

# Predictions and determinants of size-resolved particle infiltration factors in single-family homes in the U.S.

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Zeineb El Orch<sup>1</sup>, Michael Waring<sup>2</sup>, **Brent Stephens<sup>1</sup>**

<sup>1</sup>Civil, Architectural and Environmental Engineering, Illinois Institute of Technology, Chicago, IL

<sup>2</sup>Civil, Architectural and Environmental Engineering, Drexel University, Philadelphia, PA



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## The Built Environment Research Group

advancing energy, environmental, and sustainability  
research within the built environment  
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**web** [www.built-envi.com](http://www.built-envi.com) **email** [brent@iit.edu](mailto:brent@iit.edu) **twitter** [@built\\_envi](https://twitter.com/built_envi)

# Motivation: Health effects and outdoor PM

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- Epidemiological studies show associations between elevated **outdoor** particulate matter (PM) and adverse health effects
  - PM<sub>10</sub>, PM<sub>2.5</sub>, and ultrafine particles (UFP, < 100 nm)

Pope et al., **2002** *J Am Med Assoc*; Pope and Dockery, **2006** *J Air Waste Manag Assoc*; Miller et al., **2007** *New Engl J Med*; Stölzel et al., **2007** *J Expo Sci Environ Epidem*; Andersen et al., **2010** *Eur Heart J*; Brook et al. **2010** *Circulation*; and many others

- But we spend most of our time **indoors**
  - ~87% of the time on average (**~69% at home**)

Klepeis et al., **2001** *J Expo Anal Env Epi*

- Outdoor particles can infiltrate and persist in homes with varying efficiencies

Chen and Zhao, **2011** *AE*; Williams et al., **2003** *AE*; Kearney et al., **2010** *AE*

# Motivation: Exposure misclassification

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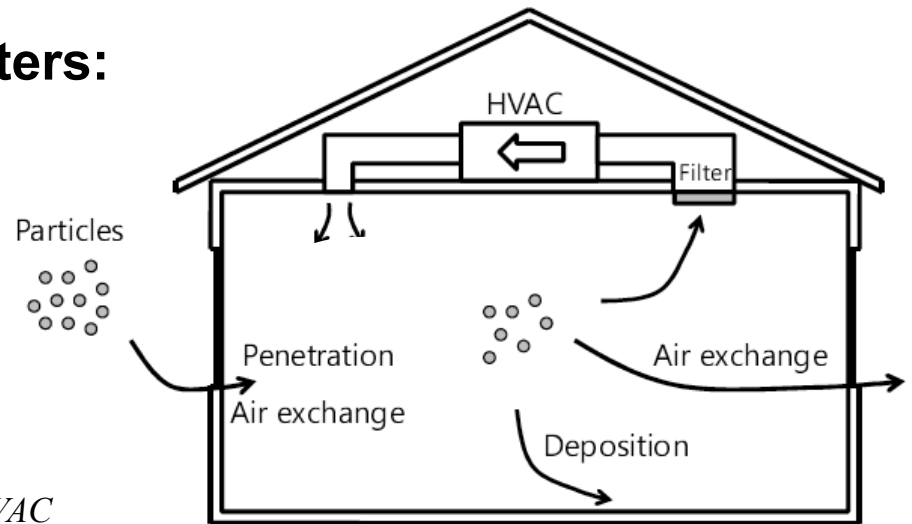
- Much of our exposure to outdoor PM often occurs **indoors**
  - **Often at home** Meng et al., **2005** *J Expo Anal Environ Epidemiol*; Kearney et al., **2010** *Atmos Environ*; Wallace and Ott **2011** *J Expo Sci Environ Epidemiol*; MacNeill et al. **2012** *Atmos Environ*
- Failing to account for differences in indoor proportions of outdoor particles can result in large **exposure misclassifications** Baxter et al. **2010** *JESEE*; Meng et al. **2005** *ES&T*; Hodas et al. **2013** *JESEE*; Baxter et al. **2013** *Air Qual Atmos Health*

# Goals of this work

- Develop and apply a Monte Carlo simulation tool to estimate the statistical distribution of long-term average size-resolved infiltration factors ( $F_{inf}$ ) for particles 0.001-10  $\mu\text{m}$  across the U.S. residential building stock
  - Allows for estimates of UFP and  $\text{PM}_{2.5}$  as well

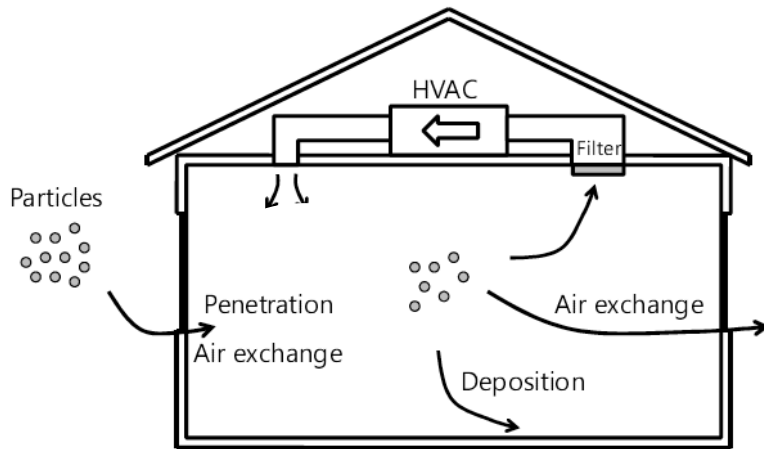
## Explore influence of key parameters:

- Air exchange rate,  $\lambda$ 
  - With and without windows open
- Particle penetration factor,  $P_i$ 
  - With and without windows open
- Deposition rates,  $k_{i,dep}$
- Removal by HVAC filter,  $\eta_{HVAC}\lambda_{HVAC}$ 
  - And filter ownership
- HVAC system runtime,  $f_{HVAC}$



$$F_{i,inf} = \frac{C_{i,in}}{C_{i,out}} = \frac{P_i \lambda}{\lambda + k_{i,dep} + \lambda_{HVAC} f_{HVAC} \eta_{i,HVAC}}$$

# Methodology: Model framework



Long-term average  
size-resolved infiltration factor

$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

Long-term average  
air exchange rates (AER,  $\lambda$ )

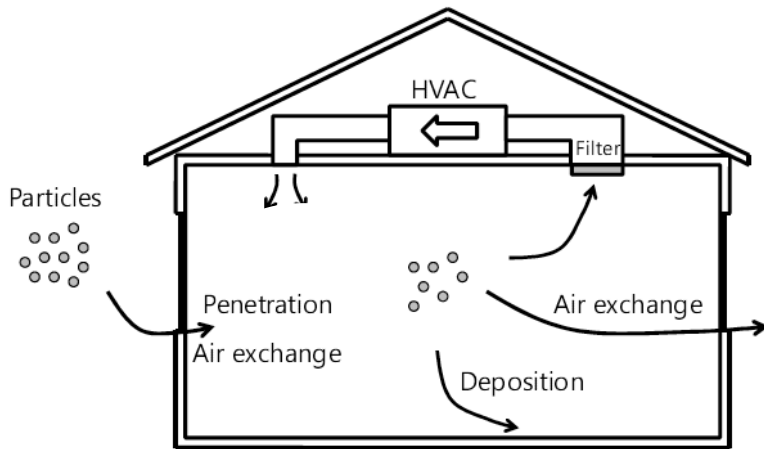
$$\lambda = \lambda_{\text{closed windows}} (1 - f_{\text{open windows}}) + \lambda_{\text{open windows}} f_{\text{open windows}}$$

