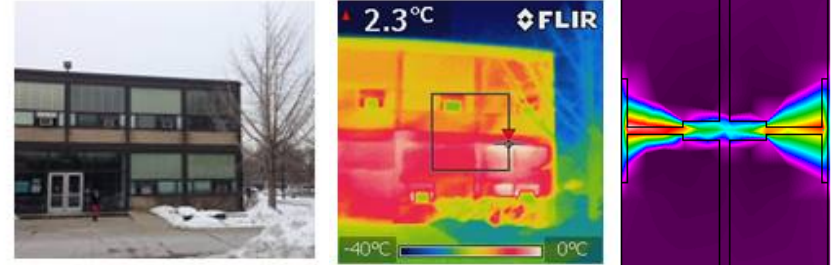


CAE 331/513

Building Science

Fall 2016



Week 8: October 11, 2016

Mechanical systems and psychrometric processes

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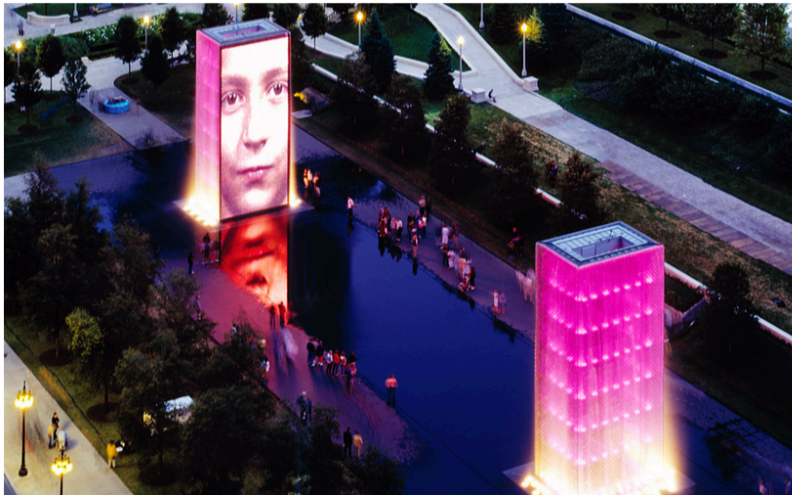
Dr. Brent Stephens, Ph.D.

Civil, Architectural and Environmental Engineering

Illinois Institute of Technology

brent@iit.edu

Lighting design internship opportunity



FALL/WINTER INTERN:

Schuler Shook's Chicago office seeks a highly motivated, detail-oriented person to be our 2016 Fall or Winter Intern. You will learn more about architectural lighting and contribute to a variety of interior and exterior lighting projects.

TO APPLY:

Email your resume and portfolio link to Jim Baney, Partner:
jbaney@schulershook.com

REQUIREMENTS:

-Be currently enrolled in a Lighting Design MFA program or an Architectural Engineering program with some lighting classes.

-Possess excellent writing and communication skills

-Proficiency with AutoCAD, Revit, Photoshop, Word, Excel, and AGI32. Experience with 3DS Max, Rhino or Daysim is a plus.

VISIT US ONLINE:

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Review from last time

- Psychrometric equations examples (SI and IP units)
- Began an overview of HVAC systems and typical components and processes involved
- **Today:** Continue HVAC systems overview and understand psychrometric processes

PSYCHROMETRIC PROCESSES

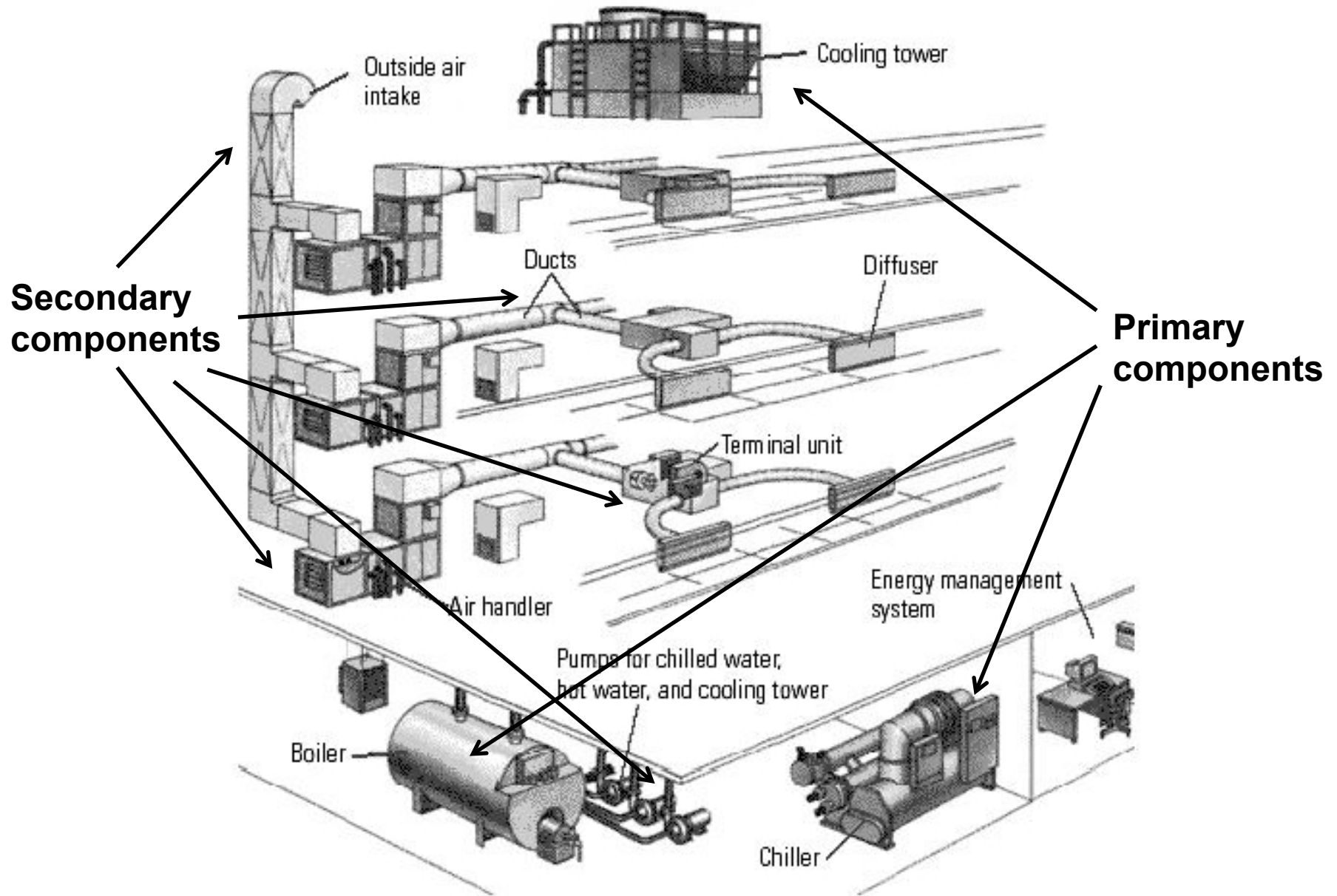
Use of the psychrometric chart for *processes*

We can use the psychrometric chart (and equations) not only to describe states of moist air, but for a number of processes that are important for building science and HVAC applications

Examples:

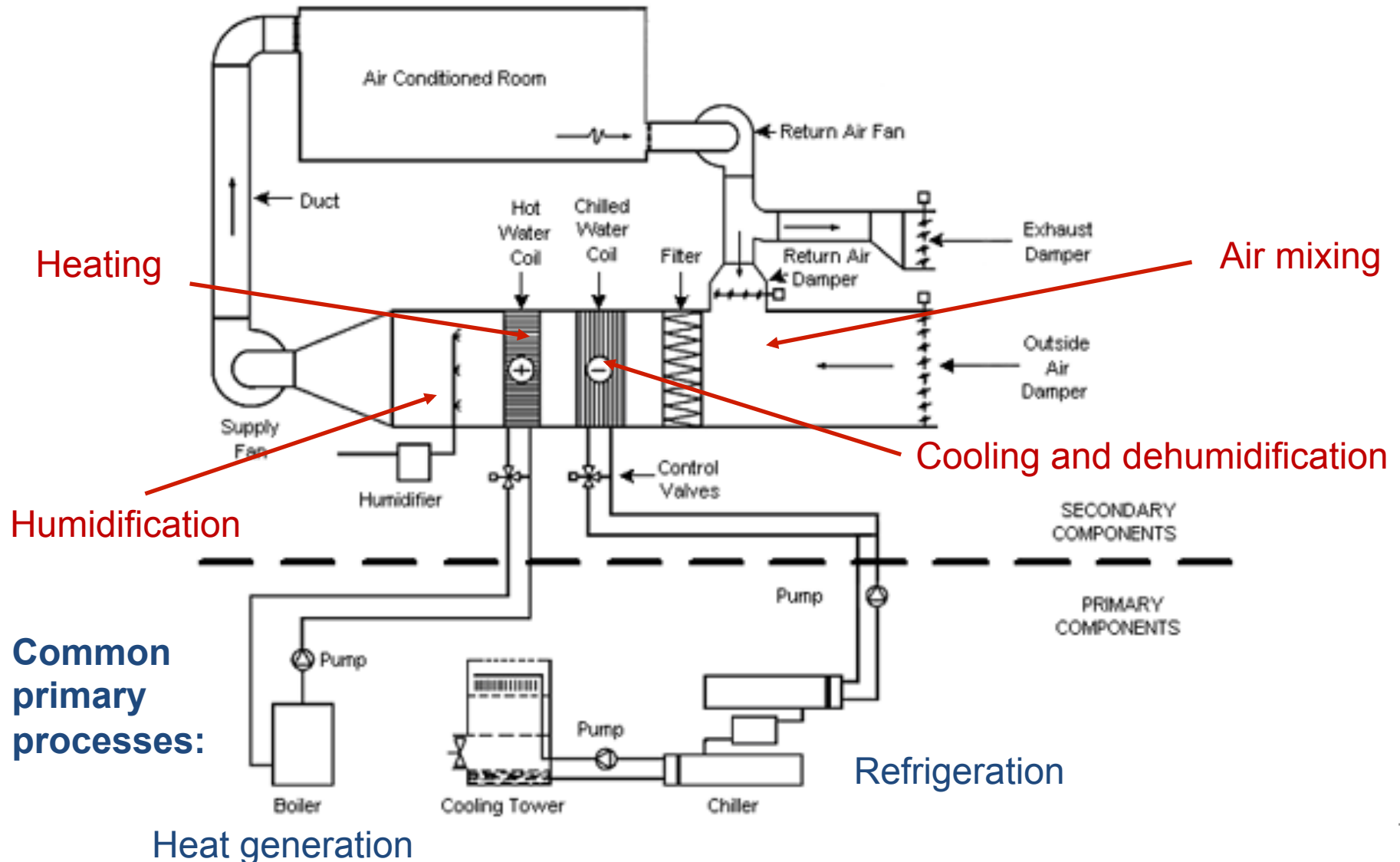
- Sensible cooling or heating
- Warming and humidification of cold, dry air
- Cooling and dehumidification of warm, humid air
 - Sensible + latent cooling
- Evaporative cooling
- Mixing of airstreams

Typical components of an HVAC system



Typical HVAC processes

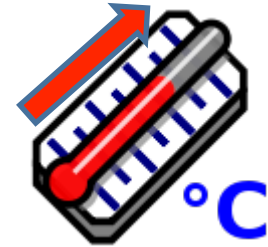
Some common psychrometric processes:



Definitions: Sensible and latent heat

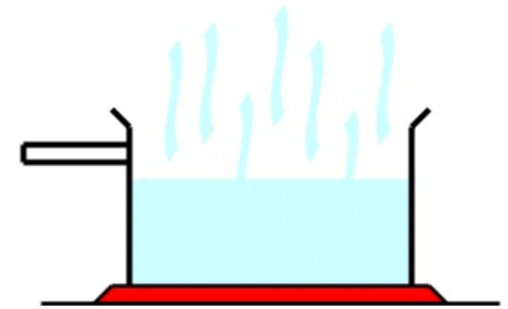
- **Sensible** heat transfer

- Increase or decrease in temperature of a substance *without* undergoing a phase change



- **Latent** heat transfer

- Heat transfer required to change the phase of a substance (e.g., heat required to change liquid to vapor)



$$Q_{total} = Q_{sensible} + Q_{latent}$$

Units of [W], [BTU/hr], or [ton]

Sensible and latent heat transfer equation

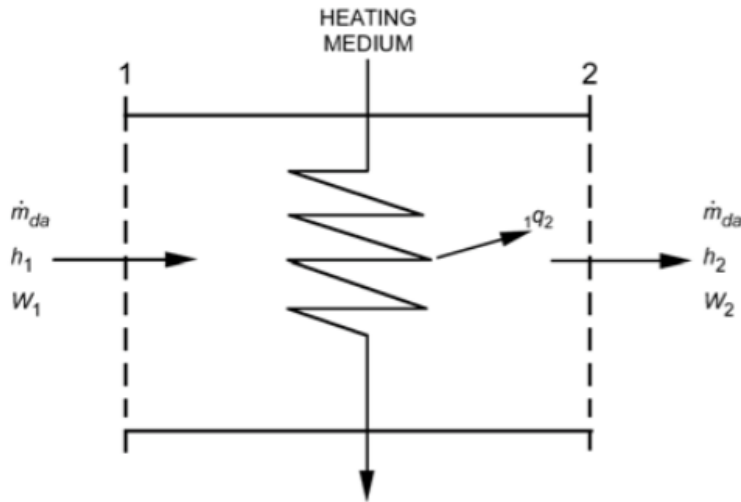


Fig. 2 Schematic of Device for Heating Moist Air

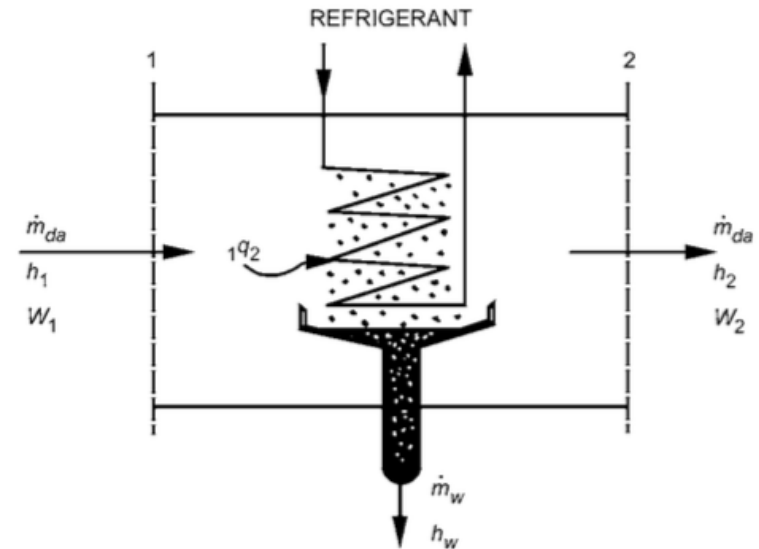


Fig. 3 Schematic of Device for Cooling Moist Air

Generic equations for both heating and cooling processes:

$$Q_{1 \rightarrow 2} = \dot{m}_{da} (h_2 - h_1) \qquad Q_{total} = \dot{m}_{da} (h_{exit} - h_{inlet})$$

$Q_{1 \rightarrow 2}$ = total rate of heat transfer from state 1 to state 2 (W or BTU/hr or ton)

\dot{m}_{da} = mass flow rate of dry air (kg_{da}/s or lb_{da}/hr)

$h_{exit,2}$ = enthalpy at the exit (J/kg_{da} or BTU/lb_{da})

$h_{inlet,1}$ = enthalpy at the inlet (J/kg_{da} or BTU/lb_{da})

Sensible heat transfer equation

$$Q_{sensible} = \dot{m}_{da} C_p (T_{exit} - T_{inlet}) = \rho_{da} \dot{V}_{da} C_p (T_{exit} - T_{inlet})$$

$Q_{sensible}$ = rate of sensible heat transfer (W or BTU/hr or ton)

C_p = specific heat of air (J/kgK or BTU/lb°F)

ρ_{da} = dry air density (kg/m³ or lb/ft³)

T_{inlet} = inlet temperature (K or °F)

T_{exit} = exit temperature (K or °F)

For heating: $Q_{sensible} > 0$

For cooling: $Q_{sensible} < 0$



Latent heat transfer equation

$$Q_{latent} = \dot{m}_{da} h_{fg} (W_{exit} - W_{inlet}) = \rho_{da} \dot{V}_{da} h_{fg} (W_{exit} - W_{inlet})$$

Q_{latent} = rate of latent heat transfer (W or BTU/hr or ton)

\dot{m}_w = mass flow rate of water vapor (kg_w/s or lb_w/hr)

h_{fg} = enthalpy, or latent heat, of vaporization (J/kg or BTU/lb)

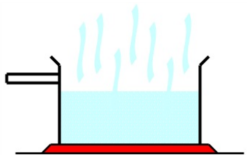
* h_{fg} = 2260 kJ/kg or 970 BTU/lb for water

W_{inlet} = inlet humidity ratio (kg_w/kg_{da} or lb_w/lb_{da})

W_{exit} = exit humidity ratio (kg_w/kg_{da} or lb_w/lb_{da})

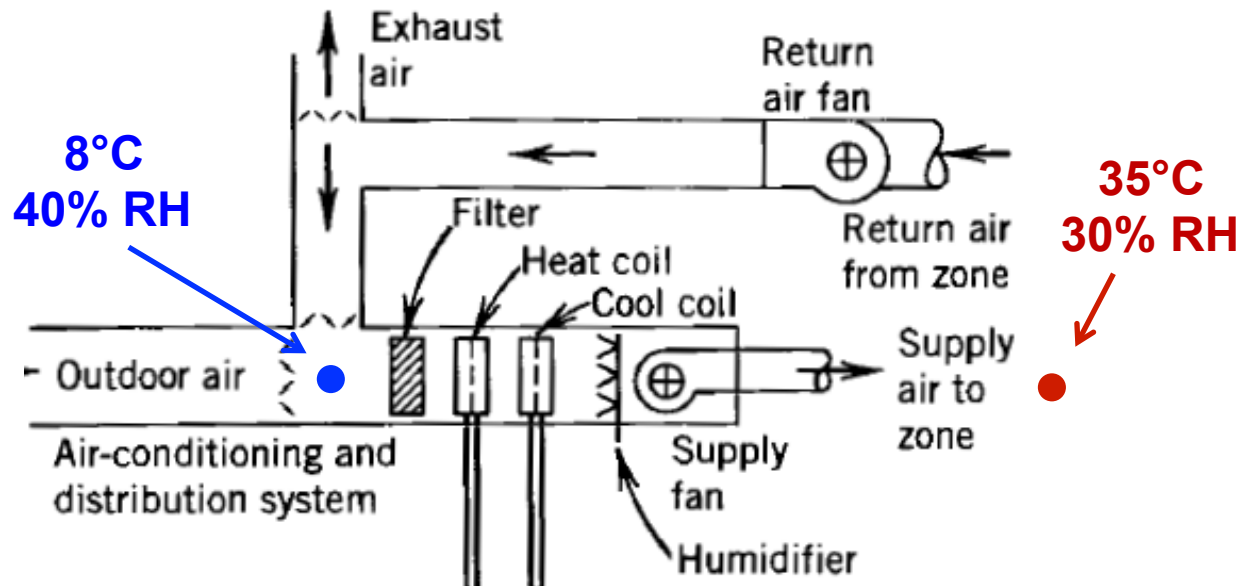
For humidification: $Q_{latent} > 0$

For dehumidification: $Q_{latent} < 0$



Heating and humidification of cold, dry air

- **Example:** Heating and humidification of air
 - Process: Adding moisture and heat (sensible + latent heating)



Q1: What is the enthalpy change required?

