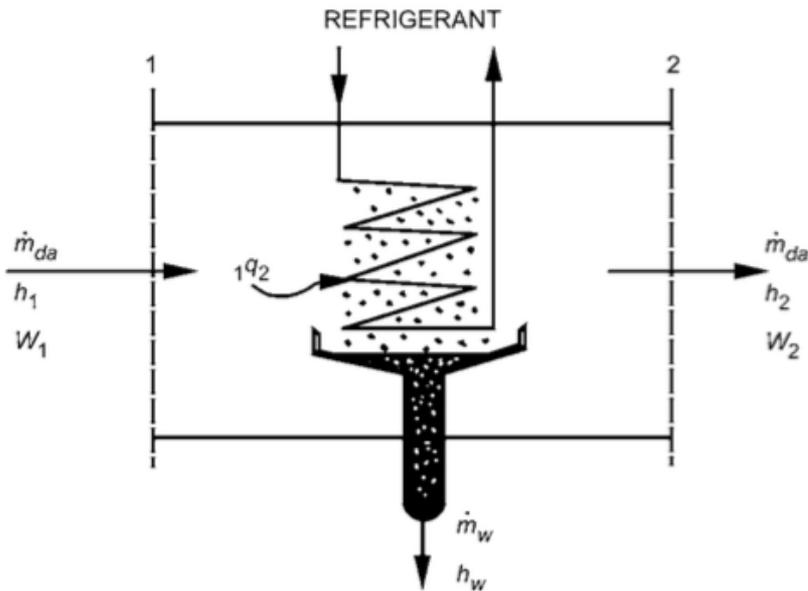
Energy balance: $\dot{m}_{da,1} h_1 + Q_{1 \rightarrow 2} = \dot{m}_{da,2} h_2$

Mass balance on air: $\dot{m}_{da,1} = \dot{m}_{da,2} = \dot{m}_{da}$

Mass balance on water vapor: $\dot{m}_{da,1} W_1 = \dot{m}_{da,2} W_2$

Therefore: $Q_{1 \rightarrow 2} = \dot{m}_{da} (h_2 - h_1)$

Energy/mass balances for psychrometric processes



Cooling and dehumidifying

*Note that $h_w = h_g$ for steam/vapor and $h_w = h_f$ for water

Energy balance: $\dot{m}_{da,1} h_1 + Q_{1 \rightarrow 2} = \dot{m}_{da,2} h_2 + \dot{m}_w h_{w,2}$

Mass balance on air: $\dot{m}_{da,1} = \dot{m}_{da,2} = \dot{m}_{da}$

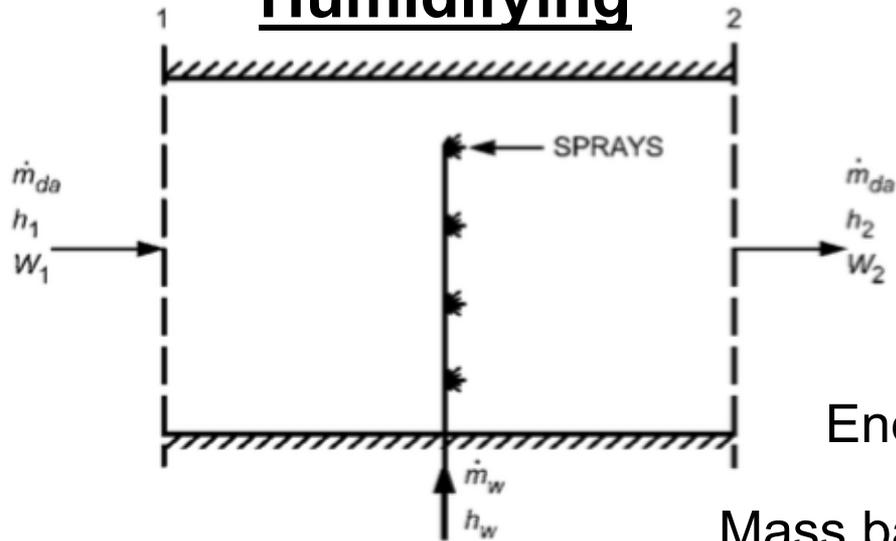
Mass balance on water vapor: $\dot{m}_{da,1} W_1 = \dot{m}_{da,2} W_2 + \dot{m}_w$