$\lambda_{\text{open windows}}$  = AER during periods of window opening ( $\text{hr}^{-1}$ )

$f_{\text{open windows}}$  = fraction of time of window opening (-)

$\lambda_{\text{closed windows}}$  = AER during periods with closed windows ( $\text{hr}^{-1}$ )

# Methodology: Model framework



Long-term average  
size-resolved infiltration factor

$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

## AERs with windows open

$$\lambda_{\text{openwindows}} = \lambda_{\text{closedwindows}} \left( \phi_{\text{openwindows,low}} m_{\text{openwindows,low}} + \phi_{\text{openwindows,high}} m_{\text{openwindows,high}} \right)$$

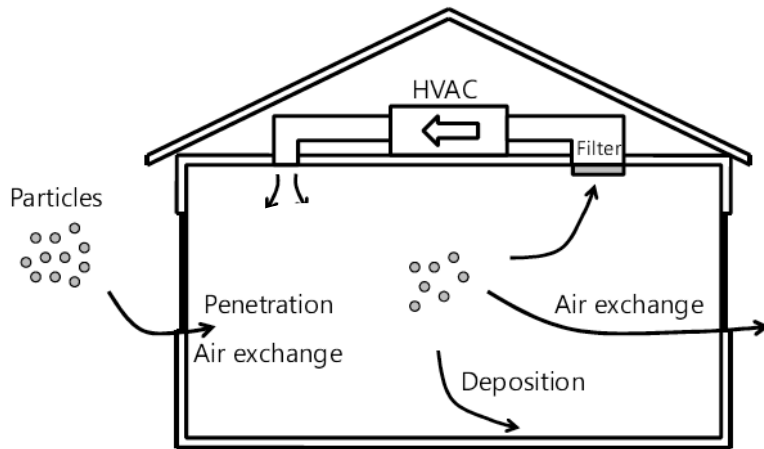
$\phi_{\text{openwindows,low}}$  = probability of low window opening (-)

$\phi_{\text{openwindows,high}}$  = probability of high window opening (-)

$m_{\text{openwindows,low}}$  = AER multiplier during low window opening (-)

$m_{\text{openwindows,high}}$  = AER multiplier during high window opening (-)

# Methodology: Model framework



Long-term average  
size-resolved infiltration factor

$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

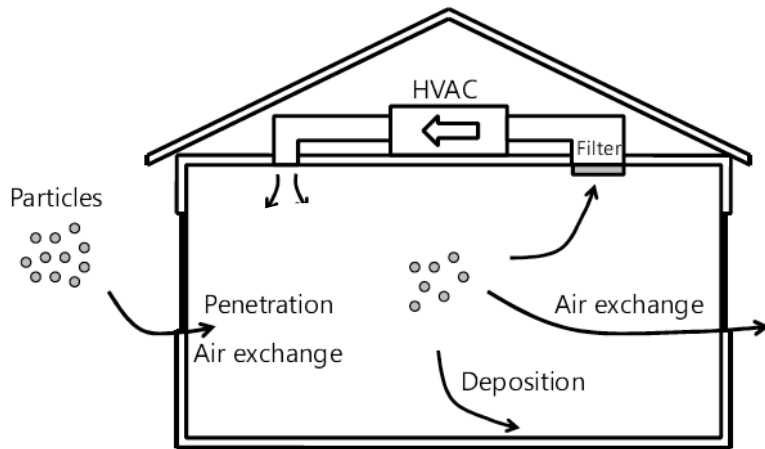
**Fraction of time windows are open**

$$f_{\text{openwindows}} = f_{\text{mild}} f_{\text{openwindows,mild}}$$

$f_{\text{mild}}$  = fraction of mild weather (-)

$f_{\text{openwindows,mild}}$  = fraction of window opening during mild weather (-)

# Methodology: Model framework



**Long-term average  
size-resolved infiltration factor**

$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

**Long-term average size-resolved envelope penetration factors**

$$P_i = P_{i,\text{closedwindows}} (1 - f_{\text{openwindows}}) + P_{i,\text{openwindows}} f_{\text{openwindows}}$$

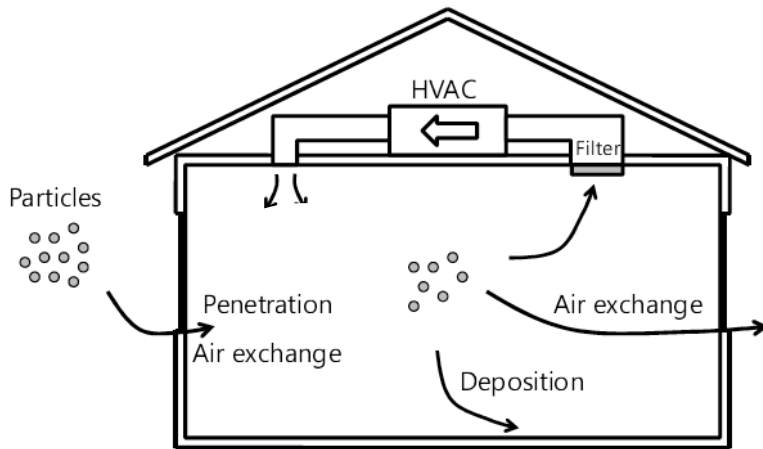
$P_{i,\text{openwindows}}$  = envelope penetration factor during periods of window opening (-)

$f_{\text{openwindows}}$  = fraction of time of window opening (-)

$P_{i,\text{closedwindows}}$  = envelope penetration factor during periods w/ closed windows (-)



# Methodology: Model framework



Long-term average  
size-resolved infiltration factor

$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

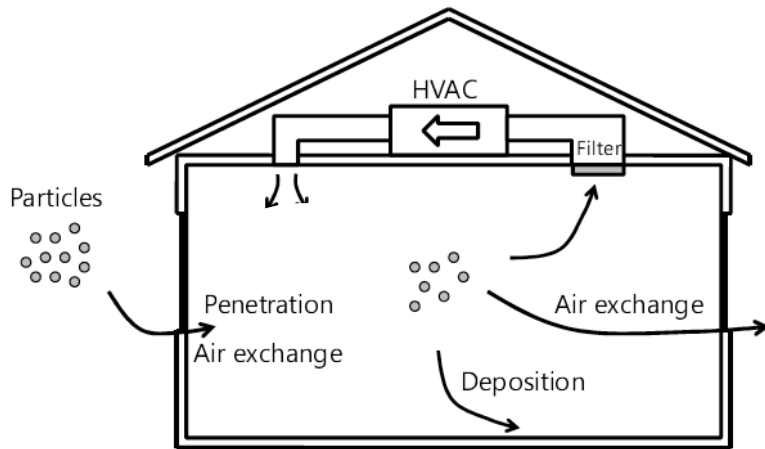
## Envelope penetration factors with open windows

$$P_{i,\text{openwindows}} = P_{i,\text{openwindows,low}} \phi_{\text{openwindows,low}} + P_{i,\text{openwindows,high}} \phi_{\text{openwindows,high}}$$

$\phi_{\text{openwindows,low}}$  = probability of low window opening (-)

$\phi_{\text{openwindows,high}}$  = probability of high window opening (-)