Q2: What is the total rate of heat transfer if the airflow rate is 10 m³/s?

Q2: What is the split between sensible and latent transfer?



ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

SEA LEVEL

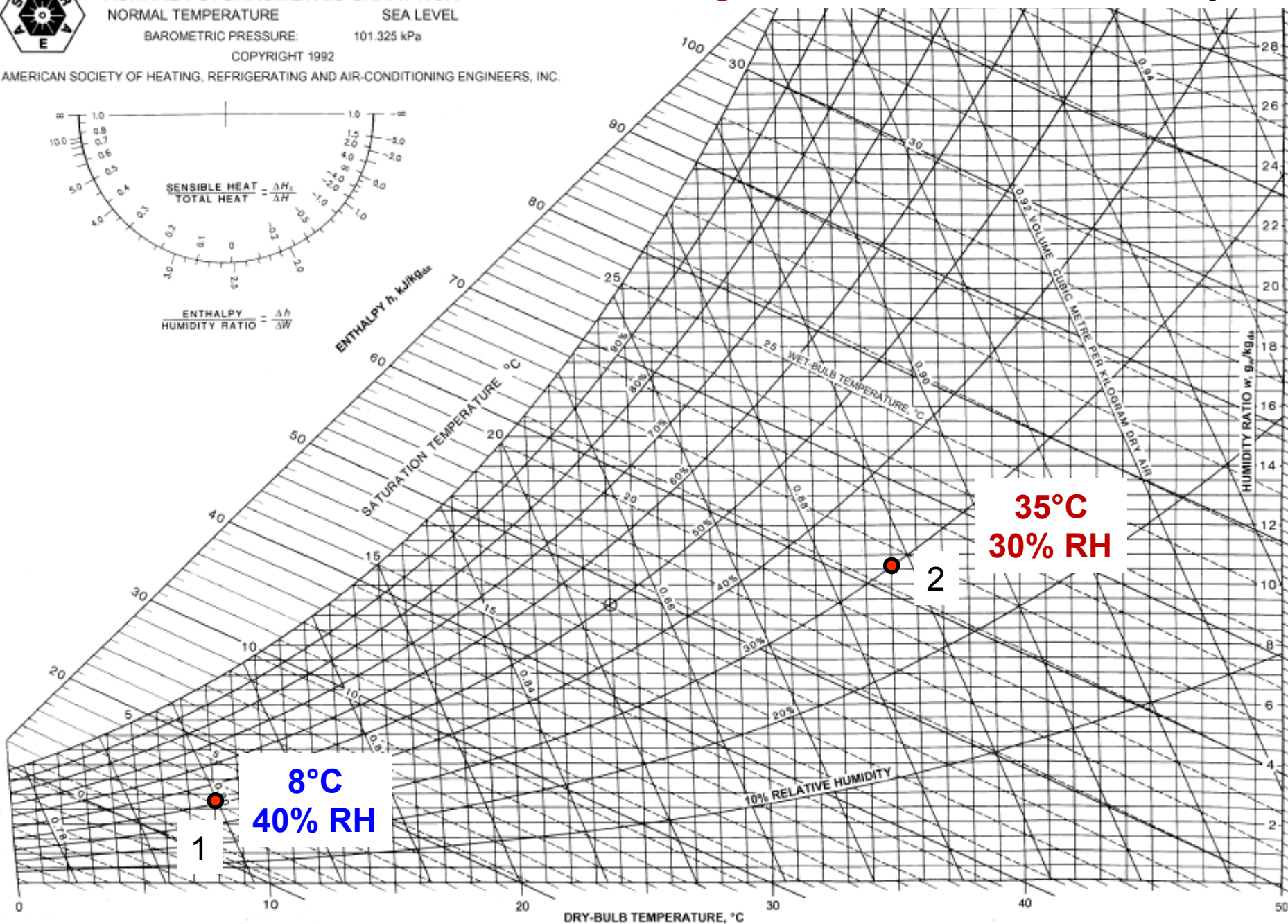
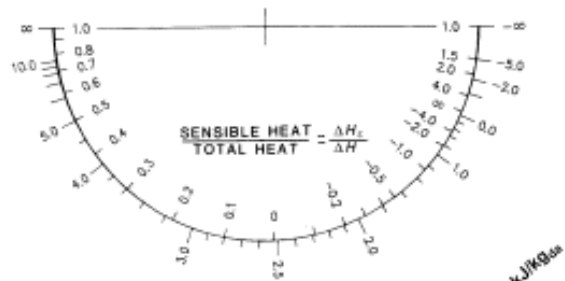
BAROMETRIC PRESSURE:

101.325 kPa

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Heating and humidification of cold, dry air

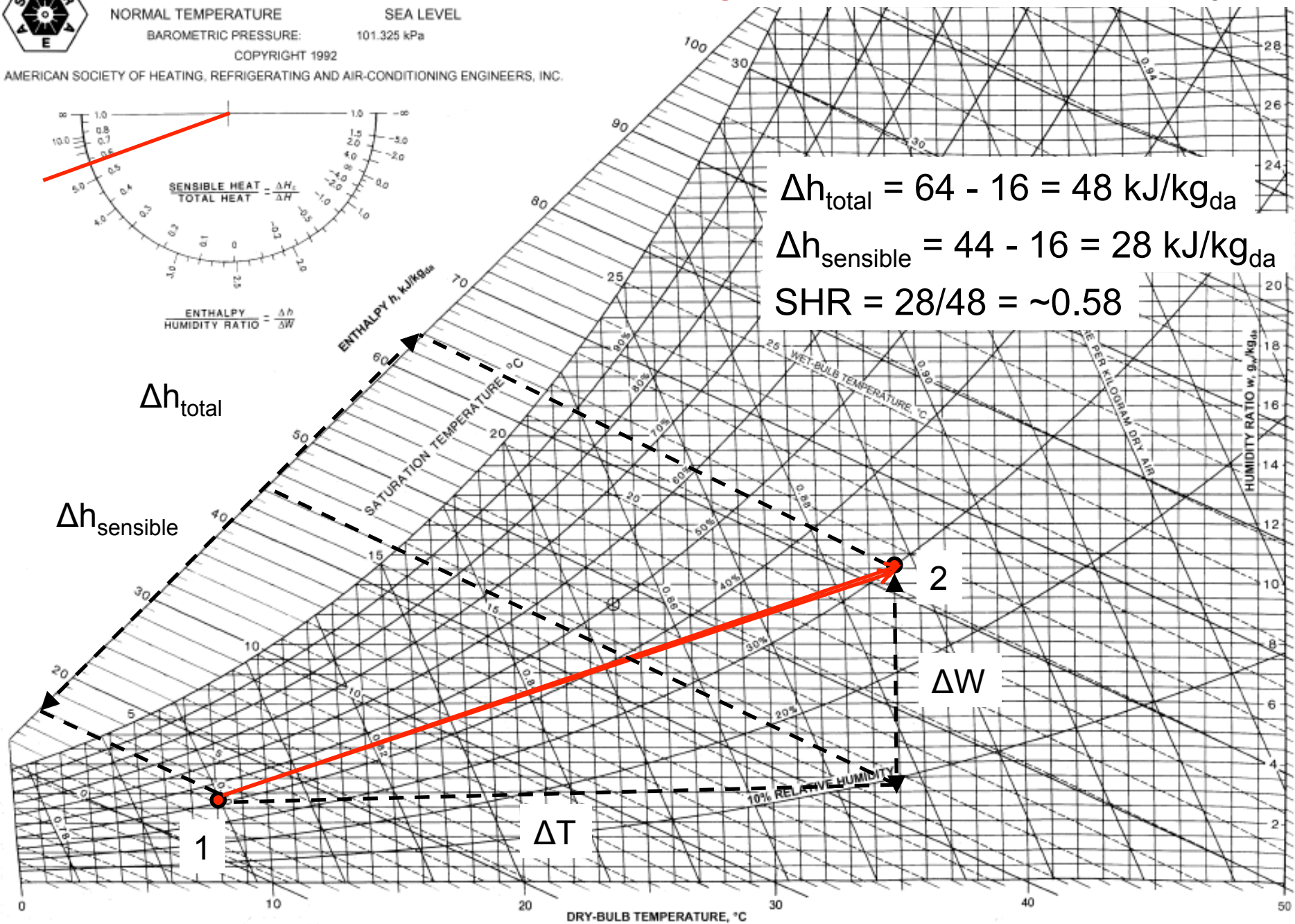
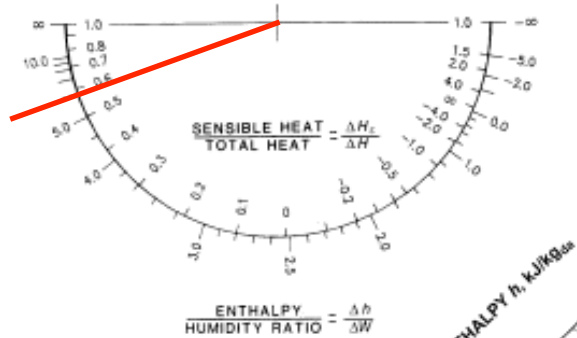




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NORMAL TEMPERATURE
SEA LEVEL
BAROMETRIC PRESSURE: 101.325 kPa
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Heating and humidification of cold, dry air

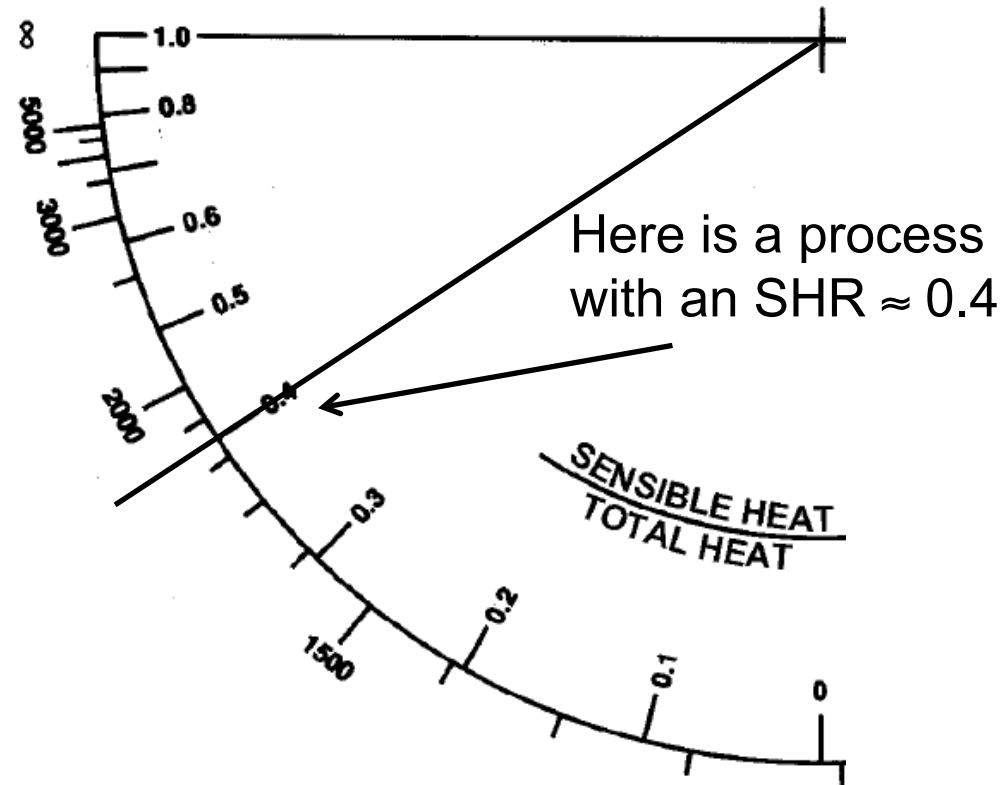


Sensible heat ratio (SHR)

- The **sensible heat ratio** is defined as:

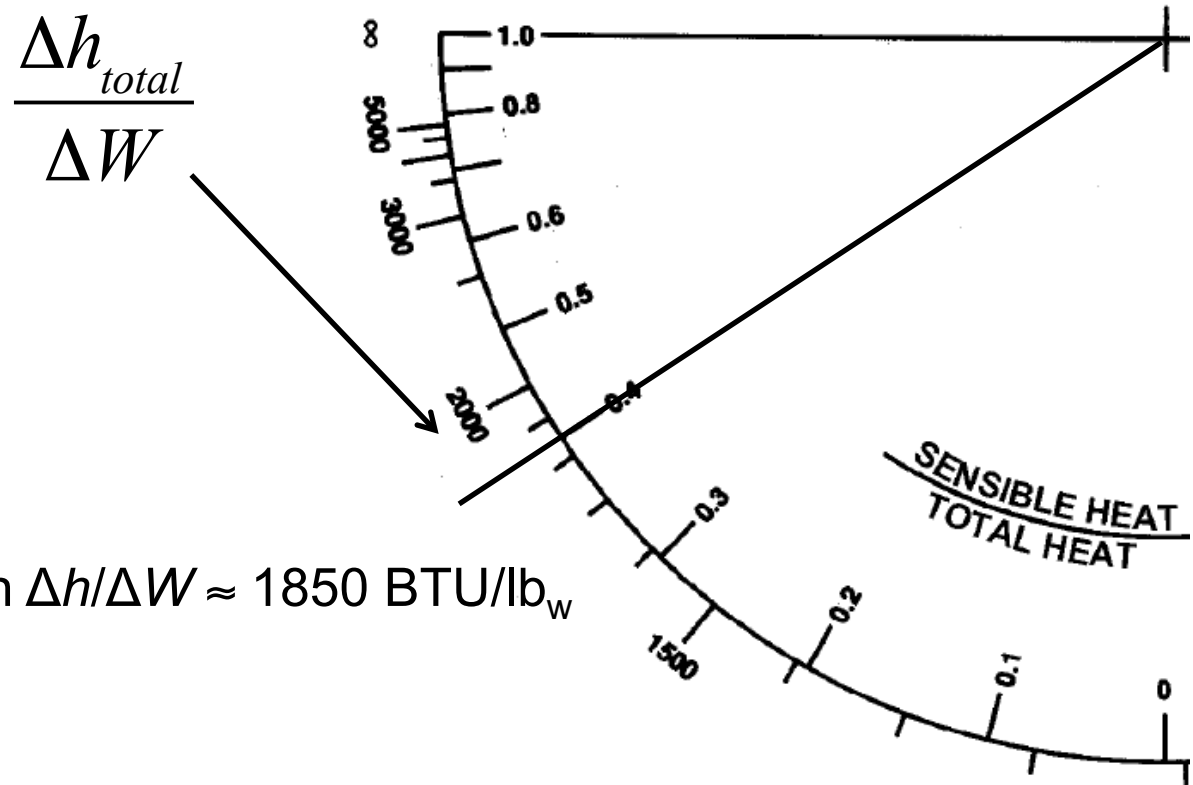
$$SHR = \frac{\dot{q}_{sens}}{\dot{q}_{total}} = \frac{\dot{q}_{sens}}{\dot{q}_{sens} + \dot{q}_{latent}} = \frac{\Delta h_{sens}}{\Delta h_{total}}$$

- Allows for understanding sensible load relative to latent load



Enthalpy protractor ($\Delta h/\Delta W$)

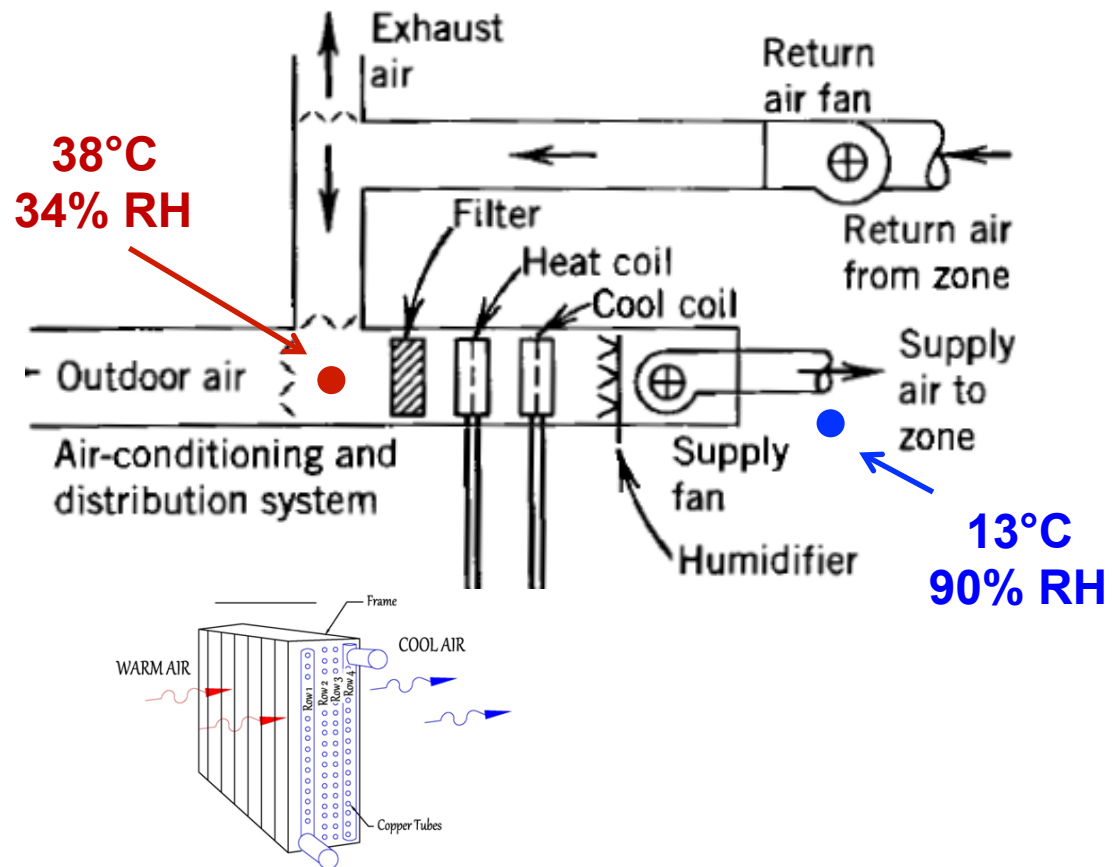
- The other side of the enthalpy protractor tells us:
 - What is the enthalpy change relative to the change in humidity ratio