Therefore: $\dot{m}_w = \dot{m}_{da} (W_1 - W_2)$

And: $Q_{1 \rightarrow 2} = \dot{m}_{da} [(h_2 - h_1) - (W_2 - W_1) h_{w,2}]$
(Q is negative for cooling)

Energy/mass balances for psychrometric processes

Humidifying



Energy balance:

$$\dot{m}_{da,1} h_1 + \dot{m}_w h_w = \dot{m}_{da,2} h_2$$

Mass balance on air:

$$\dot{m}_{da,1} = \dot{m}_{da,2} = \dot{m}_{da}$$

Mass balance on water vapor:

$$\dot{m}_{da,1} W_1 + \dot{m}_w = \dot{m}_{da,2} W_2$$

Therefore:

$$\dot{m}_w = \dot{m}_{da} (W_2 - W_1)$$

And:

$$\dot{m}_w h_w = \dot{m}_{da} (h_2 - h_1)$$

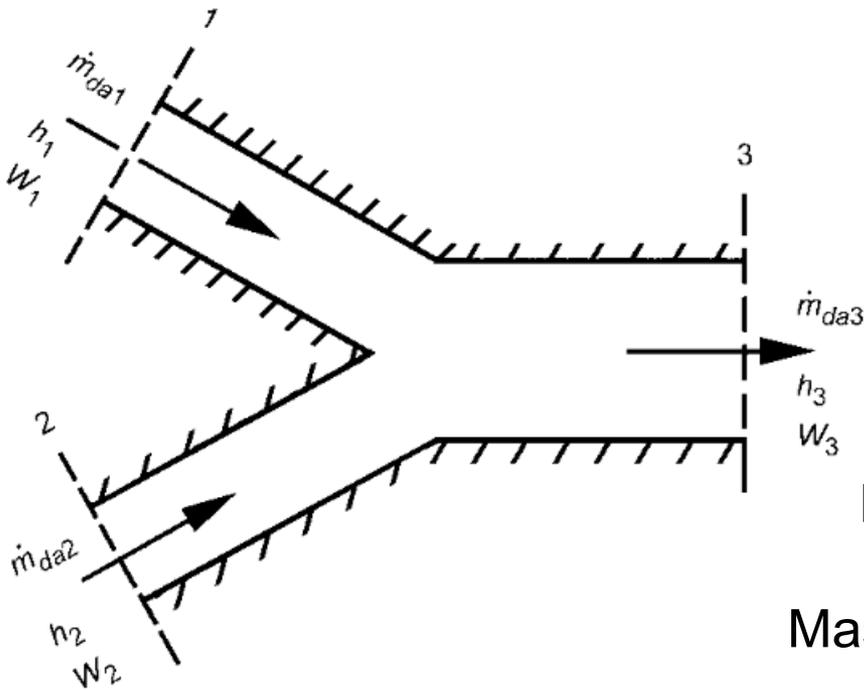
And:

$$\frac{h_2 - h_1}{W_2 - W_1} = \frac{\Delta h}{\Delta W} = h_w$$

*Note that $h_w = h_g$ for steam/vapor and $h_w = h_f$ for water

Energy/mass balances for psychrometric processes

- **Mixing:** Often in HVAC systems we mix airstreams adiabatically
 - **Adiabatically** = Without the addition or extraction of heat
 - e.g. outdoor air mixed with a portion of return/recirculated air



$$\text{Energy: } \dot{m}_{da,1} h_1 + \dot{m}_{da,2} h_2 = \dot{m}_{da,3} h_3$$

$$\text{Mass (air): } \dot{m}_{da,1} + \dot{m}_{da,2} = \dot{m}_{da,3}$$

$$\text{Mass (water): } \dot{m}_{da,1} W_1 + \dot{m}_{da,2} W_2 = \dot{m}_{da,3} W_3$$