# Methodology: Model framework



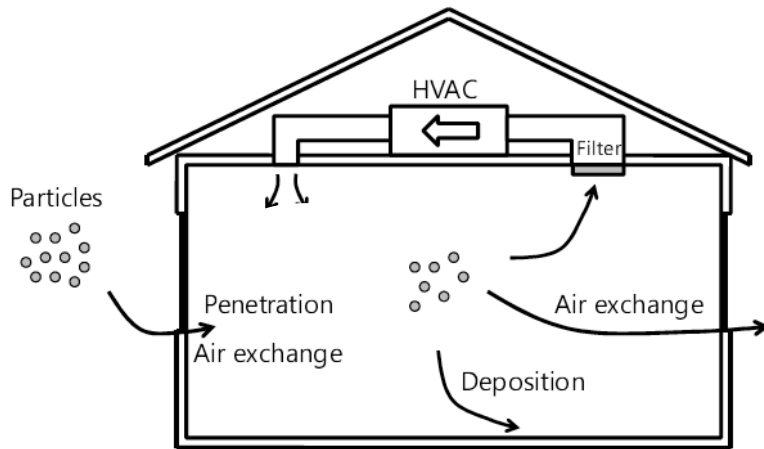
Long-term average  
size-resolved infiltration factor

$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

**Envelope penetration factors with open windows (scales with AER)**

$$P_{i,\text{openwindows,low}} = P_{i,\text{closedwindows}} \frac{\lambda_{\text{closedwindows}}}{\lambda_{\text{openwindows,low}}} + (1) \frac{\lambda_{\text{openwindows,low}} - \lambda_{\text{closedwindows}}}{\lambda_{\text{openwindows,low}}}$$

# Methodology: Model framework



Long-term average  
size-resolved infiltration factor

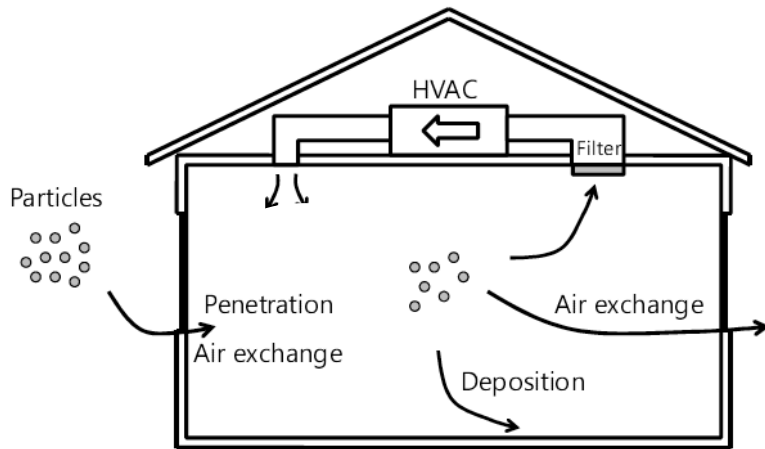
$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

Long-term average size-resolved particle deposition rates

$$k_{i,\text{dep}} = k_{i,\text{dep},\text{closedwindows}} (1 - f_{\text{openwindows}}) + k_{i,\text{dep},\text{openwindows}} f_{\text{openwindows}}$$

$$k_{i,\text{dep},\text{openwindows}} = k_{i,\text{dep},\text{openwindows},\text{low}} \phi_{\text{openwindows},\text{low}} + k_{i,\text{dep},\text{openwindows},\text{high}} \phi_{\text{openwindows},\text{high}}$$

# Methodology: Model framework



Long-term average  
size-resolved infiltration factor

$$F_{i,\text{inf}} = \frac{C_{i,\text{in}}}{C_{i,\text{out}}} = \frac{P_i \lambda}{\lambda + k_{i,\text{dep}} + \lambda_{\text{HVAC}} f_{\text{HVAC}} \eta_{i,\text{HVAC}}}$$

**HVAC recirculation rates, fractional operation times, and filter efficiency**

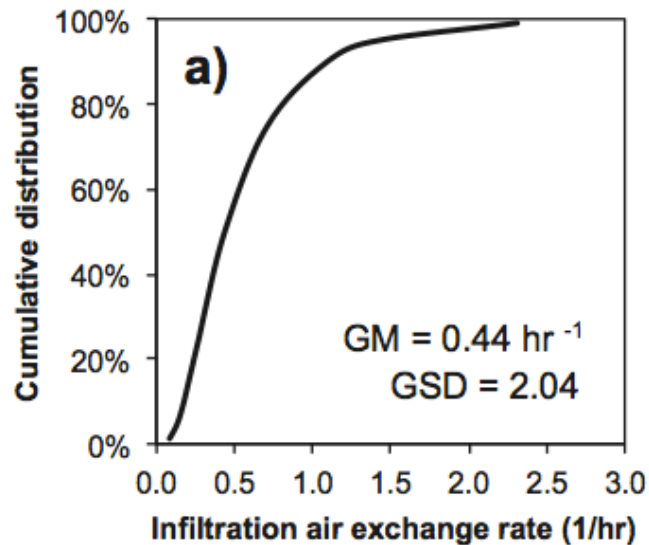
Culled directly from the literature

# Methodology: Gathering input parameters

- Large literature review identified best estimates of distributions of input parameters across the US residential building stock