Here is a process with $\Delta h/\Delta W \approx 1850 \text{ BTU/lb}_w$
SI units: kJ/kg_w

Cooling and dehumidification of **warm**, humid air

- **Example:** Air flowing over a cooling coil
- Removing both moisture and heat
 - Sensible + latent **cooling**

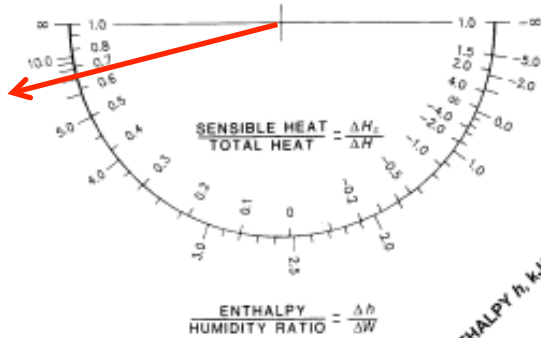




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NORMAL TEMPERATURE
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Cooling and dehumidification of **warm**, humid air

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SHR ~ 0.61

Δh

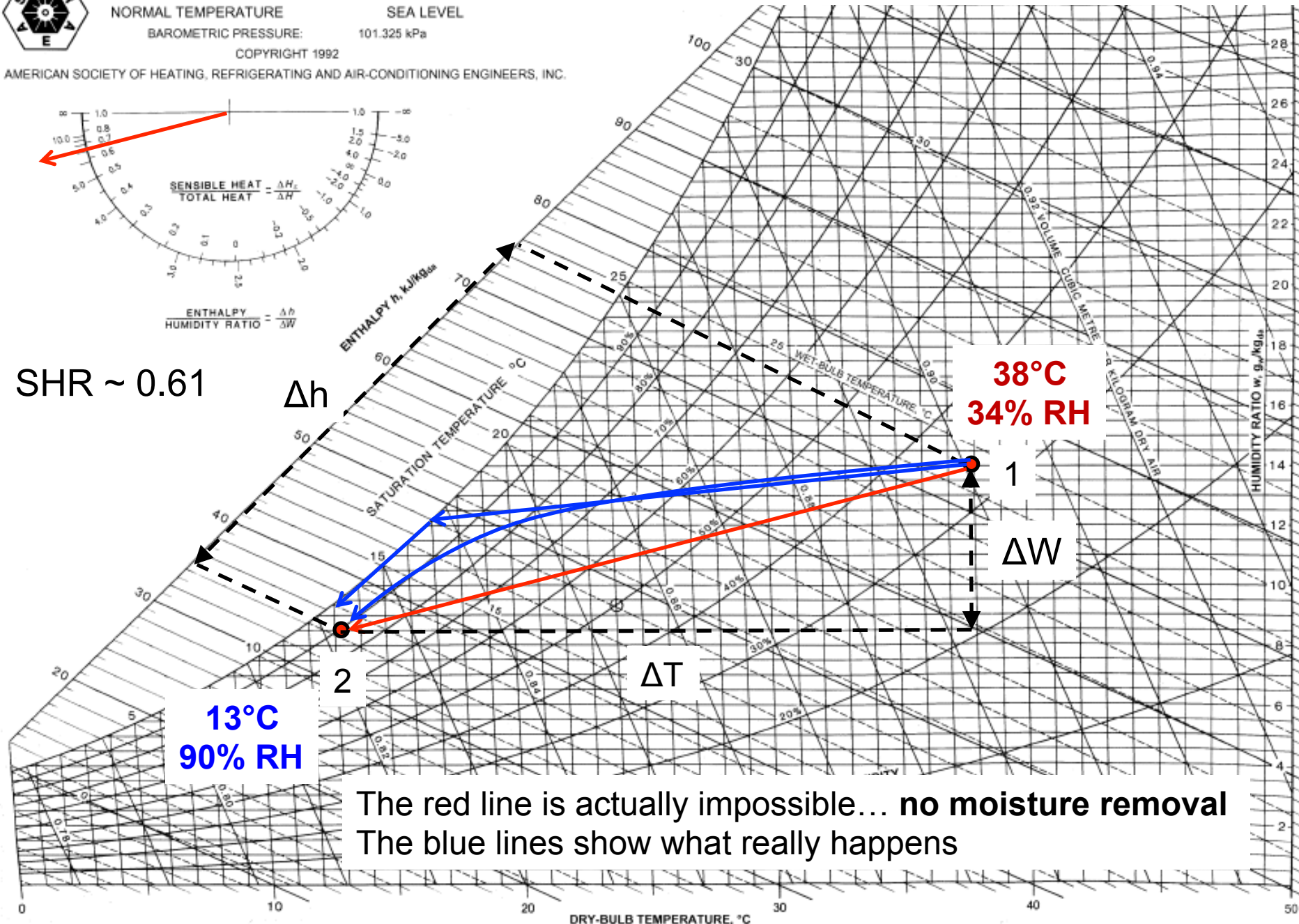
38°C
34% RH

1
 ΔW

ΔT

13°C
90% RH

The red line is actually impossible... **no moisture removal**
The blue lines show what really happens



Example: *Sensible* cooling

- Moist air is cooled from 40°C and 30% RH to 30°C without condensation
 - What is the RH at W at the process end point?



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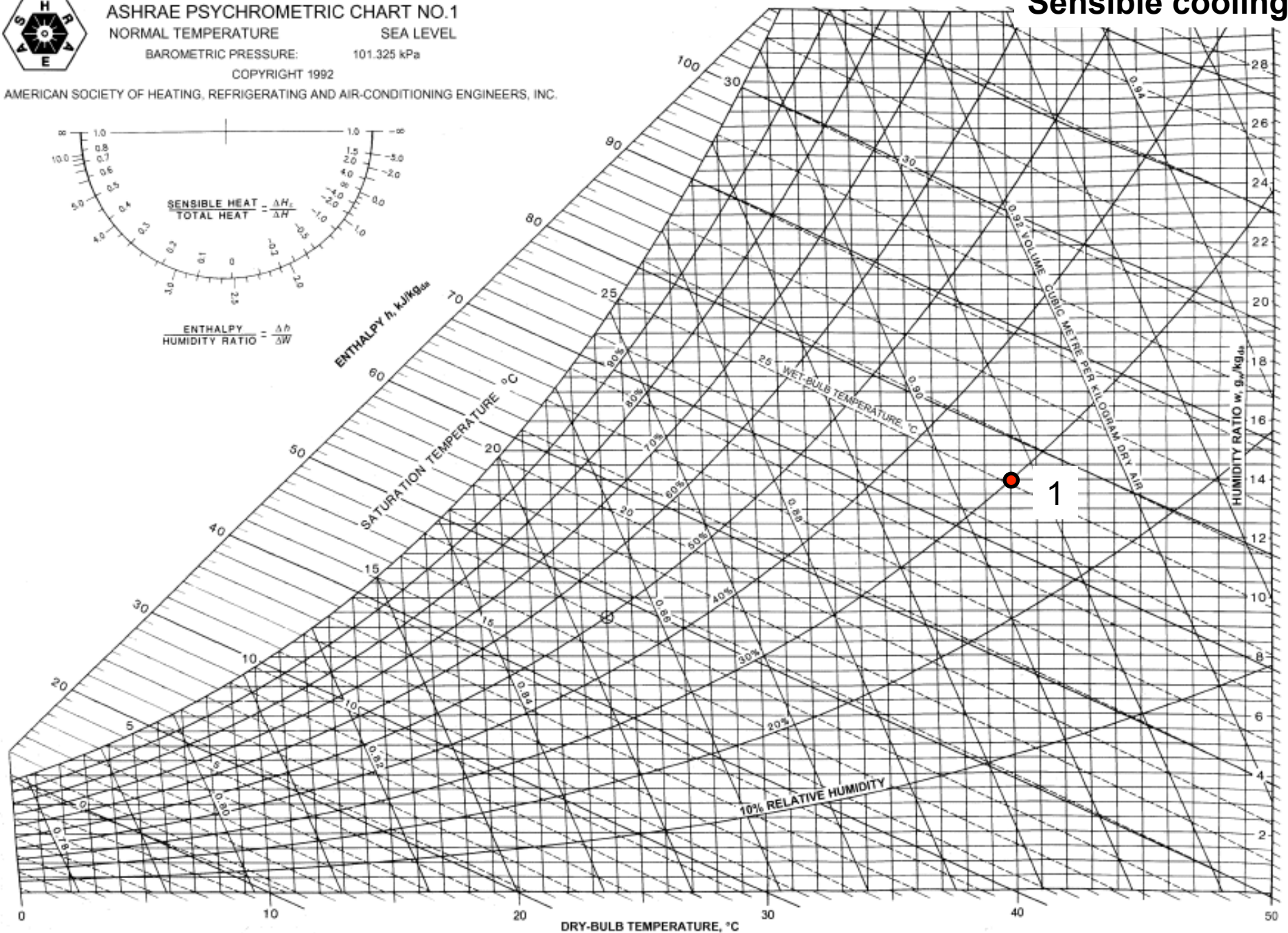
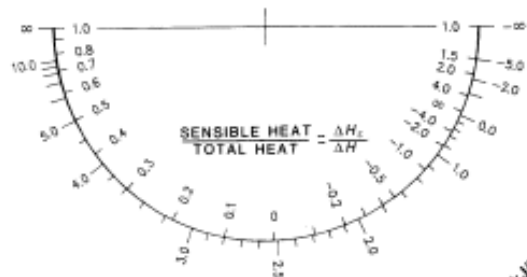
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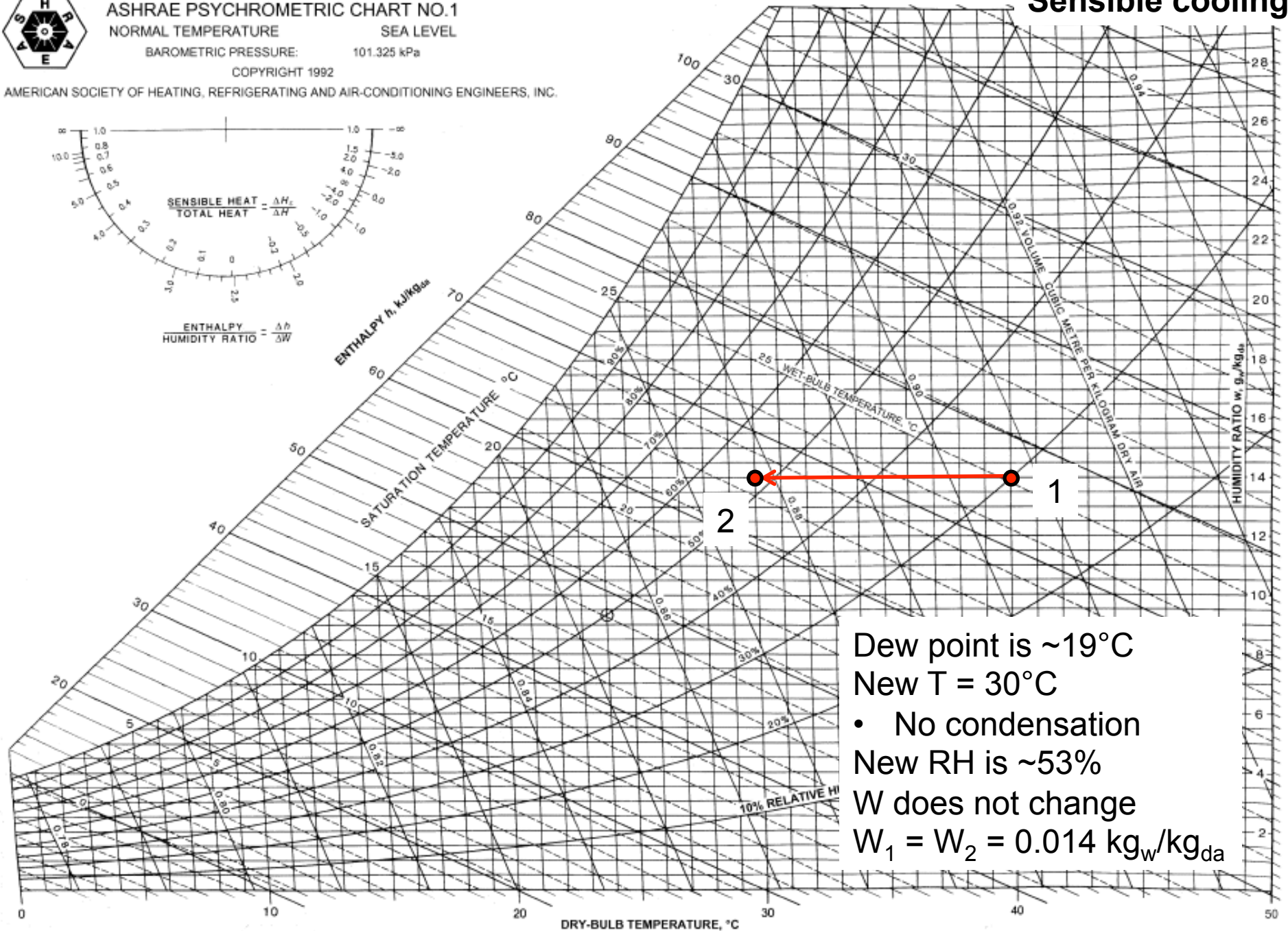
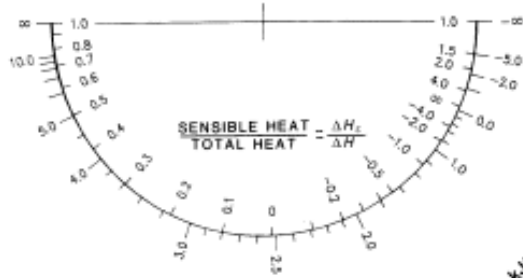
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NORMAL TEMPERATURE

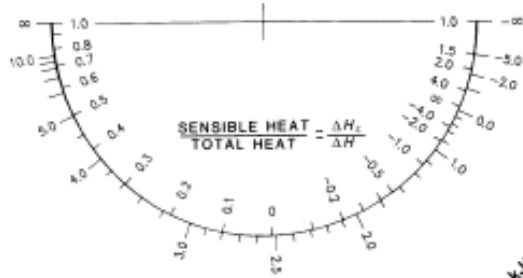
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$$\frac{\text{ENTHALPY}}{\text{HUMIDITY RATIO}} = \frac{\Delta h}{\Delta W}$$

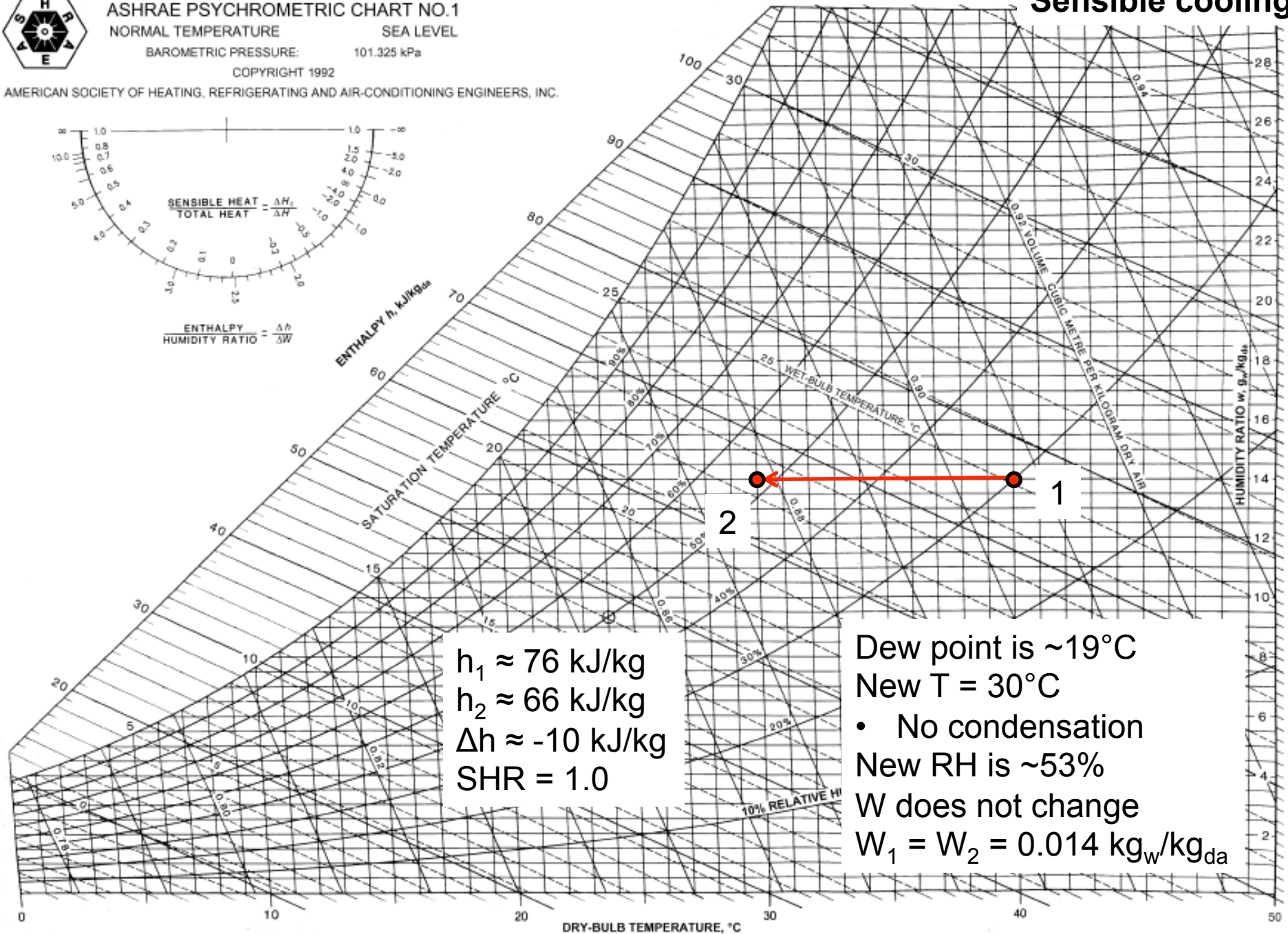
ENTHALPY h , kJ/kg_{da}

SATURATION TEMPERATURE °C

$h_1 \approx 76$ kJ/kg
 $h_2 \approx 66$ kJ/kg
 $\Delta h \approx -10$ kJ/kg
SHR = 1.0

Dew point is $\sim 19^\circ\text{C}$
New $T = 30^\circ\text{C}$
• No condensation
New RH is $\sim 53\%$
W does not change
 $W_1 = W_2 = 0.014$ kg_w/kg_{da}

Sensible cooling



Example: *Sensible + latent* cooling

- Moist air is cooled from 40°C and 30% RH to 15°C
 - Q1: Does the water vapor condense?
 - Q2: What is RH at W at the process end point?



ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

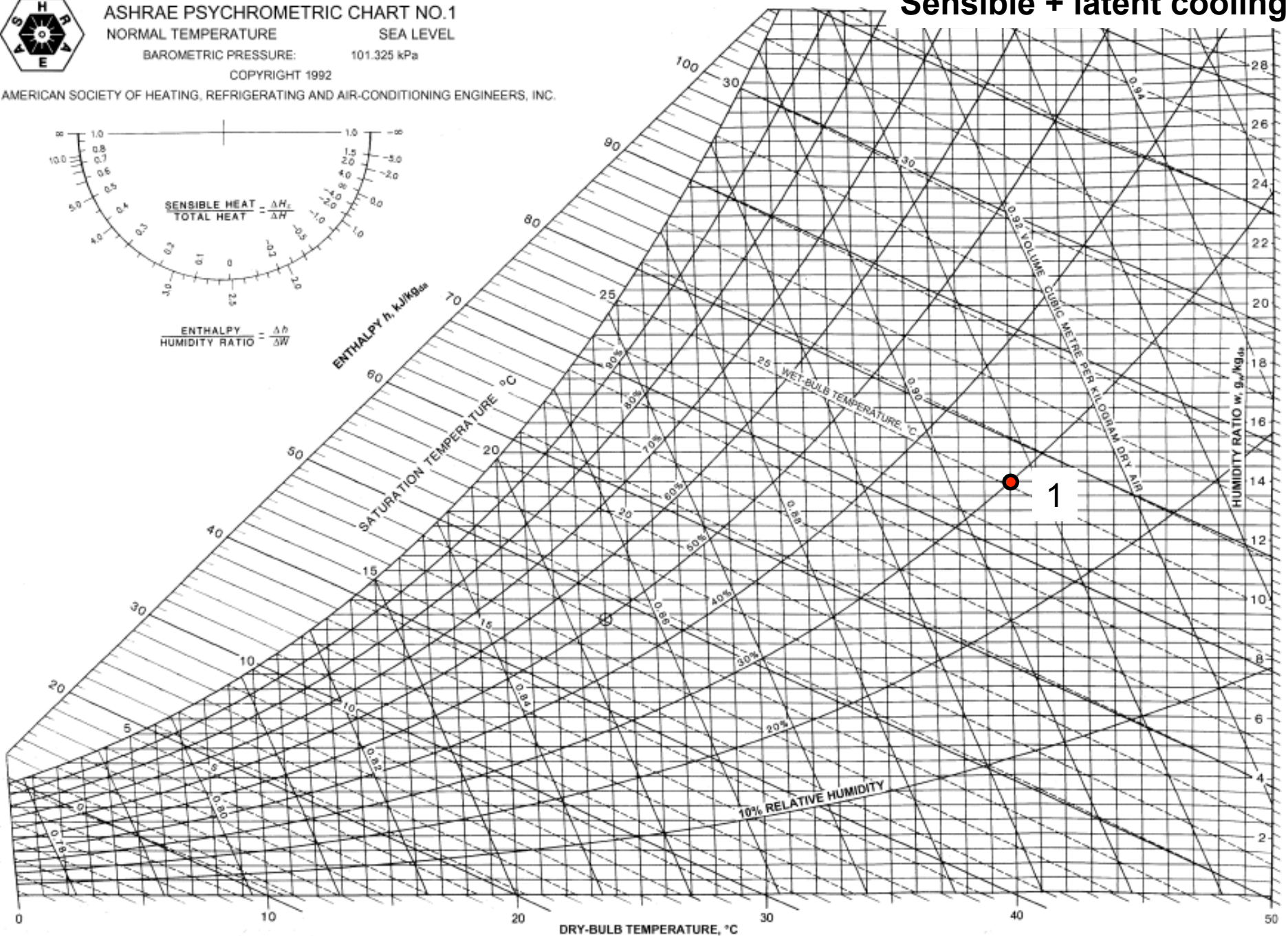
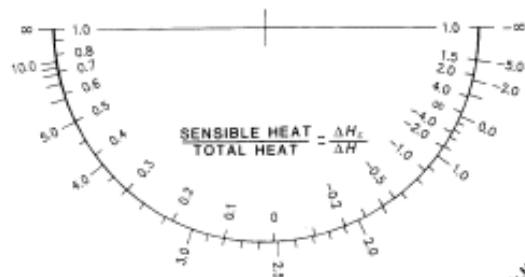
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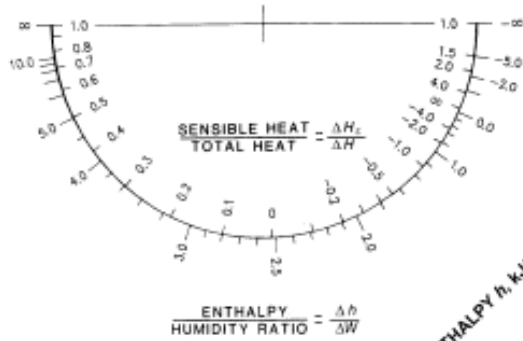
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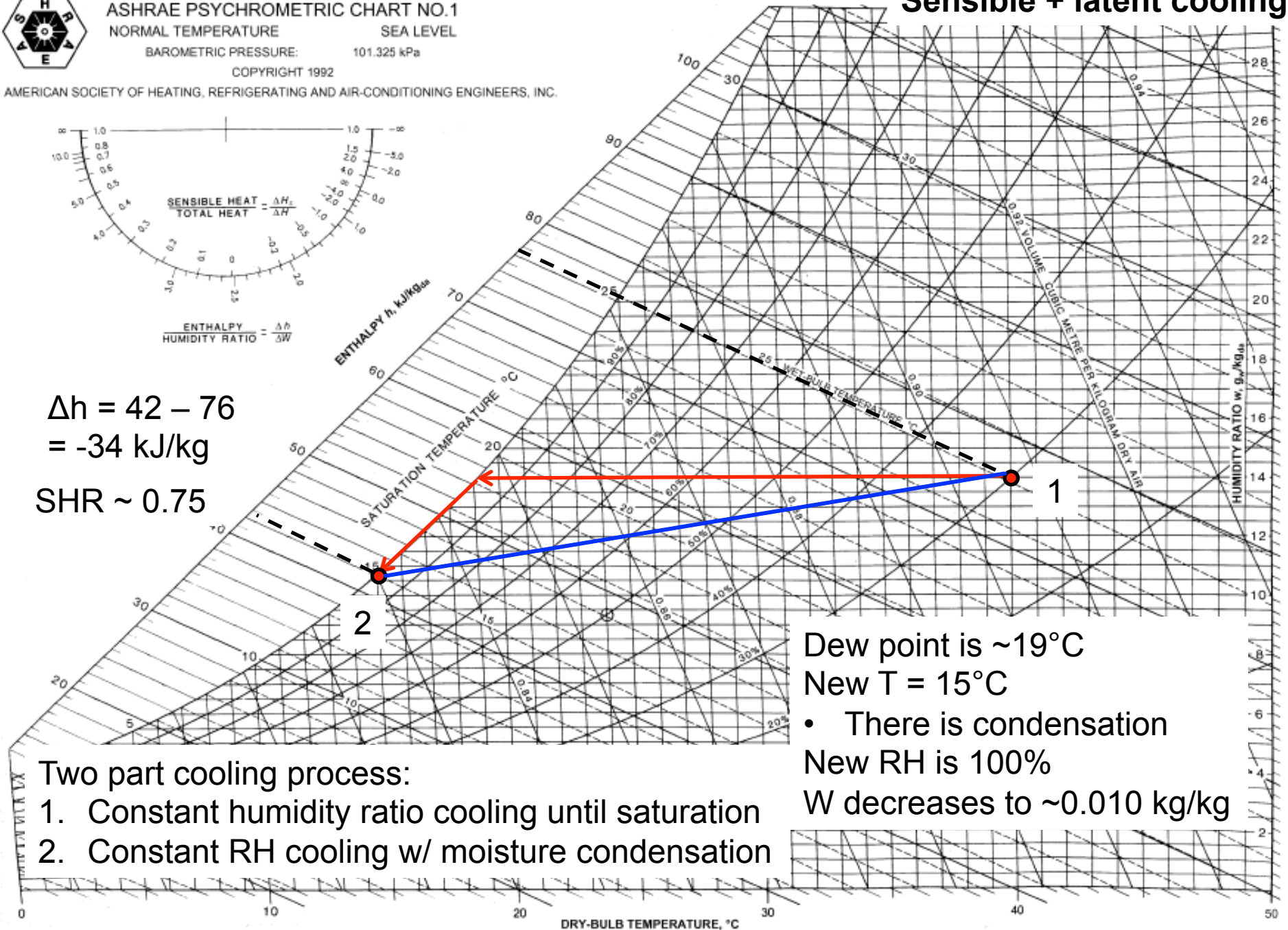
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$$\Delta h = 42 - 76$$

$$= -34 \text{ kJ/kg}$$

$$\text{SHR} \sim 0.75$$



Sensible + latent cooling

Two part cooling process:

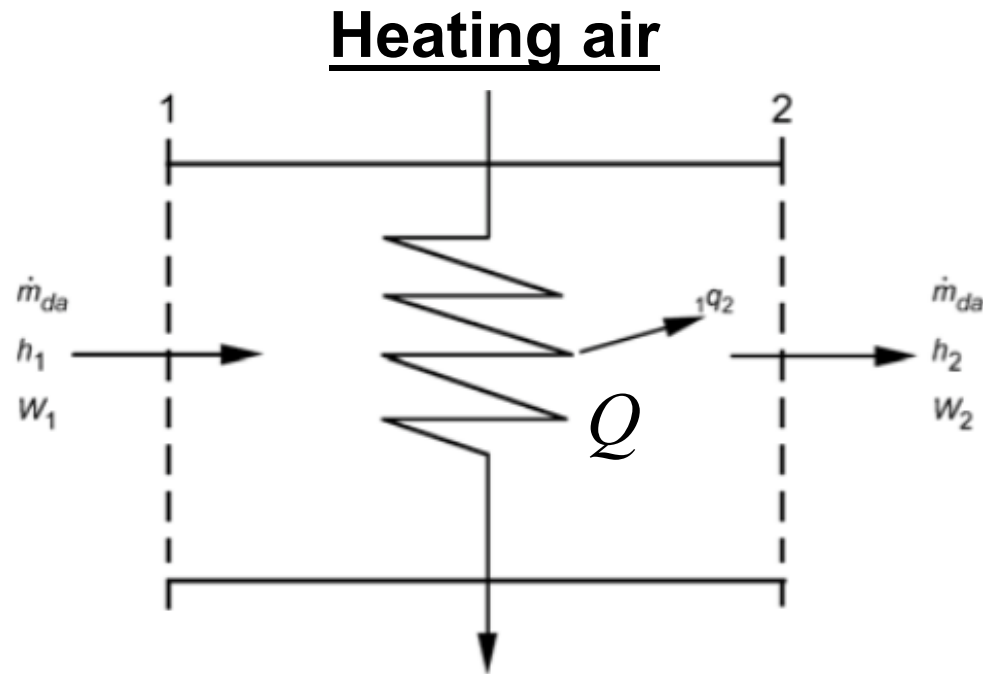
1. Constant humidity ratio cooling until saturation
2. Constant RH cooling w/ moisture condensation

Dew point is ~19°C

New T = 15°C

- There is condensation
- New RH is 100%
- W decreases to ~0.010 kg/kg

Energy balances for psychrometric processes



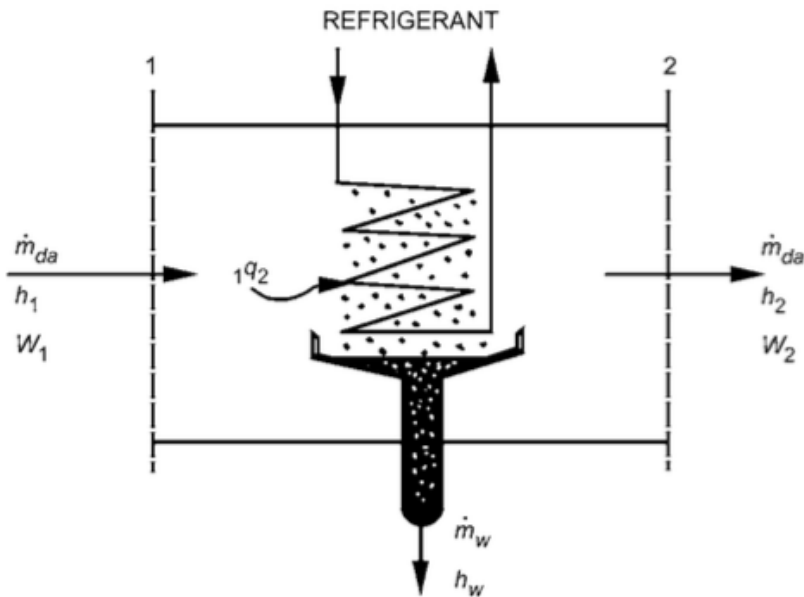
Energy balance: $\dot{m}_{da,1} h_1 + Q_{1 \rightarrow 2} = \dot{m}_{da,2} h_2$

Mass balance on air: $\dot{m}_{da,1} = \dot{m}_{da,2} = \dot{m}_{da}$

Mass balance on water vapor: $\dot{m}_{da,1} W_1 = \dot{m}_{da,2} W_2$

Therefore: $Q_{1 \rightarrow 2} = \dot{m}_{da} (h_2 - h_1)$

Energy balances for psychrometric processes



Cooling and dehumidifying

*Note that $h_w = h_g$ for steam/vapor and $h_w = h_f$ for water

Energy balance:
$$\dot{m}_{da,1} h_1 + Q_{1 \rightarrow 2} = \dot{m}_{da,2} h_2 + \dot{m}_w h_{w,2}$$

Mass balance on air:
$$\dot{m}_{da,1} = \dot{m}_{da,2} = \dot{m}_{da}$$

Mass balance on water vapor:
$$\dot{m}_{da,1} W_1 = \dot{m}_{da,2} W_2 + \dot{m}_w$$

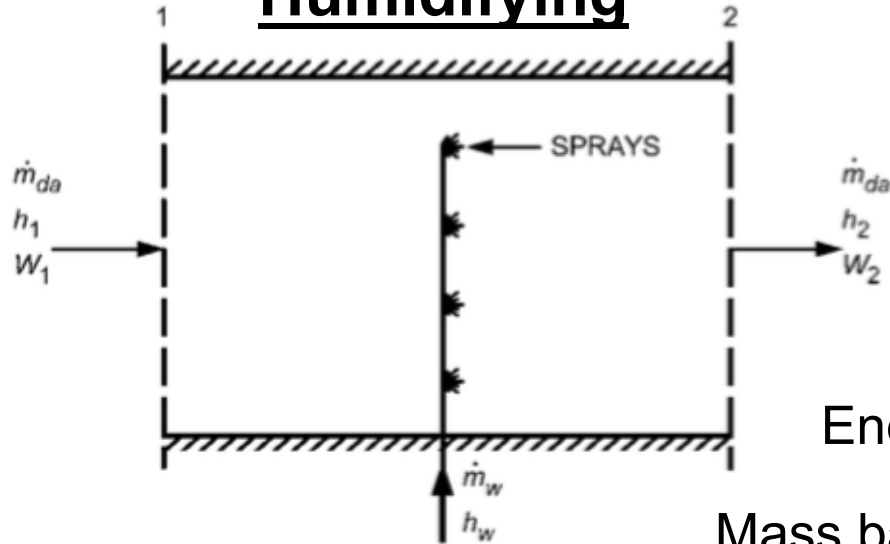
Therefore:
$$\dot{m}_w = \dot{m}_{da} (W_1 - W_2)$$

And:
$$Q_{1 \rightarrow 2} = \dot{m}_{da} [(h_2 - h_1) - (W_2 - W_1) h_{w,2}]$$

(Q is negative for cooling)