Energy/mass balances for psychrometric processes

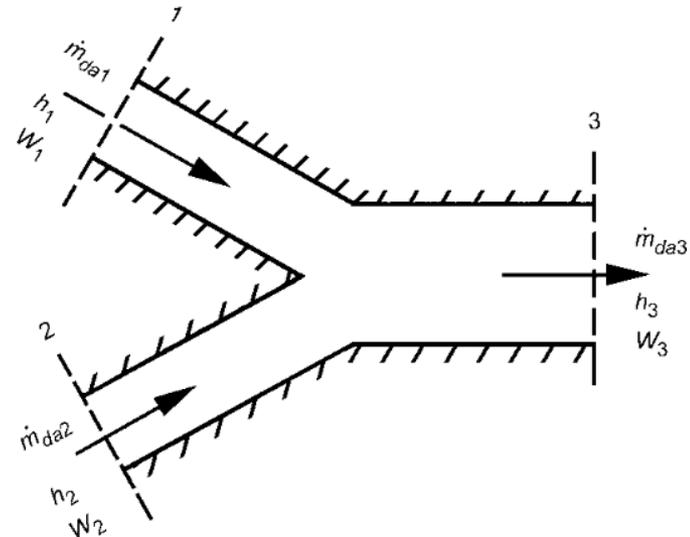
- **Mixing:** For most parameters, the outlet conditions end up being the weighted averages of the input conditions based on their mass flow rates

- Dry bulb temperature
- Humidity ratio
- Enthalpy
- (not RH!)

$$T_3 = \frac{\dot{m}_{da1}T_1 + \dot{m}_{da2}T_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

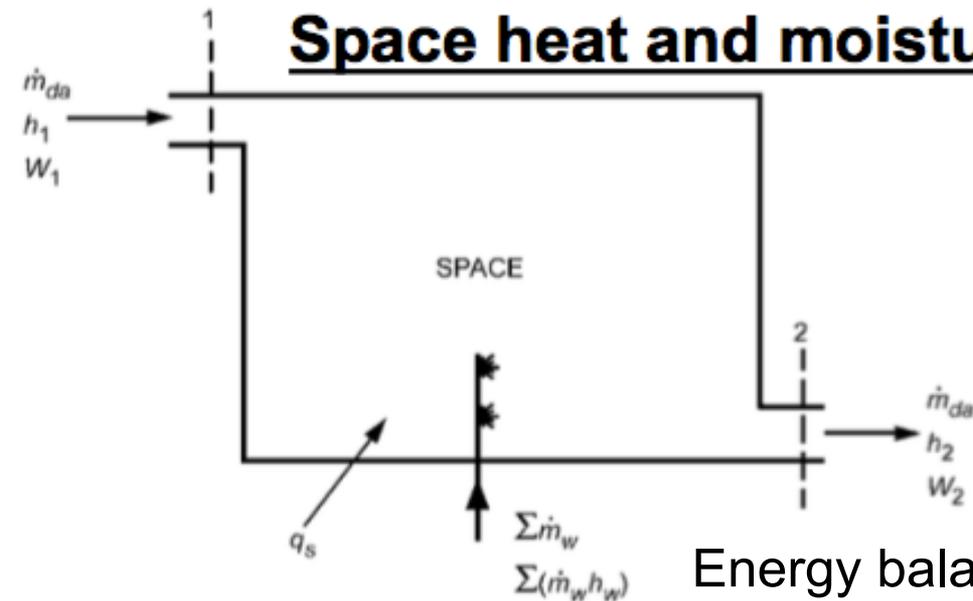
$$W_3 = \frac{\dot{m}_{da1}W_1 + \dot{m}_{da2}W_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

$$h_3 = \frac{\dot{m}_{da1}h_1 + \dot{m}_{da2}h_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$



Energy/mass balances for psychrometric processes

Space heat and moisture gains



Energy balance: $\dot{m}_{da} h_1 + Q_{gains} + \sum \dot{m}_w h_w = \dot{m}_{da} h_2$

Mass balance on water vapor: $\dot{m}_{da} W_1 + \sum \dot{m}_w = \dot{m}_{da} W_2$

Therefore: $\sum \dot{m}_w = \dot{m}_{da} (W_2 - W_1)$

Therefore: $\sum \dot{m}_w h_w + Q_{gains} = \dot{m}_{da} (h_2 - h_1)$

*Note that $h_w = h_g$ for steam/vapor and $h_w = h_f$ for water

And:
$$\frac{\Delta h}{\Delta W} = \frac{\sum \dot{m}_w h_w + Q_{gains}}{\sum \dot{m}_w}$$

Next time

- Psychrometric processes: example problems