## Infiltration AER

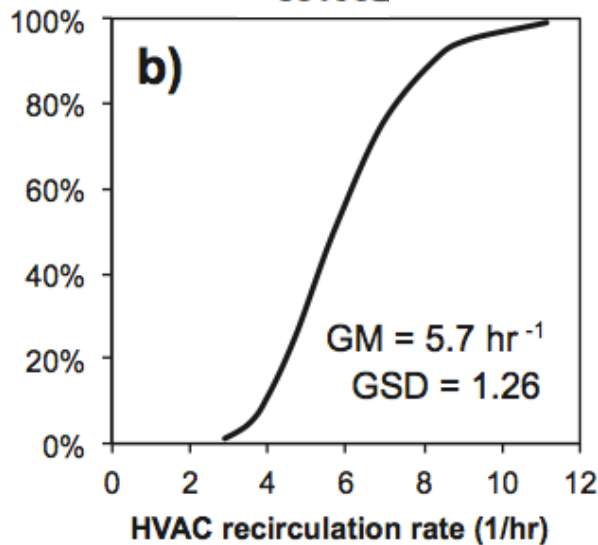
$\lambda_{\text{closed windows}}$



Persily et al. 2010 *Indoor Air*

## Recirculation rate

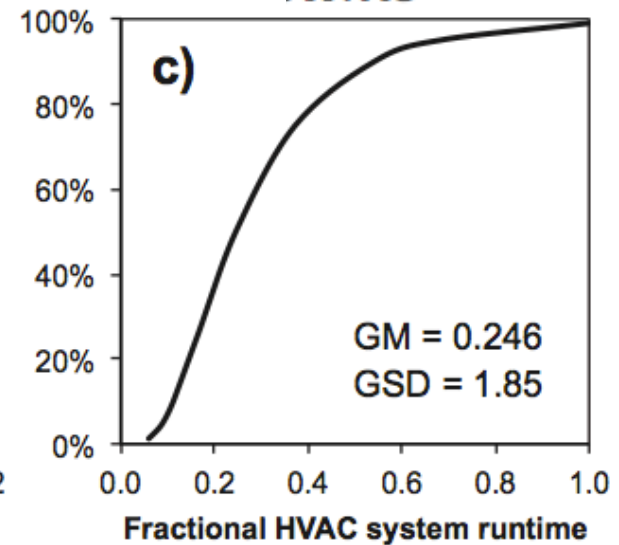
$\lambda_{\text{HVAC}}$



Stephens et al. 2011 *Build Environ*

## HVAC runtime

$f_{\text{HVAC}}$



Thornburg et al. 2004 *Atmos Environ*  
Stephens et al. 2011 *Build Environ*

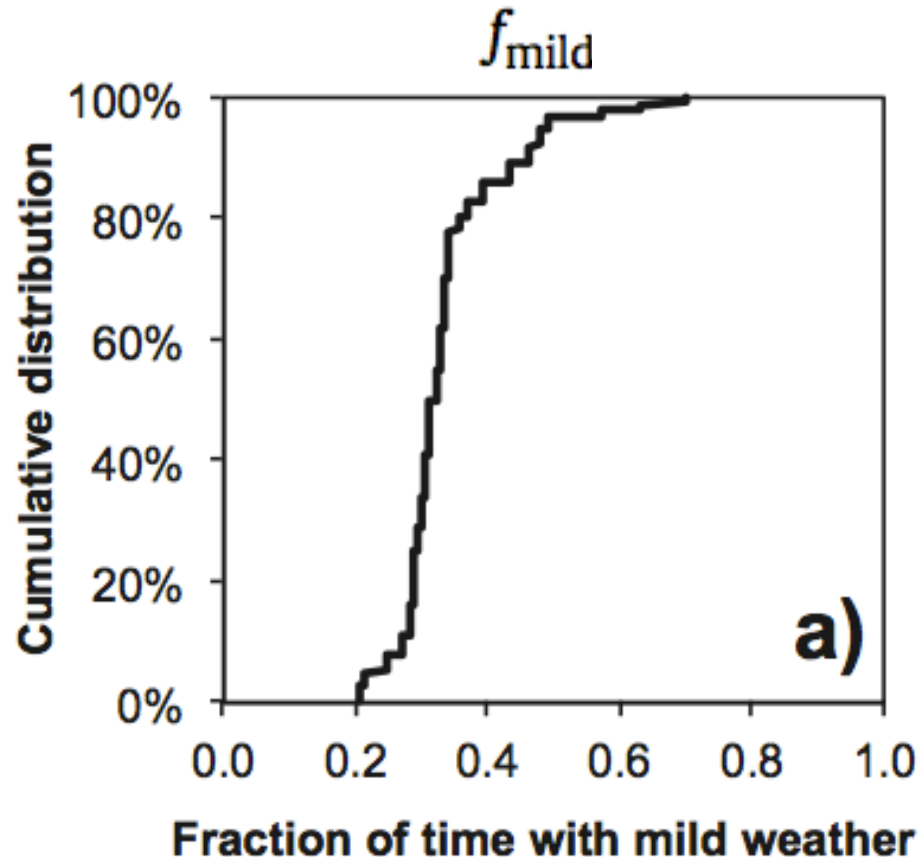
## AER multipliers:

2 when open 'low' amount

4 when open 'high' amount

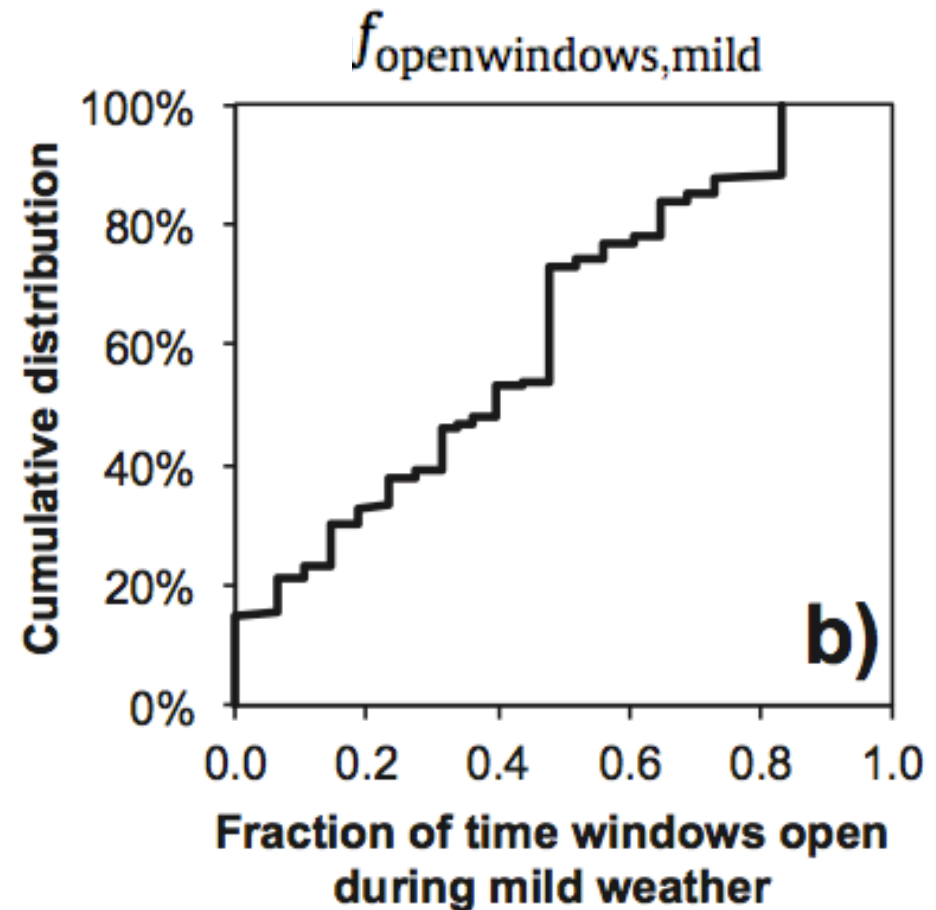
# Methodology: Gathering input parameters