Energy balances for psychrometric processes

Humidifying



Energy balance:

$$\dot{m}_{da,1} h_1 + \dot{m}_w h_w = \dot{m}_{da,2} h_2$$

Mass balance on air:

$$\dot{m}_{da,1} = \dot{m}_{da,2} = \dot{m}_{da}$$

Mass balance on water vapor:

$$\dot{m}_{da,1} W_1 + \dot{m}_w = \dot{m}_{da,2} W_2$$

Therefore:

$$\dot{m}_w = \dot{m}_{da} (W_2 - W_1)$$

And:

$$\dot{m}_w h_w = \dot{m}_{da} (h_2 - h_1)$$

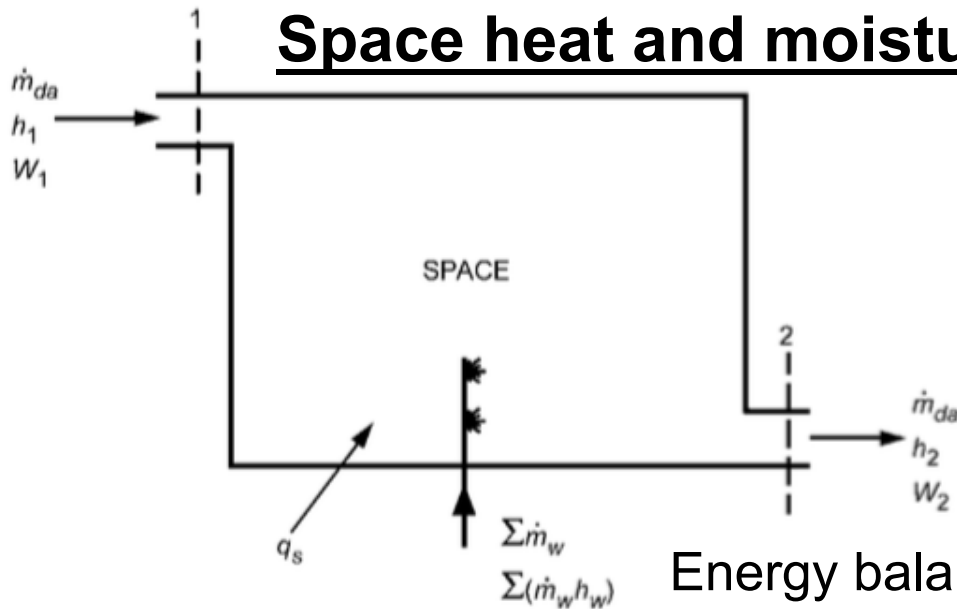
And:

$$\frac{h_2 - h_1}{W_2 - W_1} = \frac{\Delta h}{\Delta W} = h_w$$

*Note that $h_w = h_g$ for steam/vapor
and $h_w = h_f$ for water

Energy balances for psychrometric processes

Space heat and moisture gains



Energy balance: $\dot{m}_{da} h_1 + Q_{gains} + \Sigma \dot{m}_w h_w = \dot{m}_{da} h_2$

Mass balance on water vapor: $\dot{m}_{da} W_1 + \Sigma \dot{m}_w = \dot{m}_{da} W_2$

Therefore: $\Sigma \dot{m}_w = \dot{m}_{da} (W_2 - W_1)$

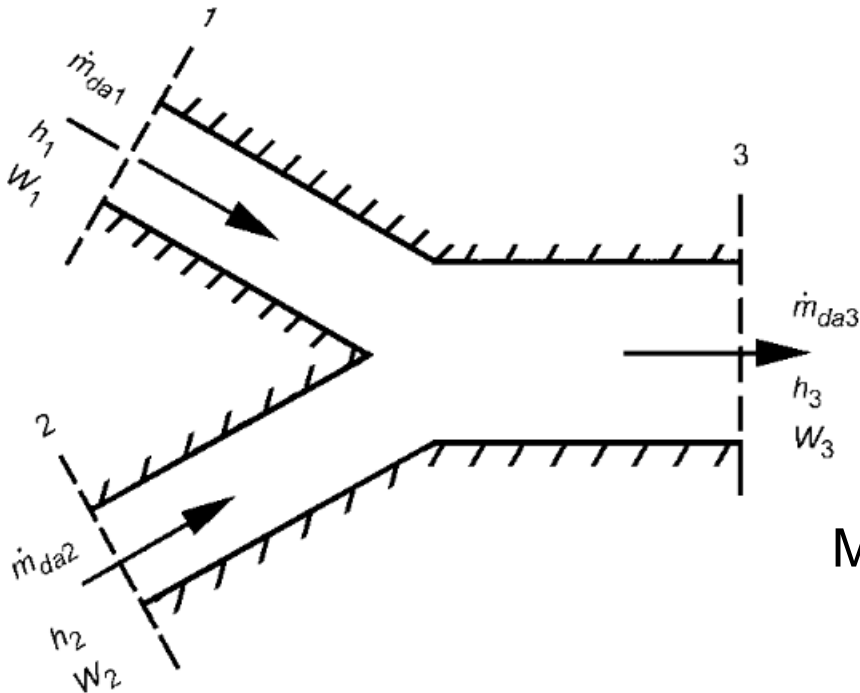
Therefore: $\Sigma \dot{m}_w h_w + Q_{gains} = \dot{m}_{da} (h_2 - h_1)$

*Note that $h_w = h_g$ for steam/vapor and $h_w = h_f$ for water

And:
$$\frac{\Delta h}{\Delta W} = \frac{\Sigma \dot{m}_w h_w + Q_{gains}}{\Sigma \dot{m}_w}$$

Mixing of air streams

- Often in HVAC systems we mix airstreams adiabatically
 - Adiabatically** = Without the addition or extraction of heat
 - e.g. outdoor air mixed with a portion of return/recirculated air



$$\text{Energy: } \dot{m}_{da,1} h_1 + \dot{m}_{da,2} h_2 = \dot{m}_{da,3} h_3$$

$$\text{Mass (air): } \dot{m}_{da,1} + \dot{m}_{da,2} = \dot{m}_{da,3}$$

$$\text{Mass (water): } \dot{m}_{da,1} W_1 + \dot{m}_{da,2} W_2 = \dot{m}_{da,3} W_3$$

$$\text{Therefore: } \frac{h_2 - h_3}{h_3 - h_1} = \frac{W_2 - W_3}{W_3 - W_1} = \frac{\dot{m}_{da,1}}{\dot{m}_{da,2}}$$

Mixing of air streams

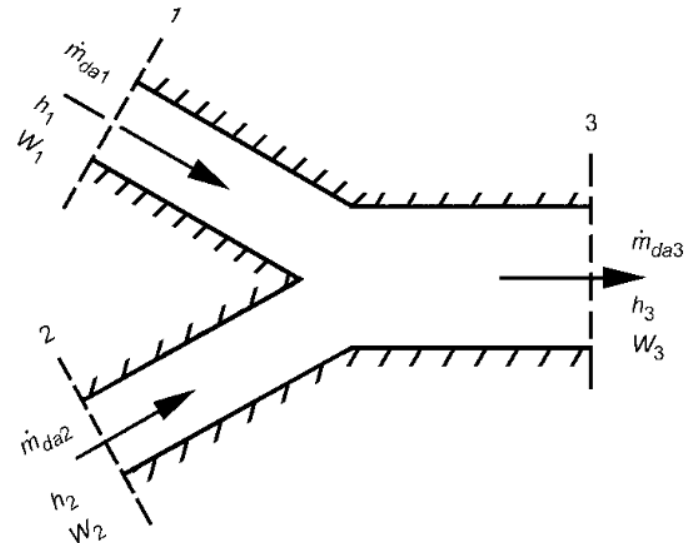
- For most parameters, the outlet conditions end up being the weighted averages of the input conditions based on their mass flow rates

- Dry bulb temperature
- Humidity ratio
- Enthalpy
- (not RH!)

$$T_3 = \frac{\dot{m}_{da1}T_1 + \dot{m}_{da2}T_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

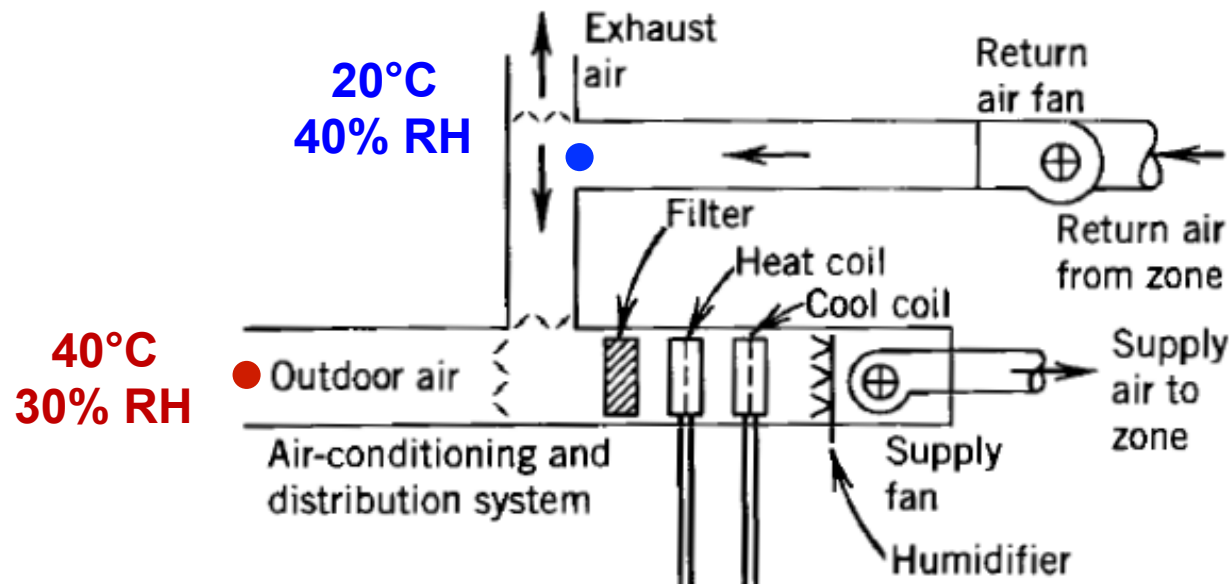
$$W_3 = \frac{\dot{m}_{da1}W_1 + \dot{m}_{da2}W_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

$$h_3 = \frac{\dot{m}_{da1}h_1 + \dot{m}_{da2}h_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$



Mixing of airstreams example

- Hot, humid outdoor air is mixed with recirculated indoor air at an outdoor air mass flow fraction of 35%
 - Q1: What is T , W , RH , and h at the mixed condition?





ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

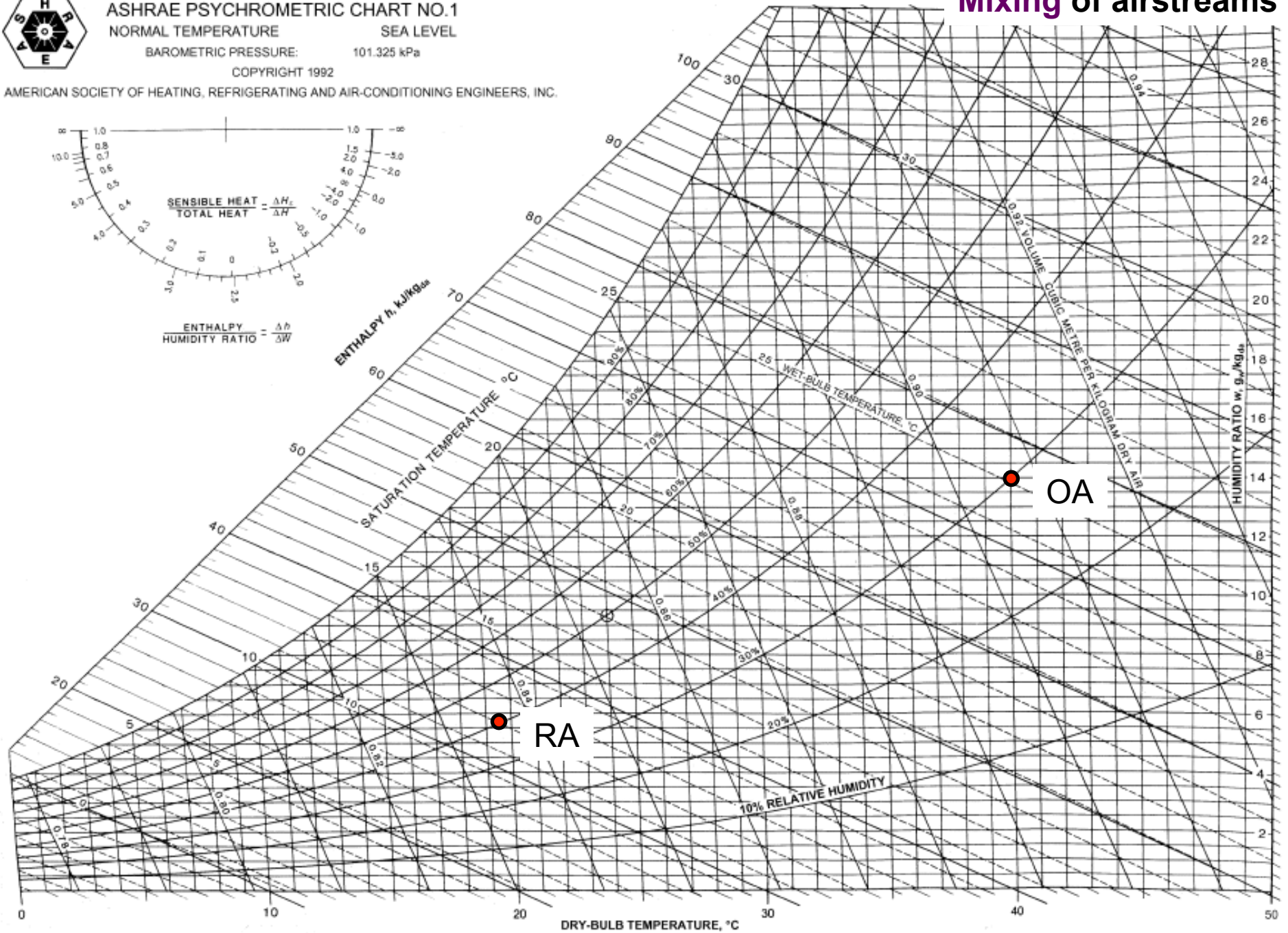
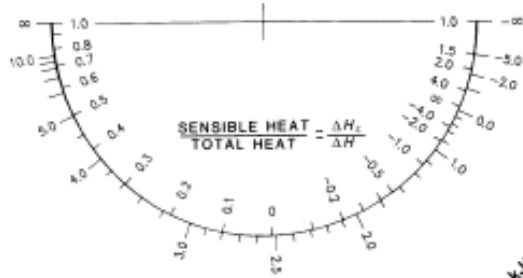
SEA LEVEL

BAROMETRIC PRESSURE:

101.325 kPa

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Mixing of airstreams



ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

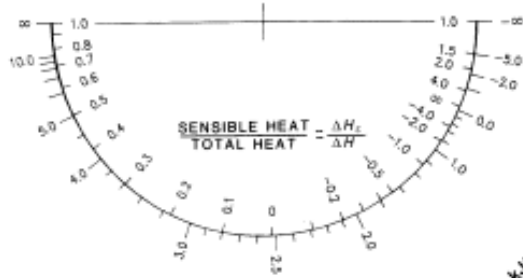
SEA LEVEL

BAROMETRIC PRESSURE:

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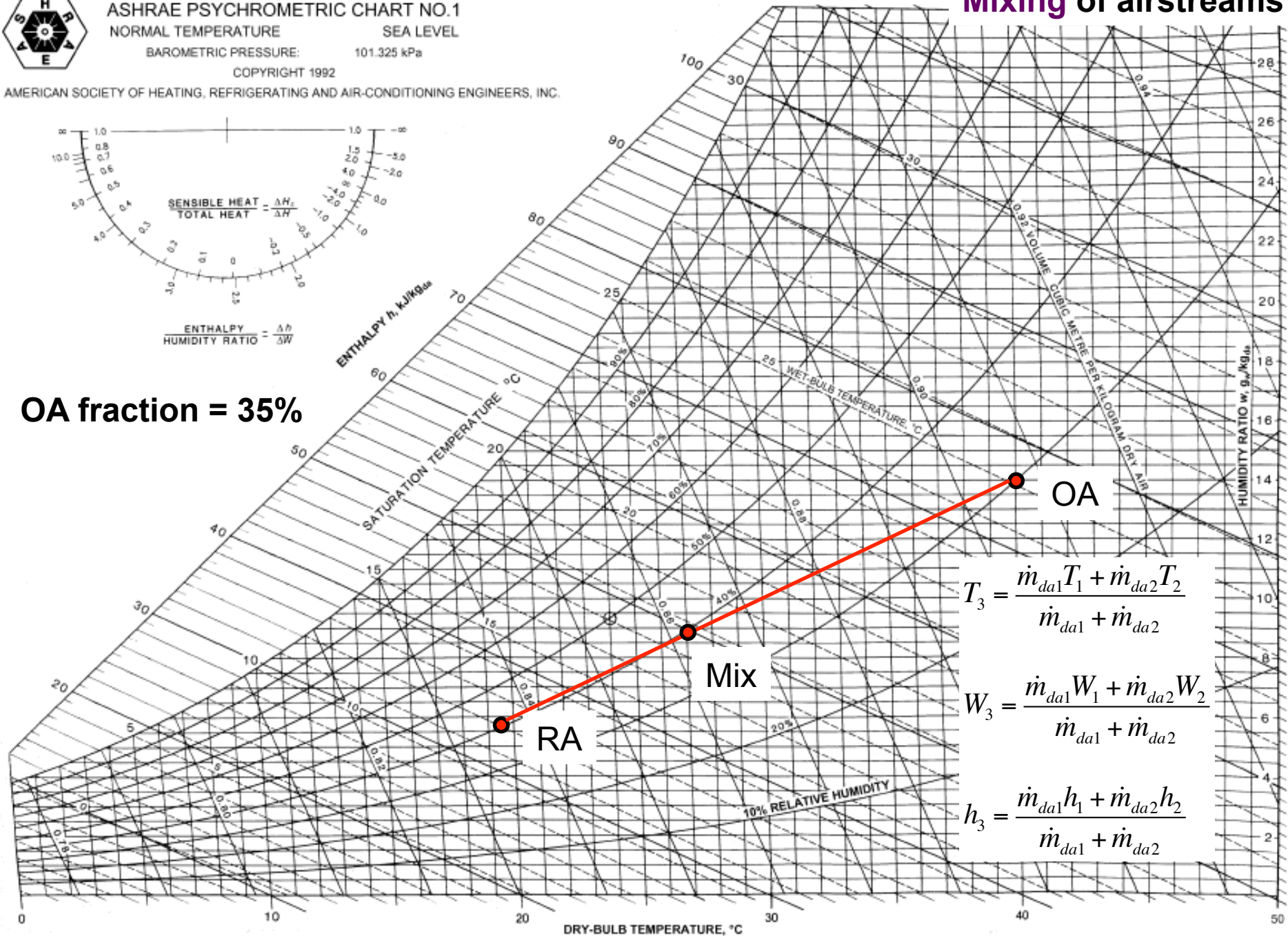
ENTHALPY h , kJ/kg_{da}

ENTHALPY h , kJ/kg_{da}

SATURATION TEMPERATURE, °C

OA fraction = 35%

Mixing of airstreams



$$T_3 = \frac{\dot{m}_{da1} T_1 + \dot{m}_{da2} T_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

$$W_3 = \frac{\dot{m}_{da1} W_1 + \dot{m}_{da2} W_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

$$h_3 = \frac{\dot{m}_{da1} h_1 + \dot{m}_{da2} h_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