Fraction of mild weather



Chen et al. 2012 *Epidemiology*

Fraction of window opening during mild weather



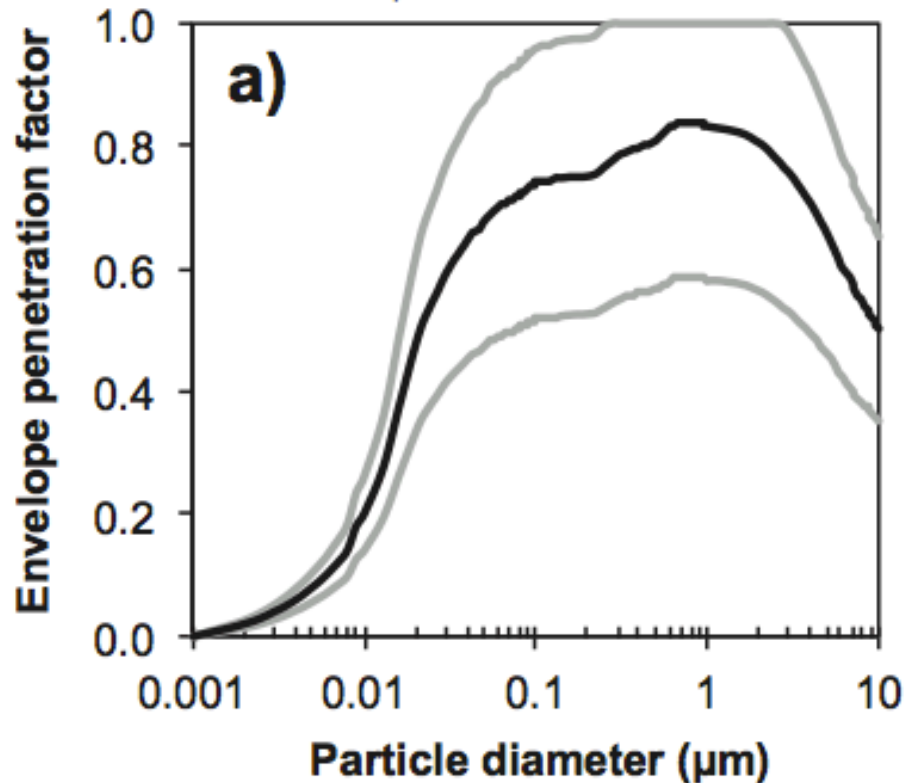
Price and Sherman 2006 *LBNL 59620*

80% open 'low' amount  
20% open 'high' amount

# Methodology: Gathering input parameters

## Envelope penetration factor

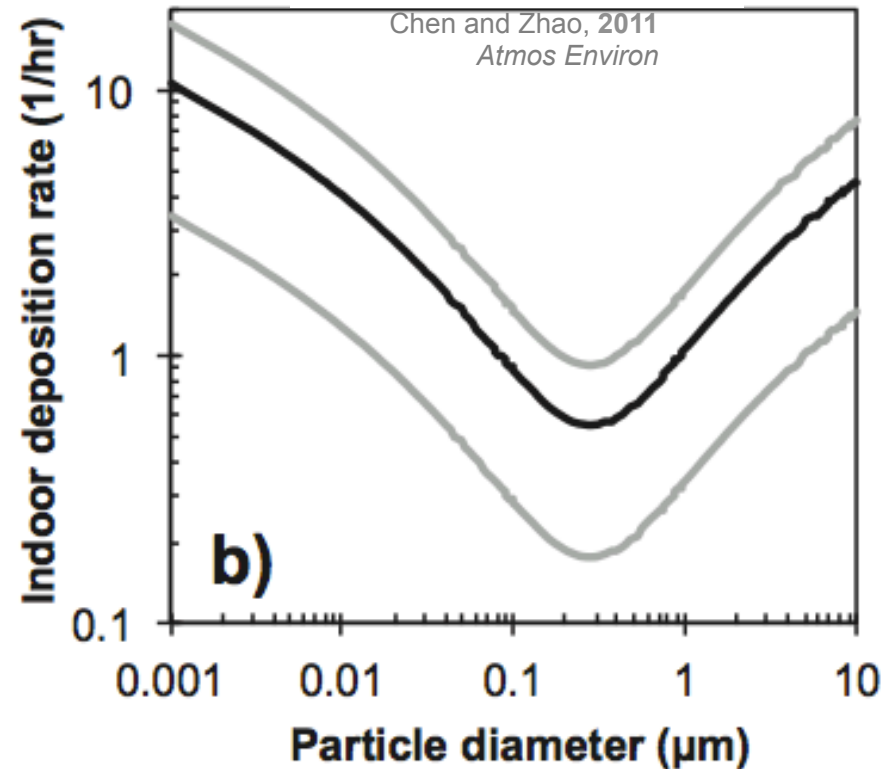
$$P_{i,\text{closedwindows}}$$



Chen and Zhao 2011 *Atmos Environ*  
 Rim et al. 2010 *Environ Sci Technol*  
 Stephens and Siegel 2012 *Indoor Air*  
 Williams et al. 2003 *Atmos Environ*

## Deposition rate

$$k_{i,\text{dep,closedwindows}}$$



Adjusted from He et al. 2005 *Atmos Environ*

**$k_{i,\text{dep}}$  multipliers:**

1.2 when windows open 'low' amount

1.7 when windows open 'high' amount

He et al. 2005 & assumed to vary with AER multipliers

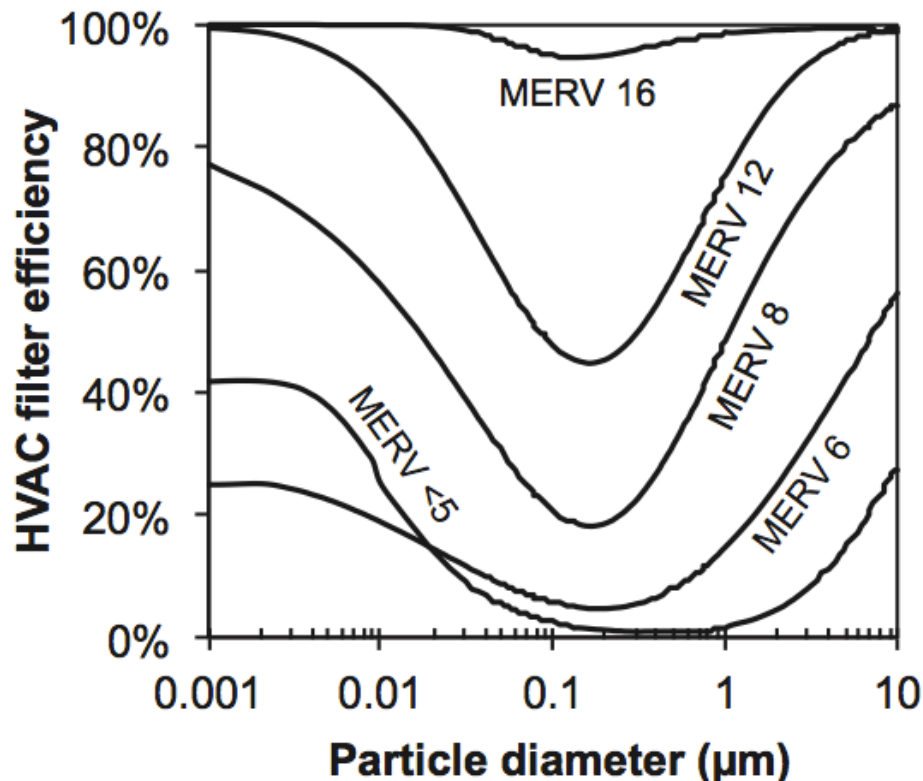
# Methodology: Gathering input parameters

Estimate of HVAC filter ownership across the residential building stock (for homes with HVAC systems).

Filter type	% Ownership
MERV < 5	25%
MERV 6	30%
MERV 8	30%
MERV 12	10%
MERV 16	5%

## Filter ownership

Stephens and Siegel **2012** *Indoor Air*  
Offermann **2009** *CARB Report*  
Anonymous filtration industry contacts