DRY-BULB TEMPERATURE, °C

HUMIDITY RATIO w , g/kg_{da}

50



ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

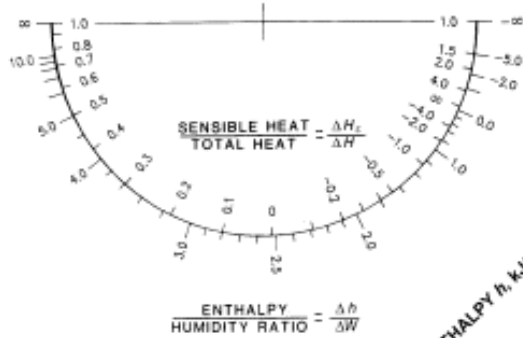
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101.325 kPa

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OA fraction = 35%

Mixing of airstreams

$$T_3 = \frac{0.65(20) + 0.35(40)}{1.0} = 27^\circ\text{C}$$

$$W_3 = \frac{0.65(6) + 0.35(14)}{1.0} = 8.8 \frac{\text{g}_w}{\text{kg}_{da}}$$

$$h_3 = \frac{0.65(34) + 0.35(77)}{1.0} = 49 \frac{\text{kJ}}{\text{kg}_{da}}$$

Notice:
35% this way →

← 65% this way

RA

Mix

OA

$$T_3 = \frac{\dot{m}_{da1}T_1 + \dot{m}_{da2}T_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

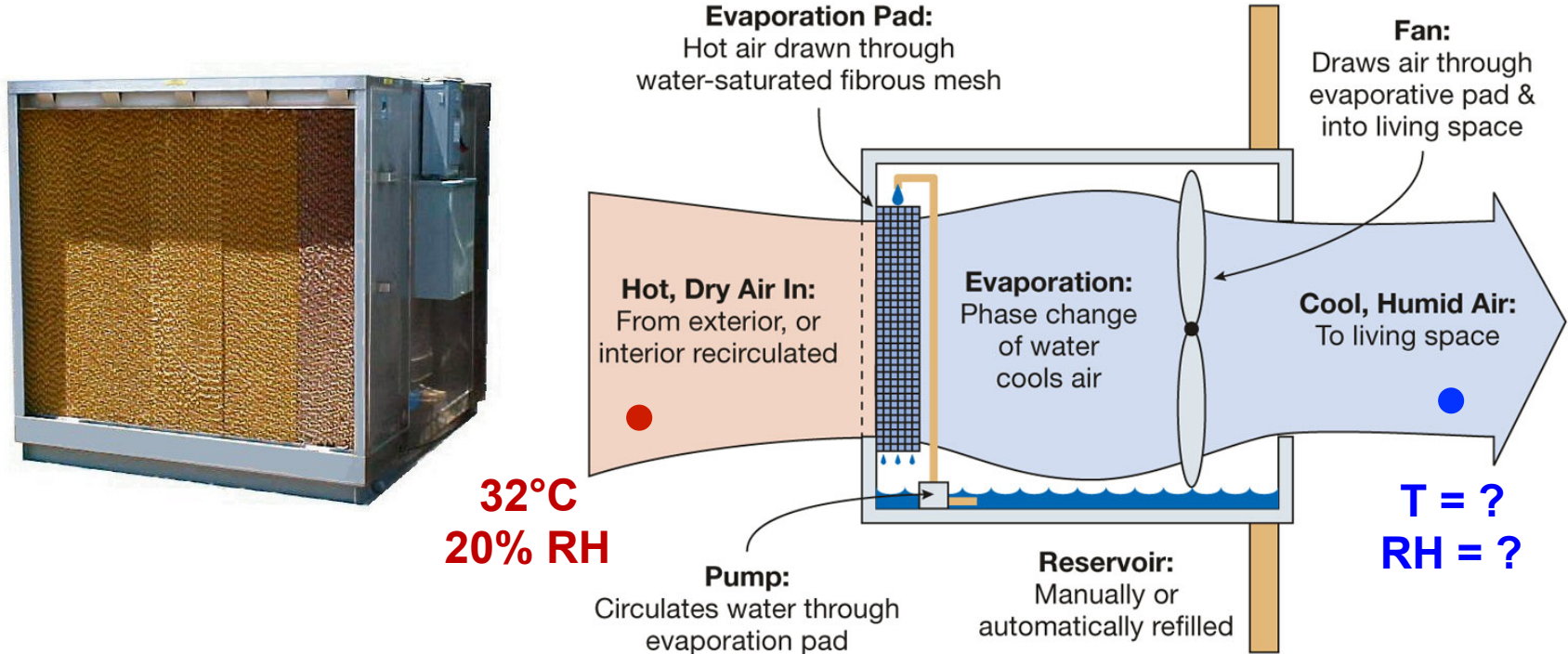
$$W_3 = \frac{\dot{m}_{da1}W_1 + \dot{m}_{da2}W_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

$$h_3 = \frac{\dot{m}_{da1}h_1 + \dot{m}_{da2}h_2}{\dot{m}_{da1} + \dot{m}_{da2}}$$

DRY-BULB TEMPERATURE, °C

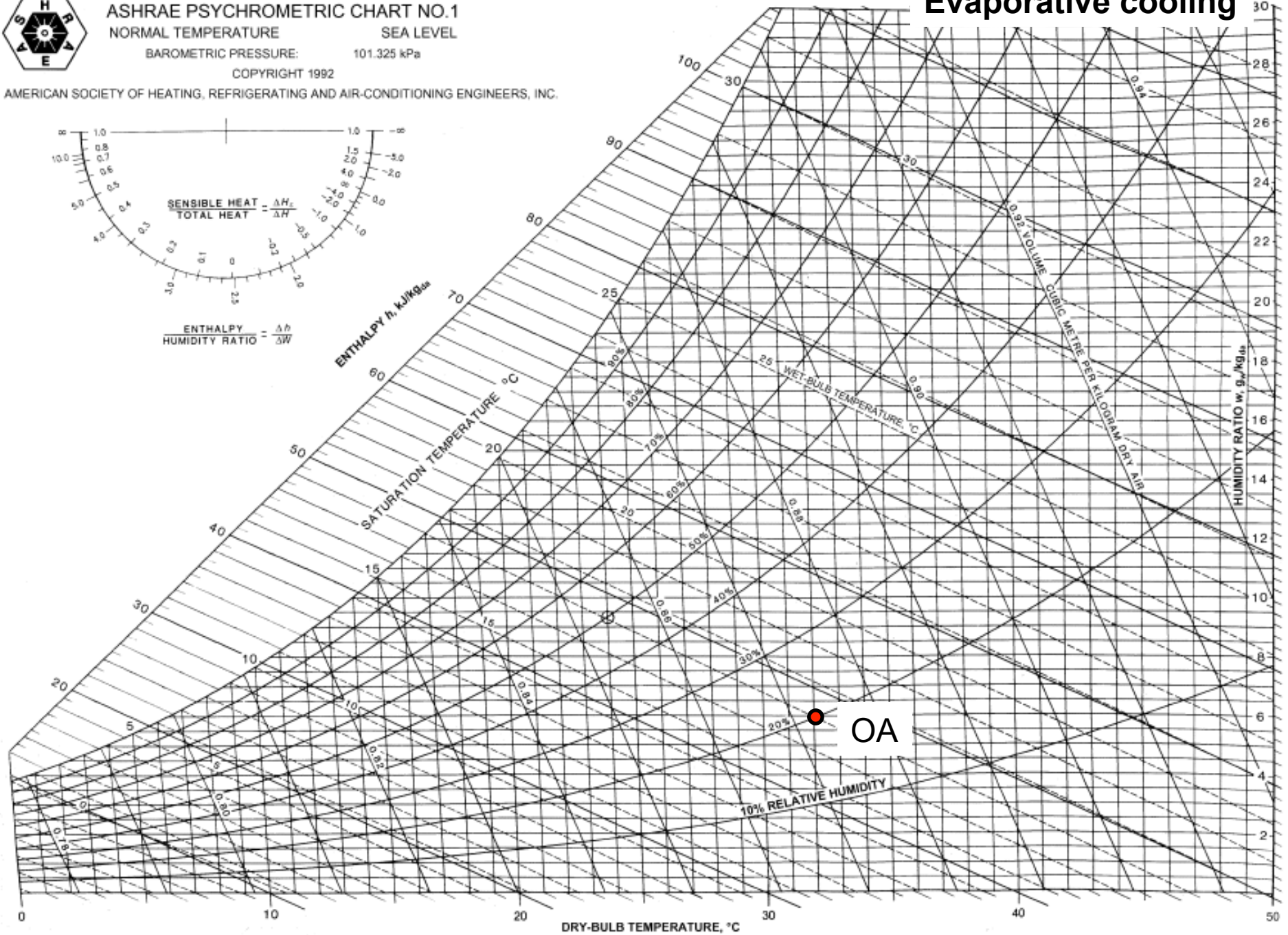
Evaporative **cooling** example

- Hot, dry outdoor air is cooled with an evaporative cooler, or “swamp cooler”
 - Q1: What is the T, RH, and W of the supply air?**
 - Q2: Why would we choose this system?**





$$\frac{\text{ENTHALPY}}{\text{HUMIDITY RATIO}} = \frac{\Delta h}{\Delta W}$$





ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

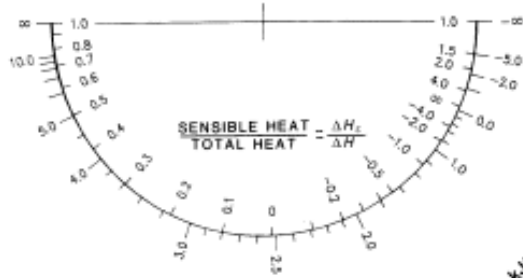
SEA LEVEL

BAROMETRIC PRESSURE:

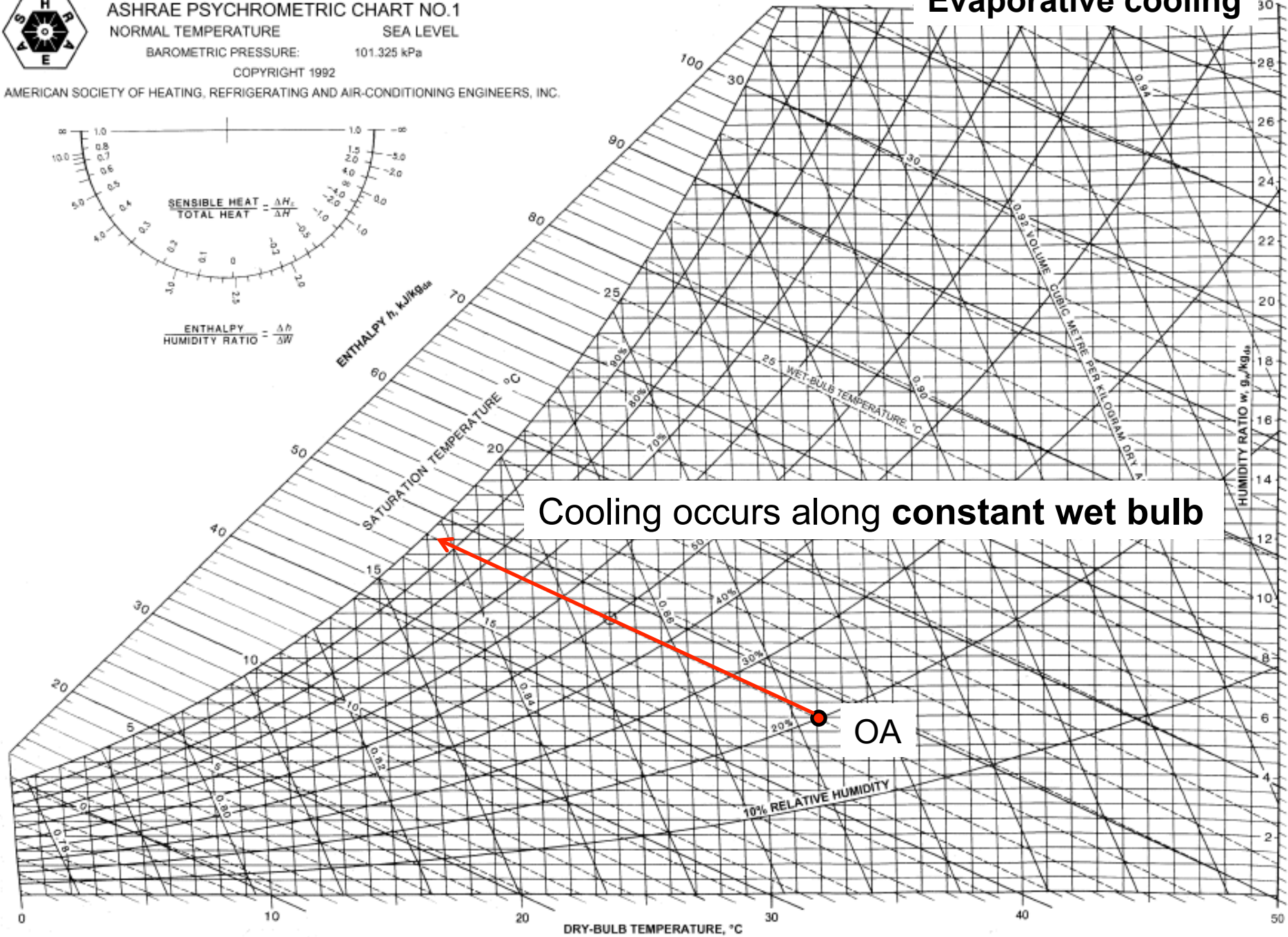
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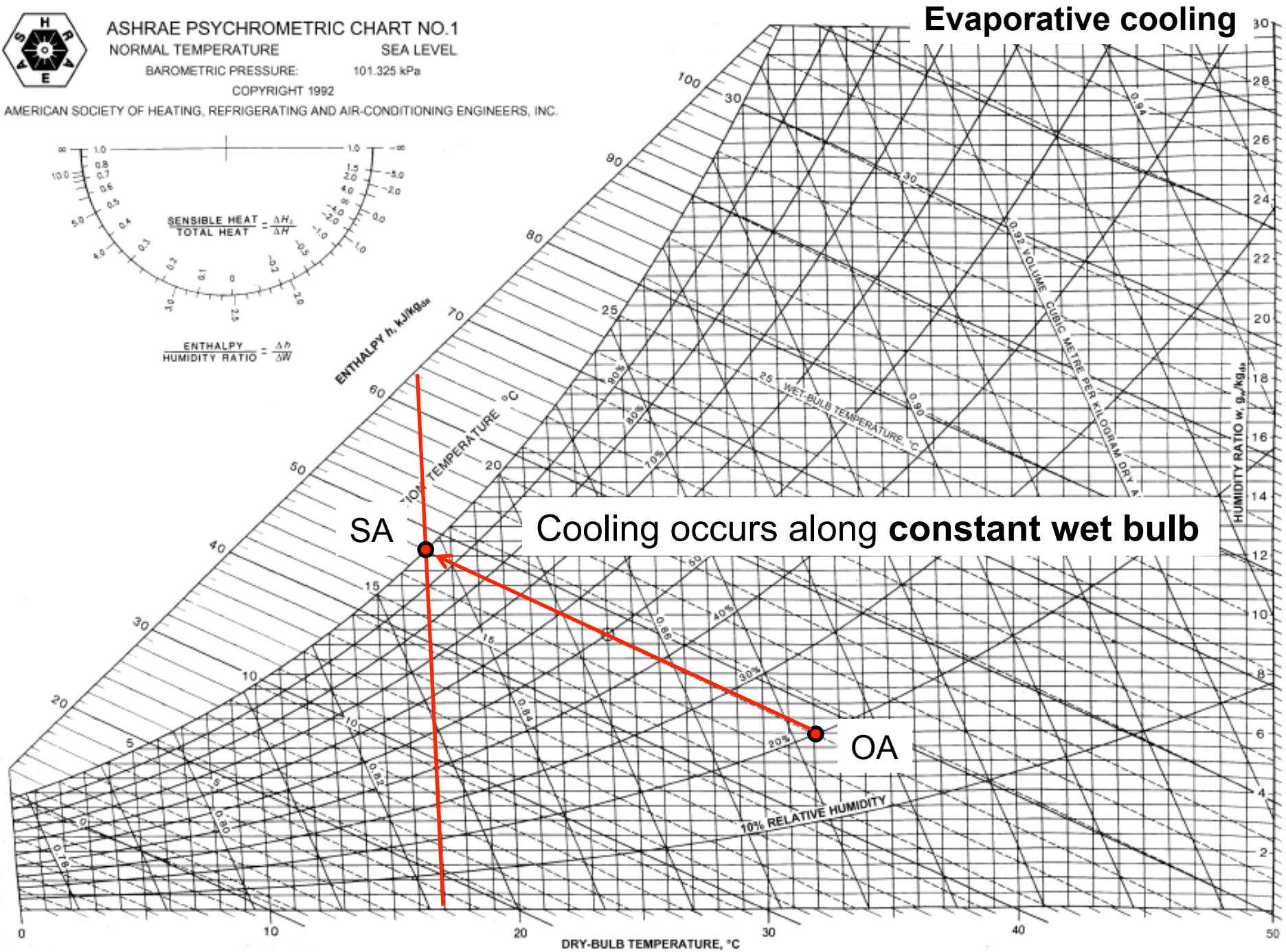
Evaporative cooling





The chart is a semi-circular scale with the following features:

- Top Horizontal Axis:** Labeled $\frac{\text{SENSIBLE HEAT}}{\text{TOTAL HEAT}} = \frac{\Delta H_s}{\Delta H}$. It has two scales: the top scale from 0.0 to 1.0, and the bottom scale from -5.0 to 5.0.
- Inner Curved Axis:** Labeled $\frac{\text{ENTHALPY}}{\text{HUMIDITY RATIO}} = \frac{\Delta h}{\Delta W}$. It has a scale from 0.0 to 10.0.
- Outer Curved Axis:** Labeled $\text{ENTHALPY } h, \text{ KJ/Kg}$. It has a scale from -2.0 to 15.0.
- Center:** Marked with 0.





ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

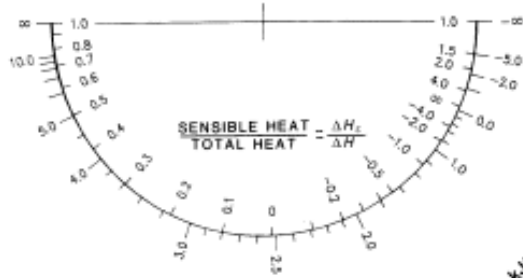
SEA LEVEL

BAROMETRIC PRESSURE:

101.325 kPa

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$$\frac{\text{ENTHALPY}}{\text{HUMIDITY RATIO}} = \frac{\Delta h}{\Delta W}$$

ENTHALPY h , kJ/kg_{da}

TEMPERATURE °C

SA

RH near 100%
 $W = \sim 12.2 \text{ g}_w/\text{kg}_{da}$
 $\Delta h = 0$

OA

10% RELATIVE HUMIDITY

DRY-BULB TEMPERATURE, °C

Evaporative cooling

HUMIDITY RATIO w , g_w/kg_{da}

0.92 VOLUME CUBIC METRE PER KILOGRAM DRY AIR



ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

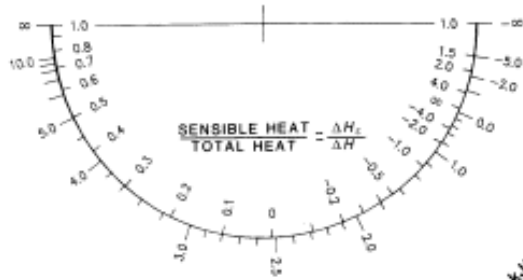
SEA LEVEL

BAROMETRIC PRESSURE:

101.325 kPa

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ENTHALPY h , kJ/kg_{da}

ENTHALPY h , kJ/kg_{da}

TEMPERATURE °C

SA

RH near 100%

$W = \sim 12.2 \text{ g}_w/\text{kg}_{da}$

$\Delta h = 0$

OA

$\Delta h = 0$ means no energy is required other than for fans (for air) and pumps (for water)

DRY-BULB TEMPERATURE, °C

Evaporative cooling

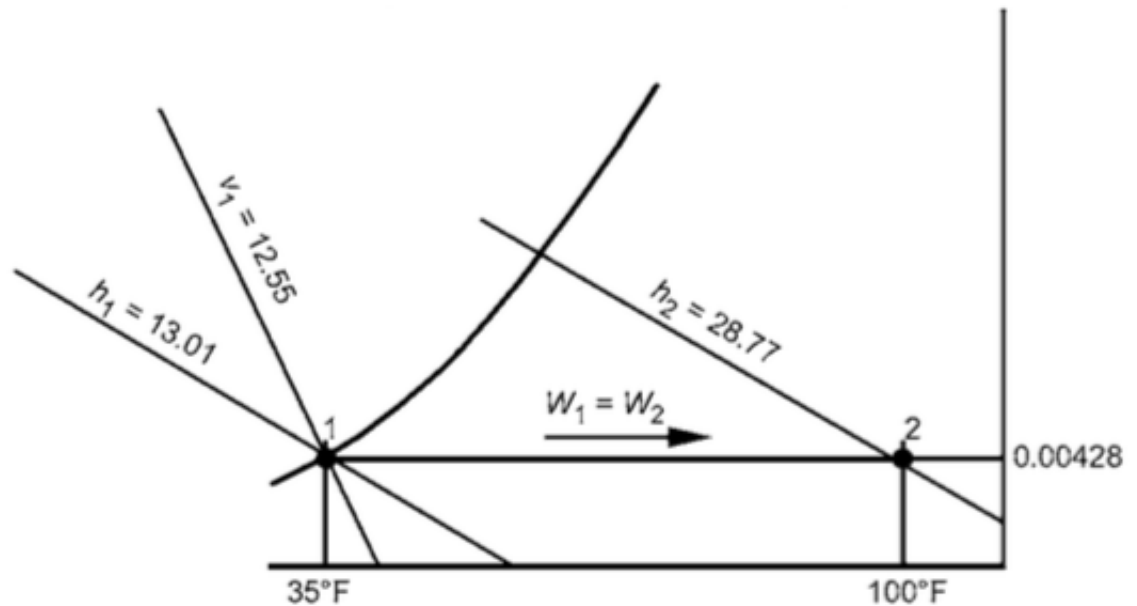
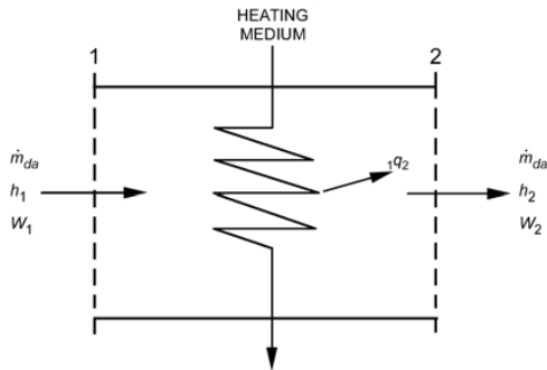
HUMIDITY RATIO w , g_w/kg_{da}

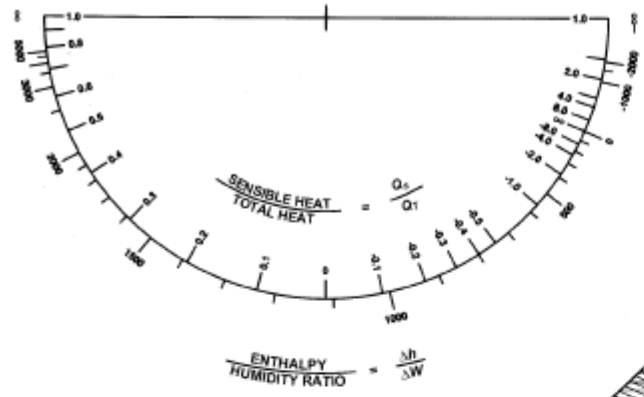
40

50

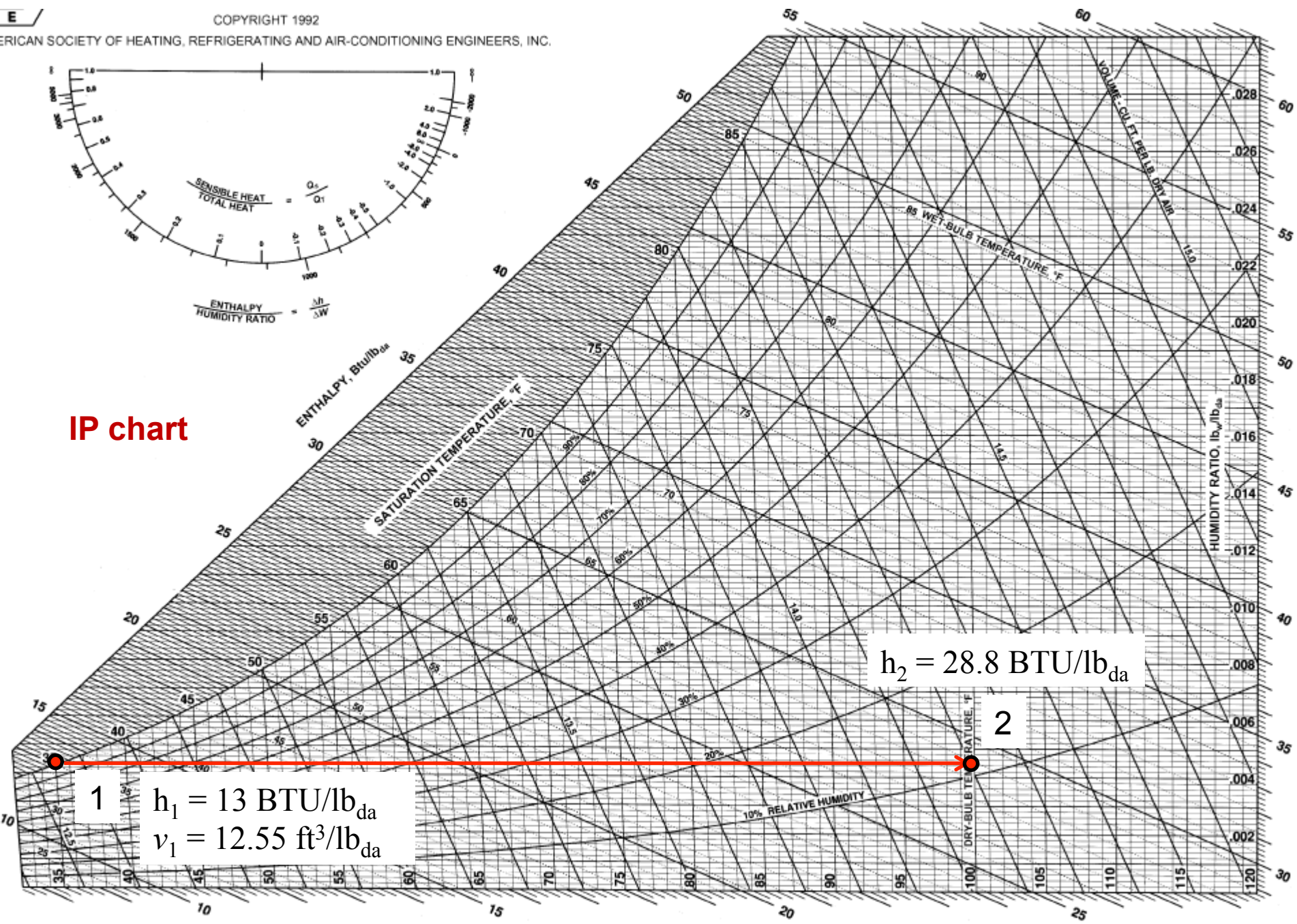
IP unit examples

- Moist air, saturated at 35°F, enters a heating coil at a rate of 20,000 CFM and air leaves the coil at 100°F
 - What process is this?
 - Find the required rate of heat addition





IP chart



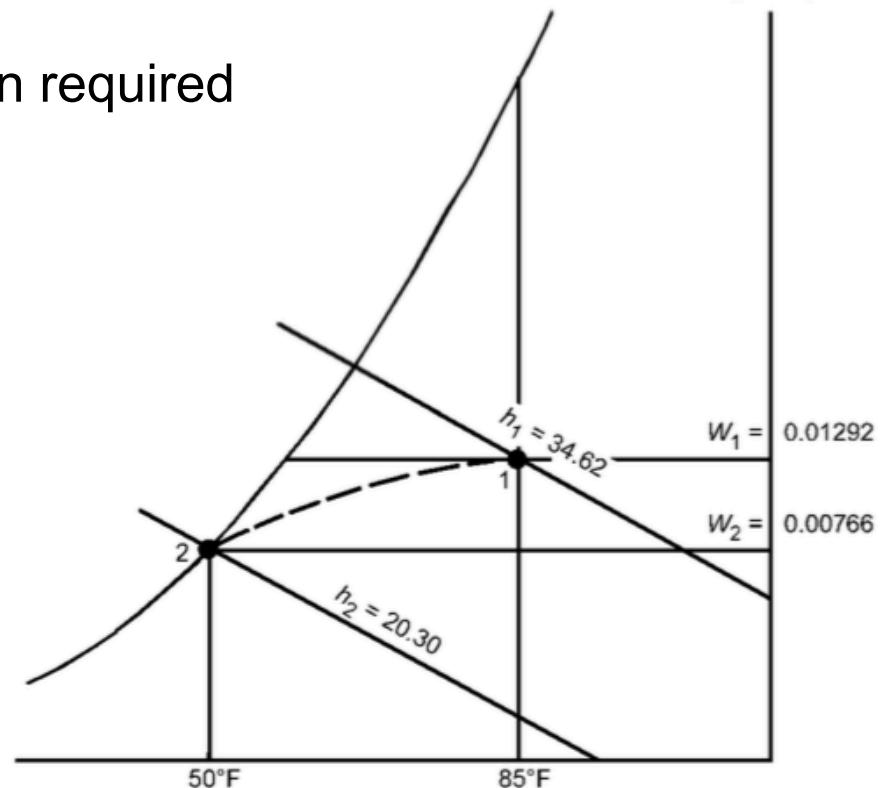
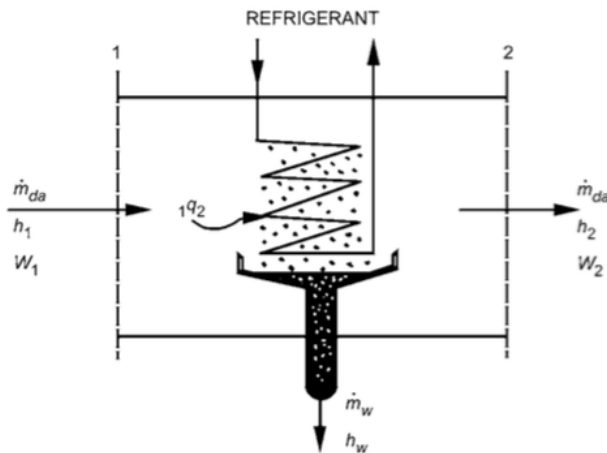
1 $h_1 = 13 \text{ BTU/lb}_{da}$
 $v_1 = 12.55 \text{ ft}^3/\text{lb}_{da}$

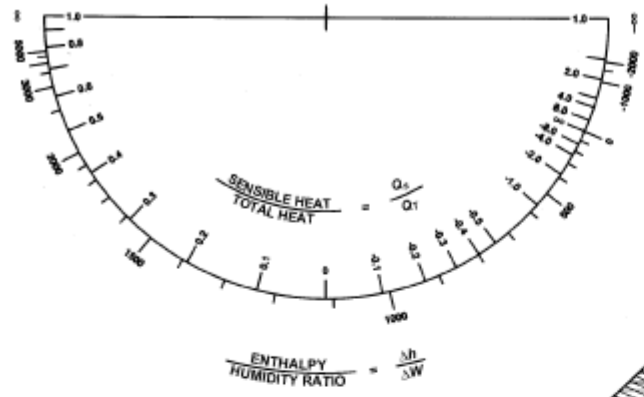
$h_2 = 28.8 \text{ BTU/lb}_{da}$

2

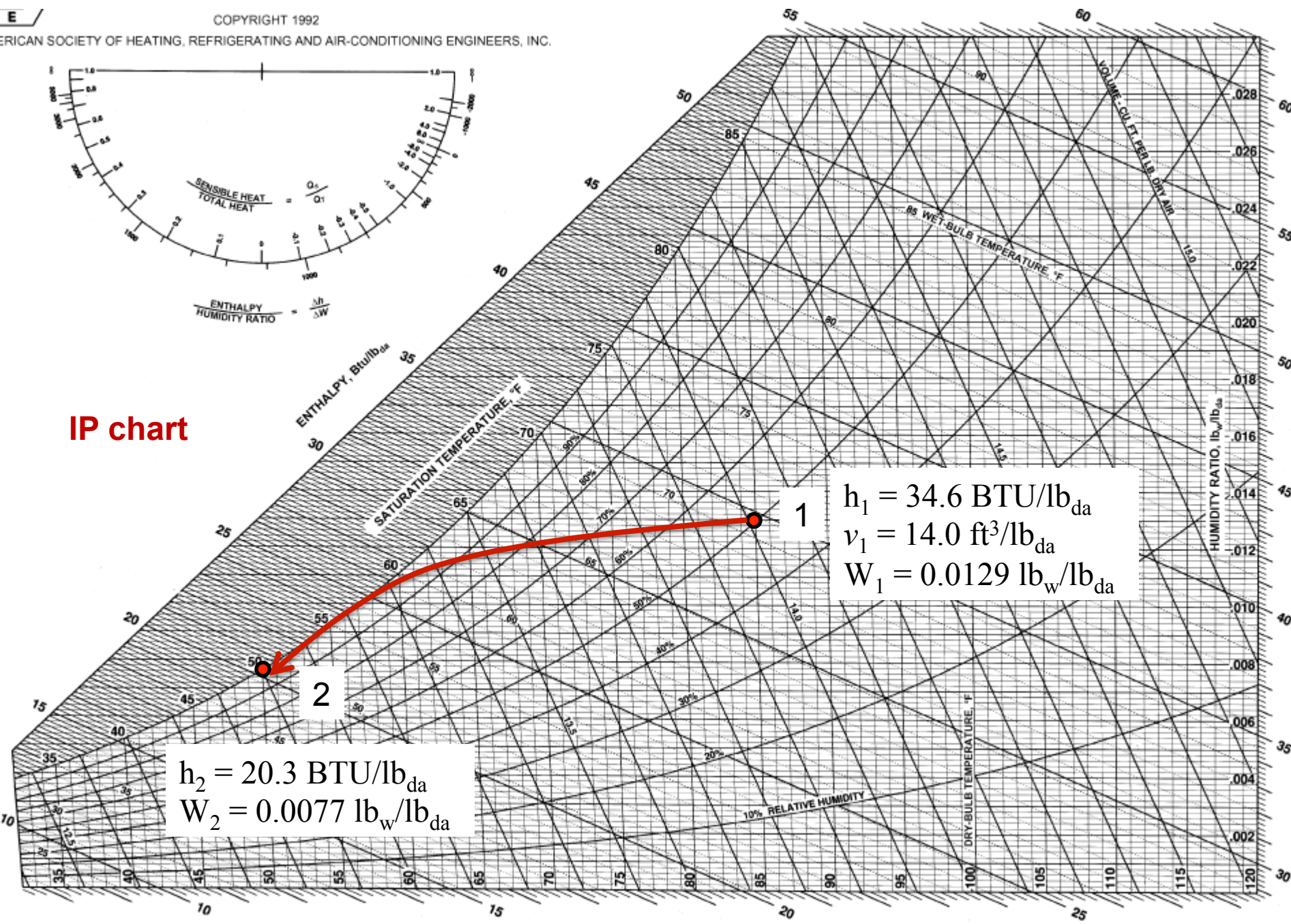
IP unit examples

- Moist air at 85°F dry-bulb temperature and 50% RH enters a cooling coil at 10,000 CFM and is processed to final saturation conditions at 50°F
 - What processes is this?
 - Find the tons of refrigeration required