## Filter efficiency

$$\eta_{i,HVAC}$$

Hecker and Hofacre **2008** *EPA*  
Waring and Siegel **2008** *Indoor Air*



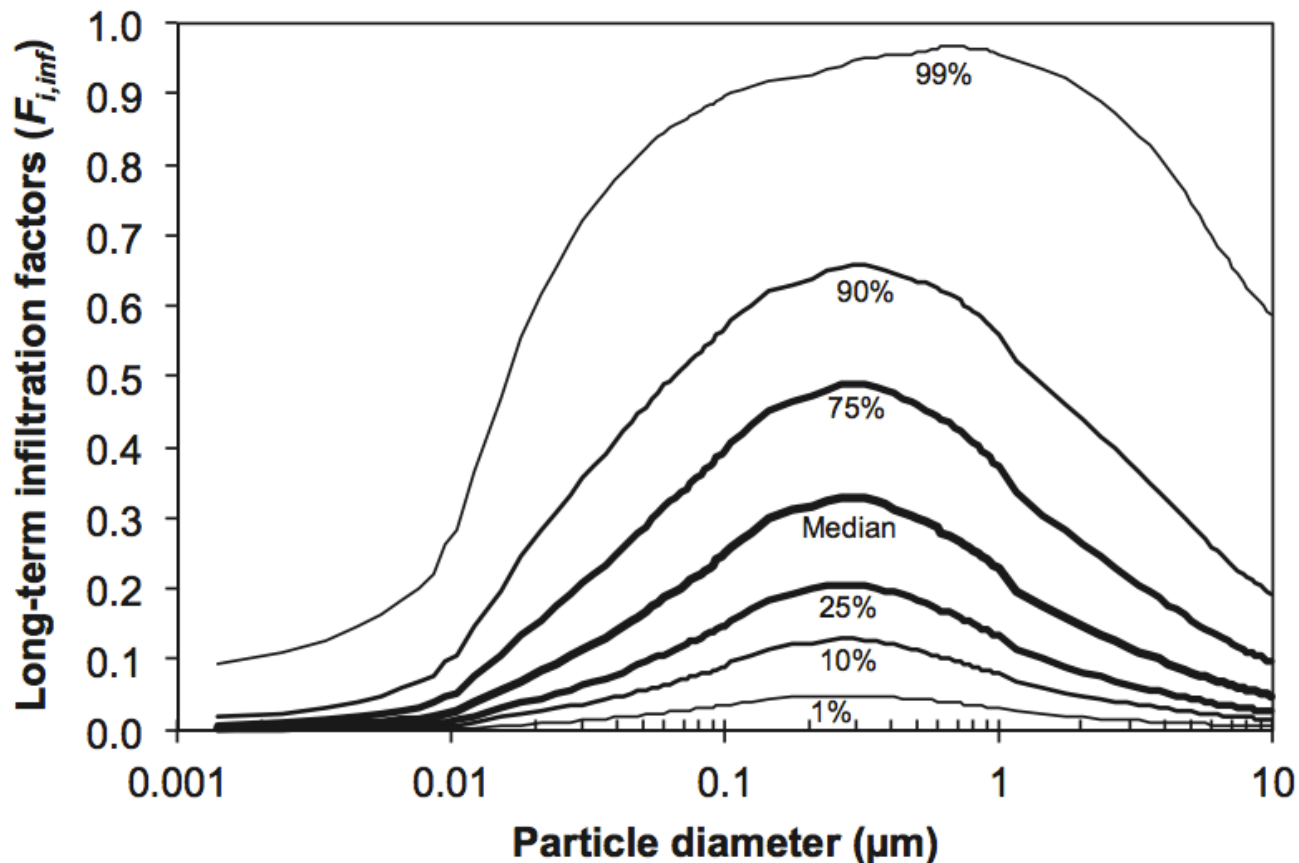
# Methodology for simulations

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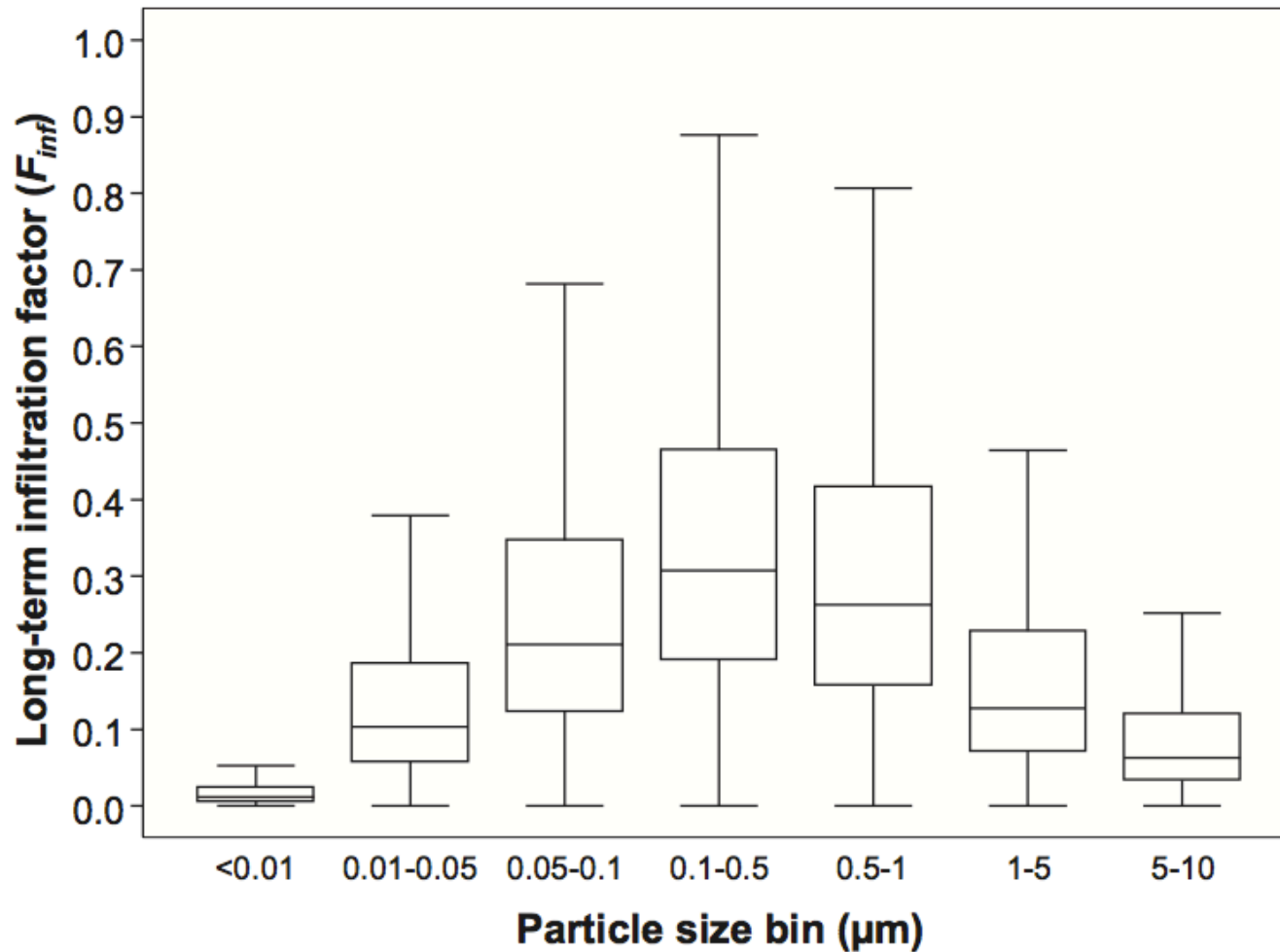
- A Monte Carlo simulation was used to model long-term average infiltration factors for 100,000 homes across the U.S. residential building stock using these best available data for input parameters
- Long term parameters were calculated as a combination of infiltration parameters and open-window parameters
- Size-resolved simulations (0.001 to 10  $\mu\text{m}$ )
- We assumed that our sample of homes was comprised of:
  - 65% of homes own HVAC systems HUD 2007
    - Filters ranging from MERV <5 to MERV 16
  - 35% of homes without HVAC systems (no filtration) HUD 2007

# Results: Long-term average size-resolved $F_{inf}$

Infiltration factors were predicted to be **20-100 higher** in the **most protective homes** (1st percentile) vs. the least protective ones (99<sup>th</sup> percentile)