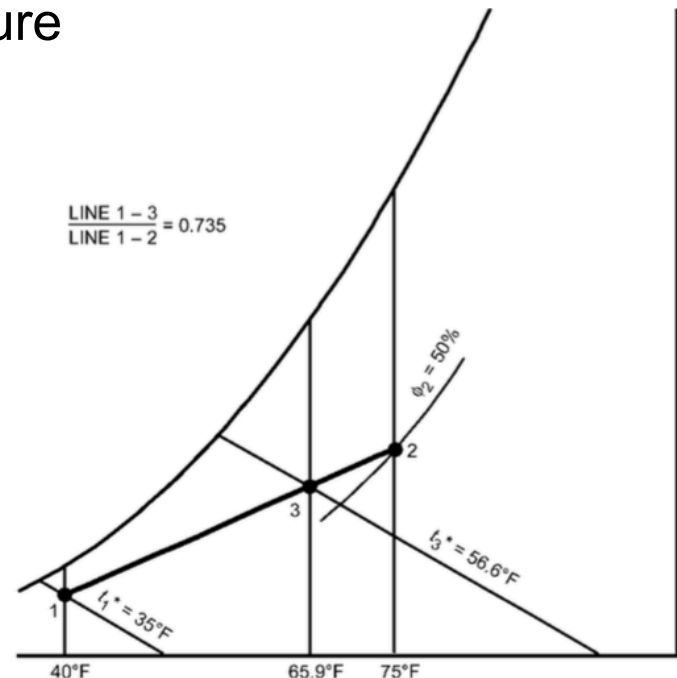
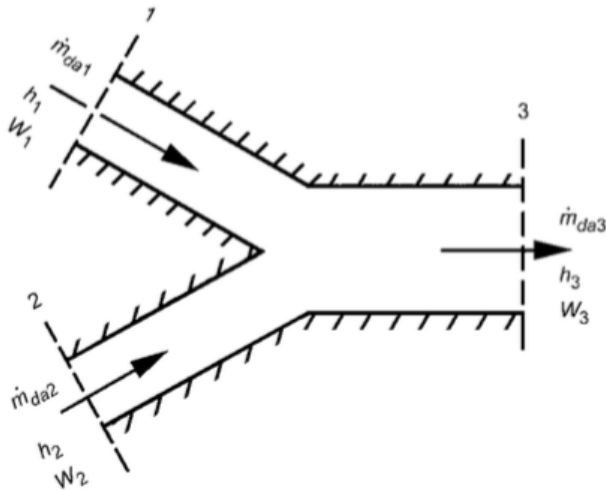


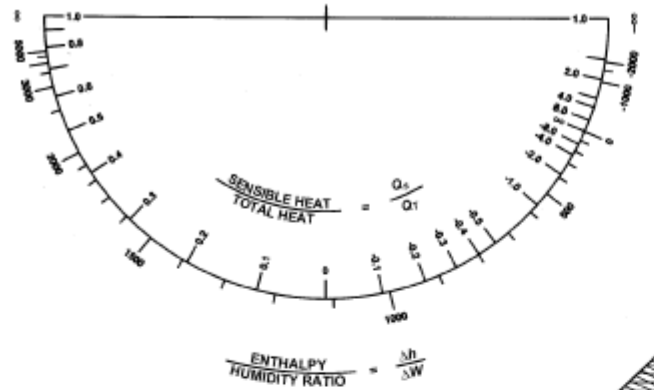
IP chart



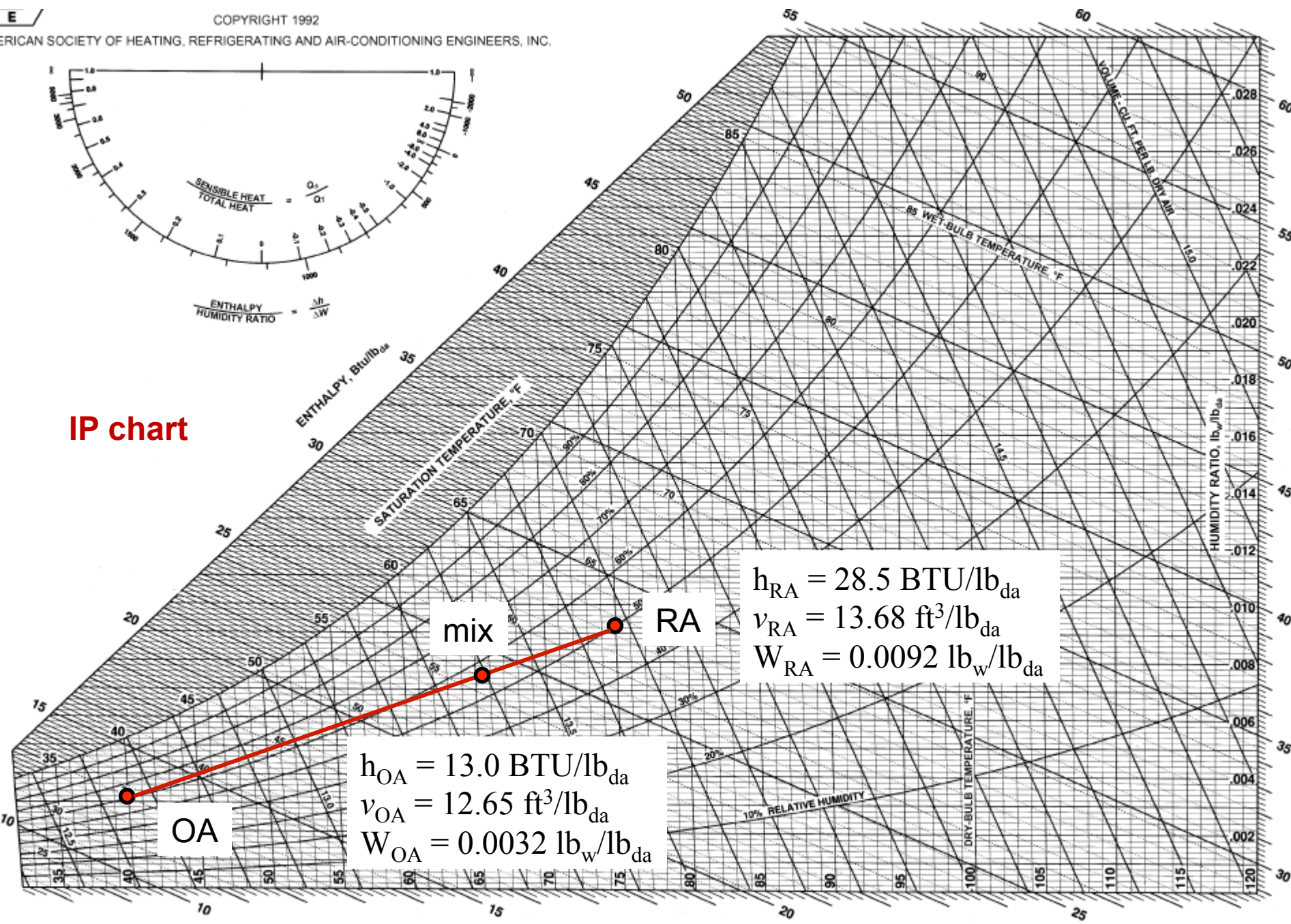
IP unit examples

- A stream of 5000 CFM of outdoor air at 40°F dry bulb temperature and 35°F thermodynamic wet bulb temperature is adiabatically mixed with 15,000 CFM of recirculated air at 75°F dry bulb temperature and 50% RH
 - What processes is this?
 - Find the dry bulb temperature and thermodynamic wet bulb temperature of the resulting mixture



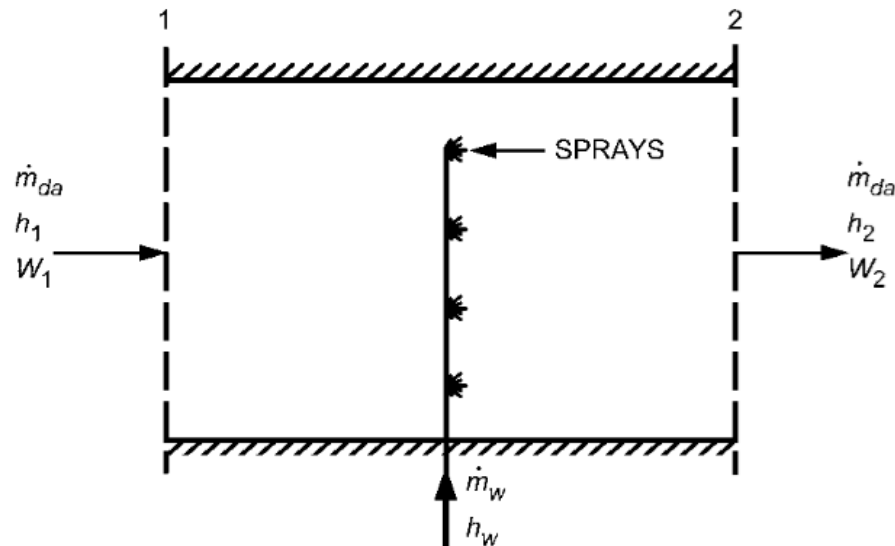


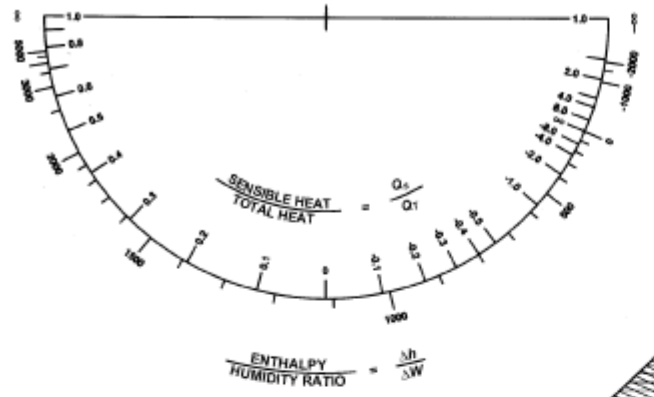
IP chart



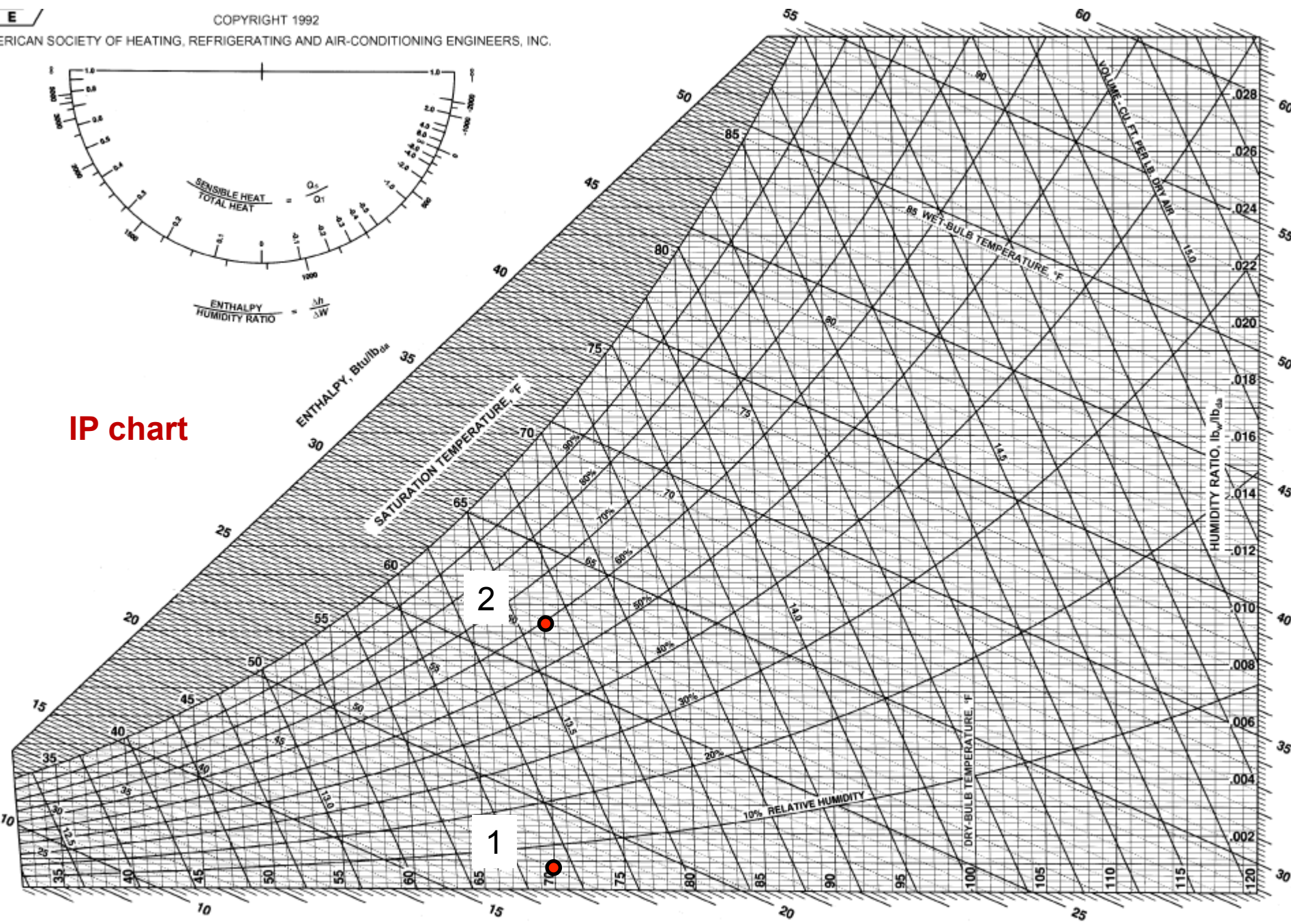
IP unit examples

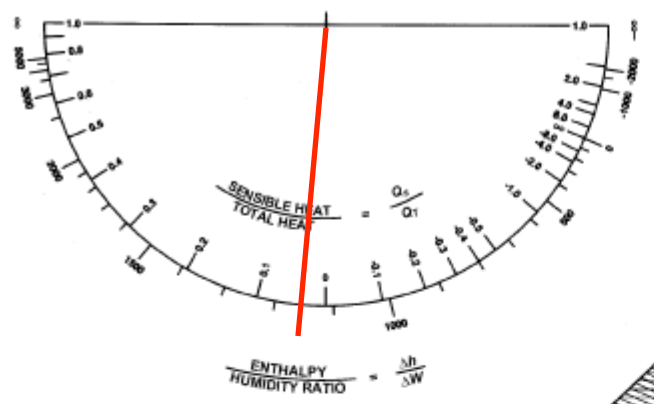
- Moist air at 70°F dry bulb temperature and 45°F wet bulb temperature is to be processed to a final dew point of 55°F by adiabatic injection of saturated steam at 230°F
- The air flow rate is 10,000 CFM
 - Find the rate of steam flow required



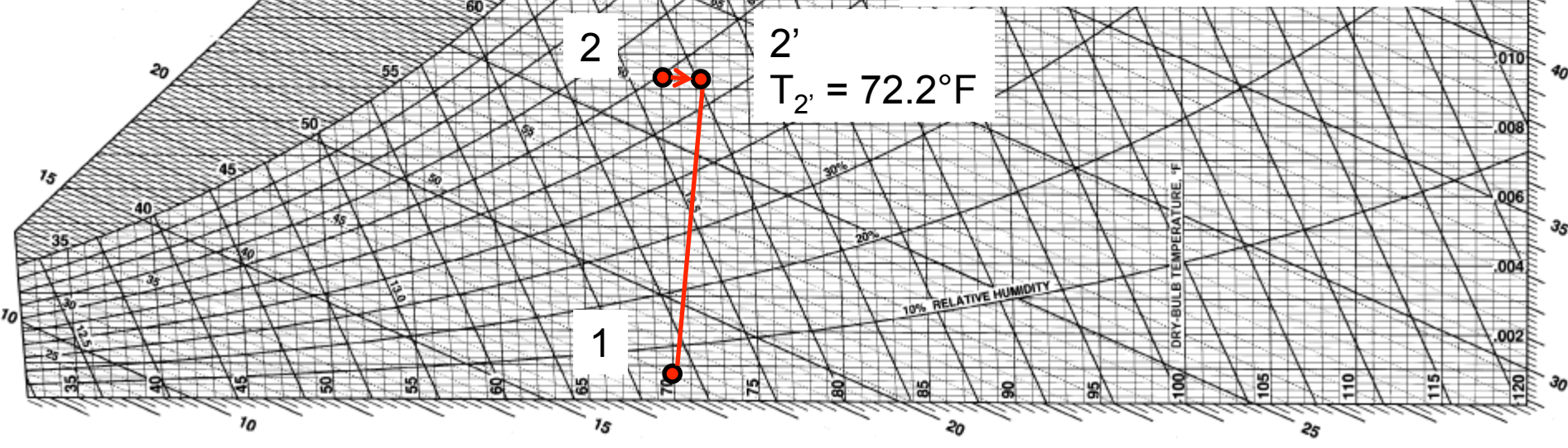
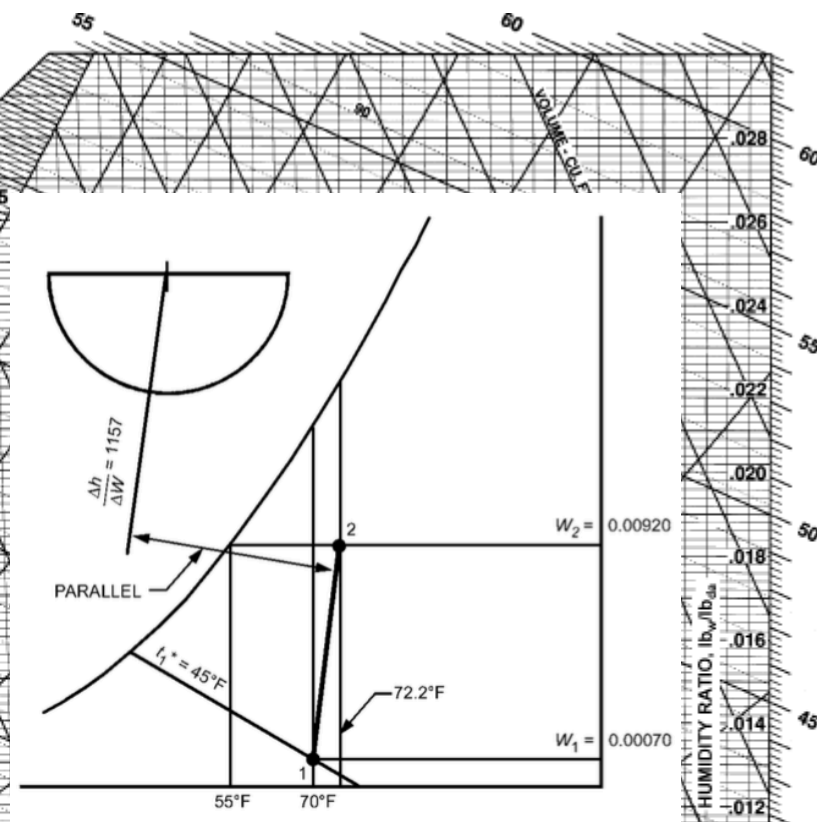


IP chart





$$\frac{\Delta h}{\Delta W} = 1157 \frac{\text{BTU}}{\text{lb}_w}$$



2' T_{2'} = 72.2°F

HW 4 assigned

- HW 4 assigned, due Tuesday, October 18