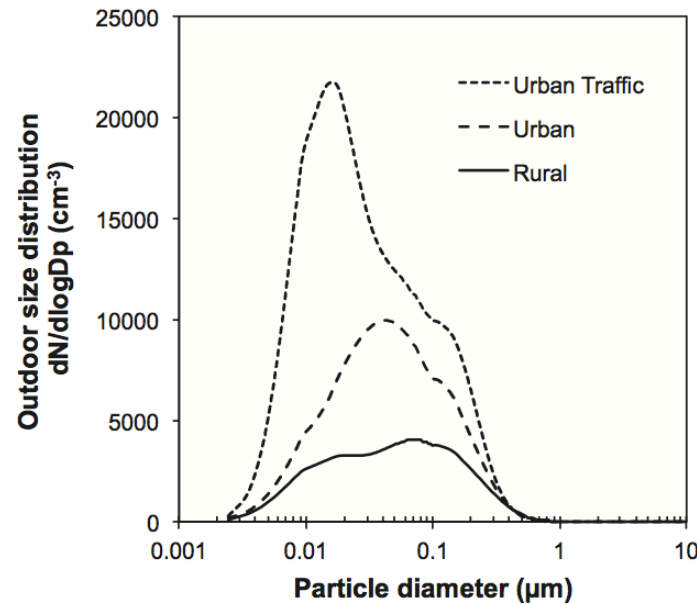


# Results: Long-term average binned $F_{inf}$

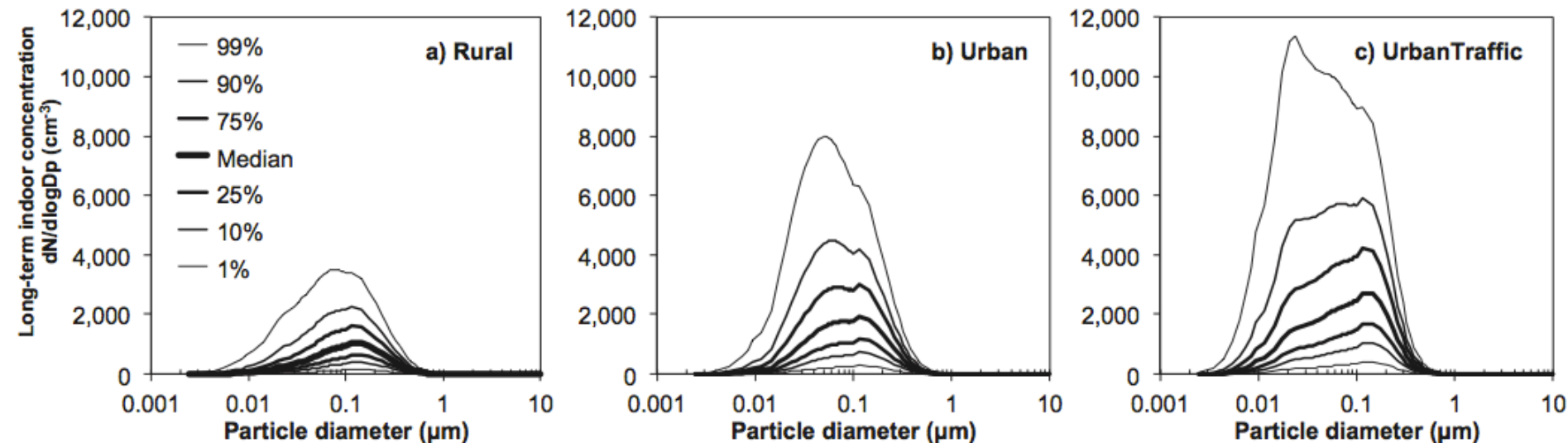


UFP estimates generally in line with measurements in Kearney et al. 2011  
*Atmos Environ*: 0.03-0.9, median of 0.19-0.27, and others

# Results: Mapping to outdoor size distributions

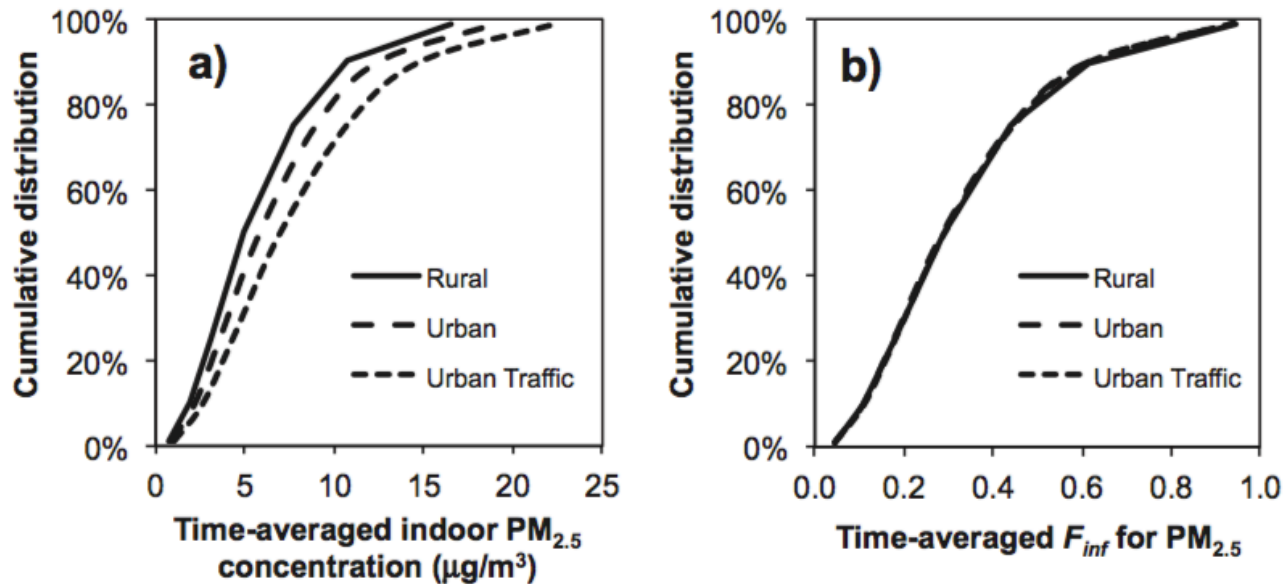


Costabile et al 2009  
*Atmos Phys Chem*

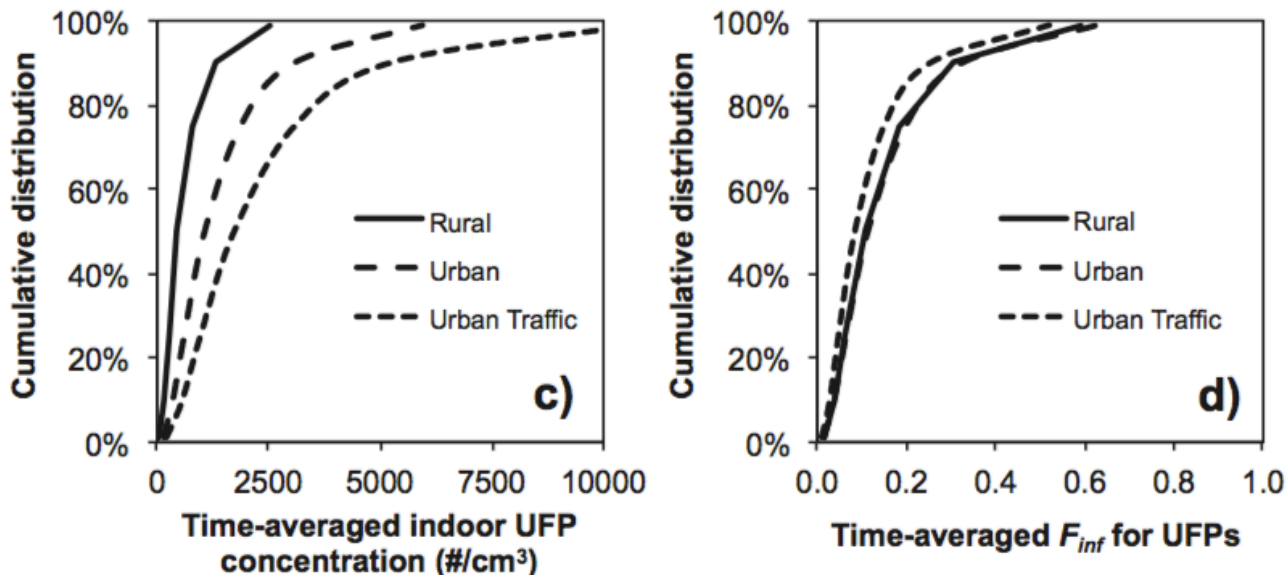


# Results: Predicting CDFs of UFPs and PM<sub>2.5</sub>

PM<sub>2.5</sub>



UFPs  
(< 100 nm)



# Results: Multiple regression for influential factors

## Largest influences

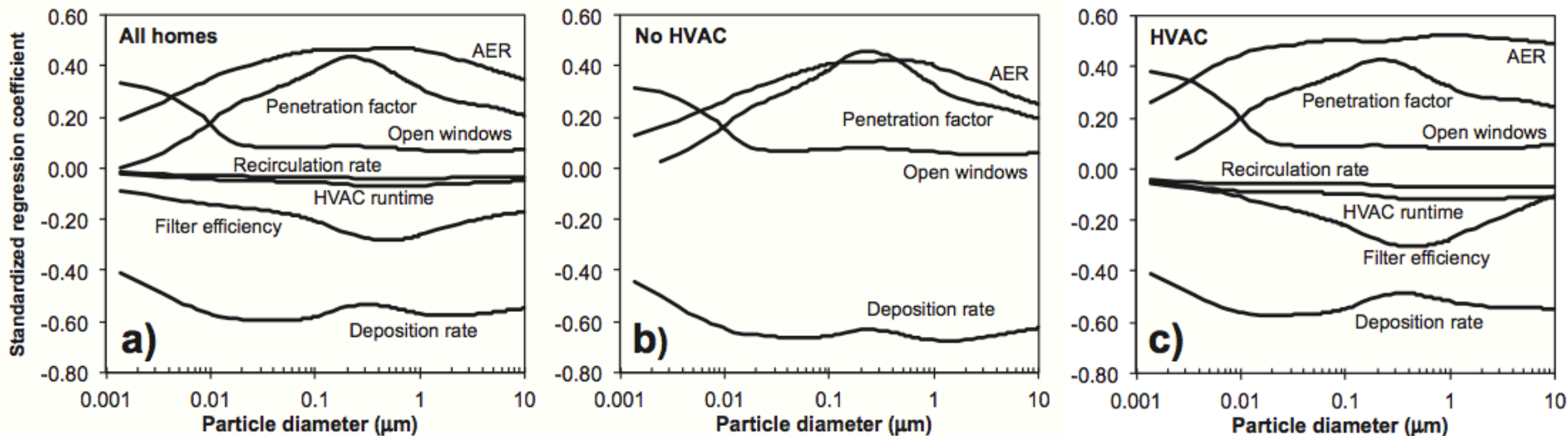
- (1) Closed-window deposition rates
- (2) Closed-window AER
- (3) Closed-window penetration factor
- (4) HVAC filter efficiency

## MLR

$$F_{i,\text{inf}} = \beta_0 + \beta_1 \lambda_{\text{closedwindows}} + \beta_2 f_{\text{openwindows}} + \beta_3 f_{\text{HVAC}} + \beta_4 \lambda_{\text{HVAC}} + \beta_5 \eta_{i,\text{HVAC}} + \beta_6 k_{i,\text{dep,closedwindows}} + \beta_7 P_{i,\text{closedwindows}}$$

*Model  $R^2$  values ranged 0.35 to 0.79 depending on particle size*

## Standardized regression coefficients (size-resolved)



# Limitations and future research

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- Need more accurate measurements of the important predictors in a larger number and variety of buildings
  - Deposition rates, air exchange rates, and size-resolved penetration factors
- Need more accurate distributions of HVAC system runtimes, filter efficiencies, filter ownership, and window opening behaviors
- Need more information about U.S. outdoor particle size distributions
  - Although size distribution may not have a large impact on UFPs/PM<sub>2.5</sub>
- Need to incorporate indoor sources into the Monte Carlo model
- Can also use this approach to model inhalation exposures with different individuals with different human activity patterns
- Need more information on correlation between input parameters in order to incorporate and improve this model
  - e.g. P and AER

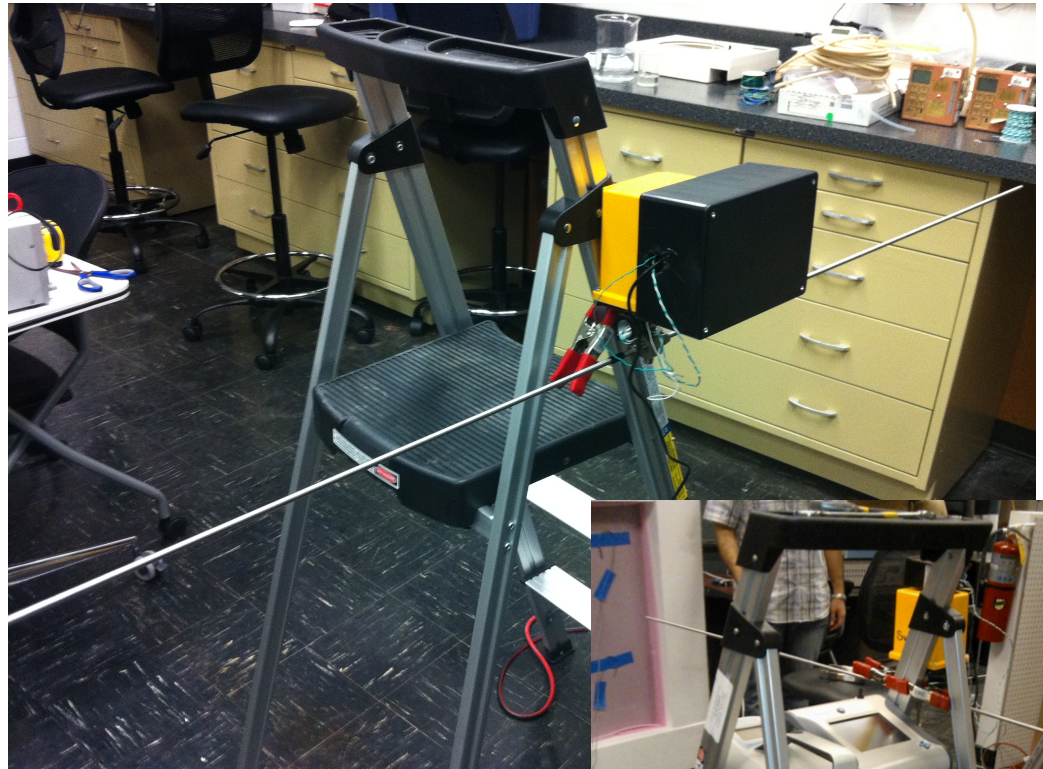


# Next steps: PM infiltration measurements in Chicago



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email: [brent@iit.edu](mailto:brent@iit.edu)



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